

Almanac

**Generic Field Level Inference for Full-Sky Cosmological Fields
and Angular Power Spectra**

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(Oskar Klein Centre, Stockholm University & Imperial College London)**

The Almanac Team



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Prof. Andrew Jaffe

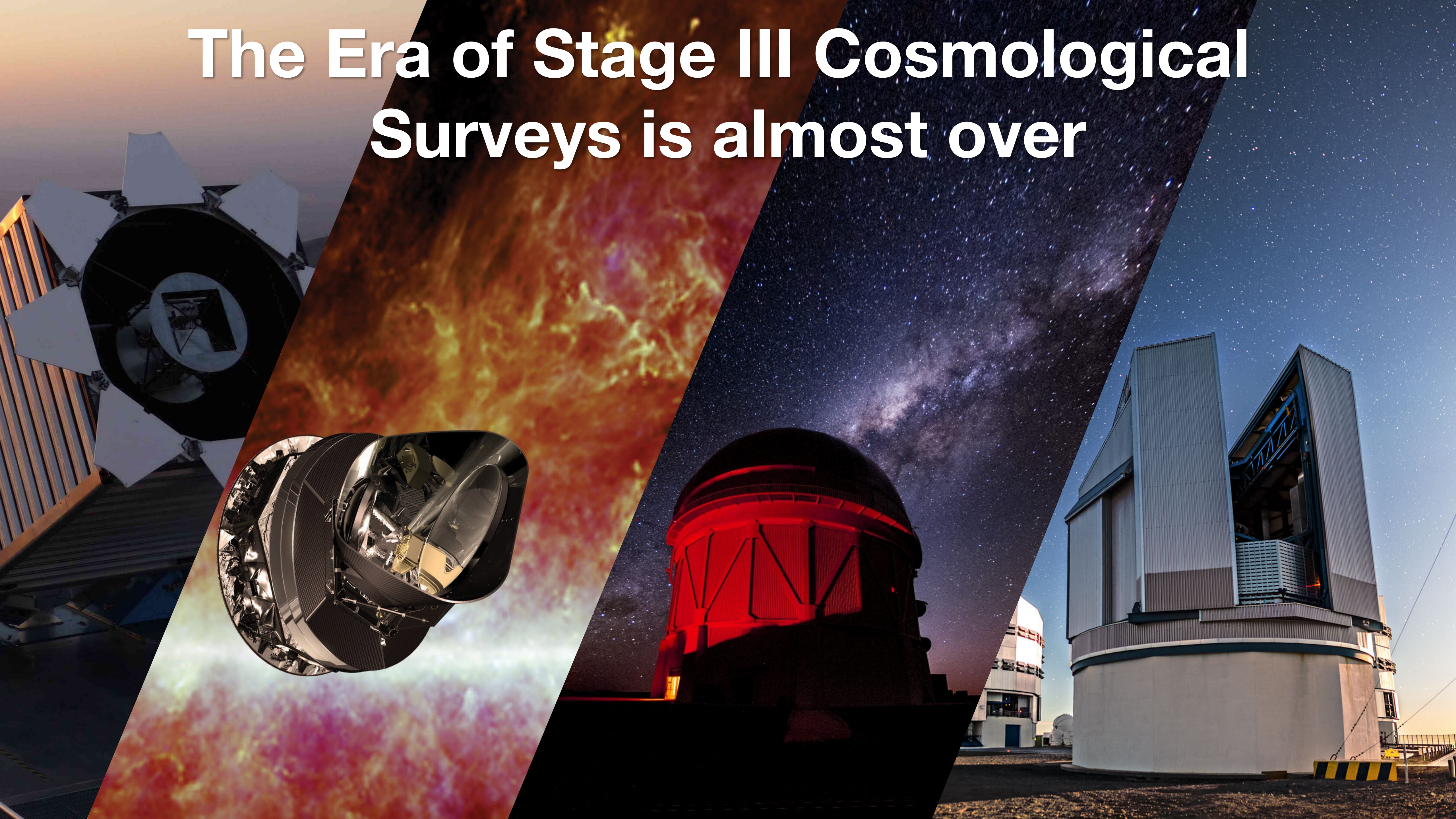


+ Javier S. Lafaurie

1. Observational Cosmology

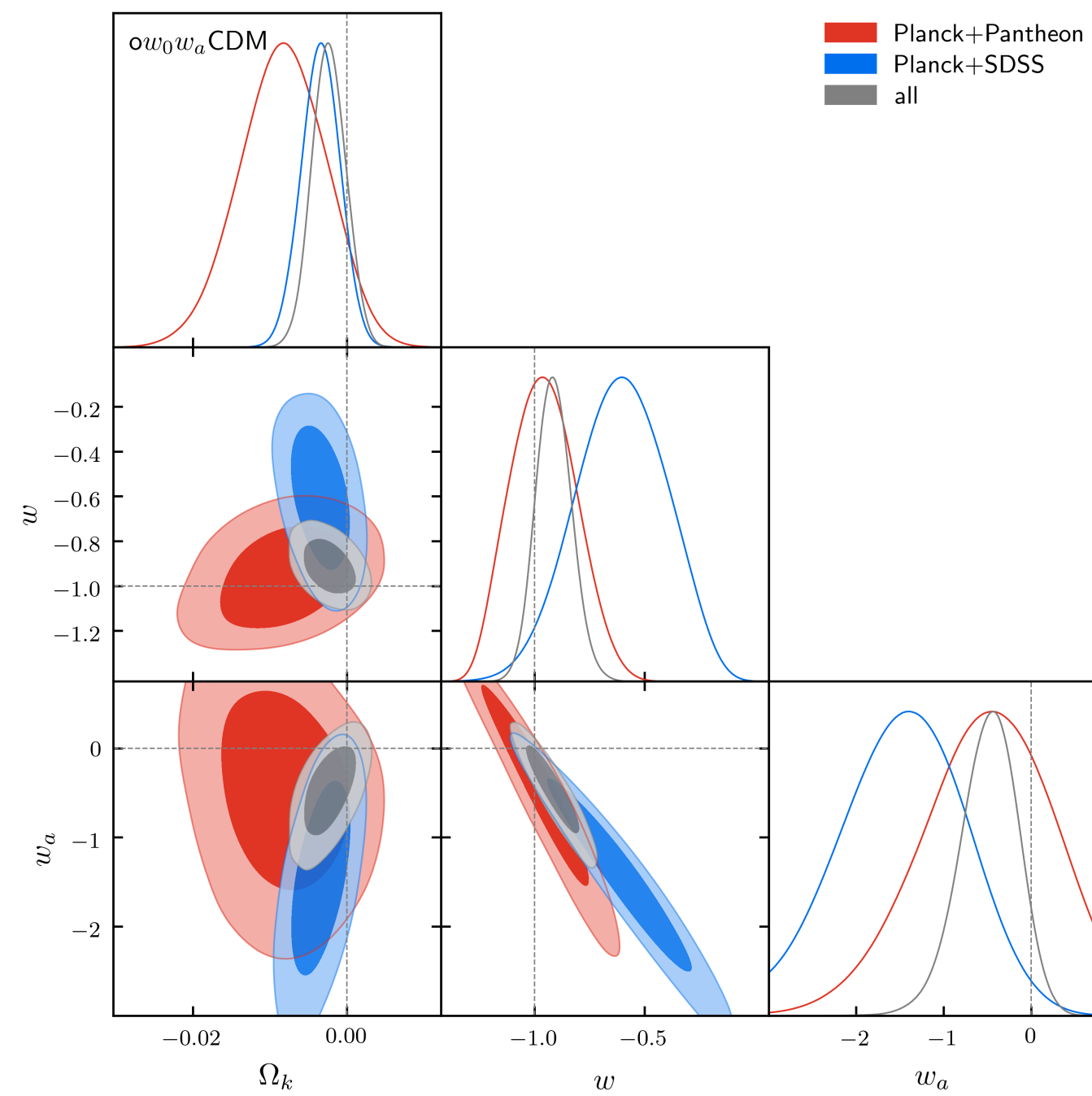
Where are we, and where are we going?

The Era of Stage III Cosmological Surveys is almost over

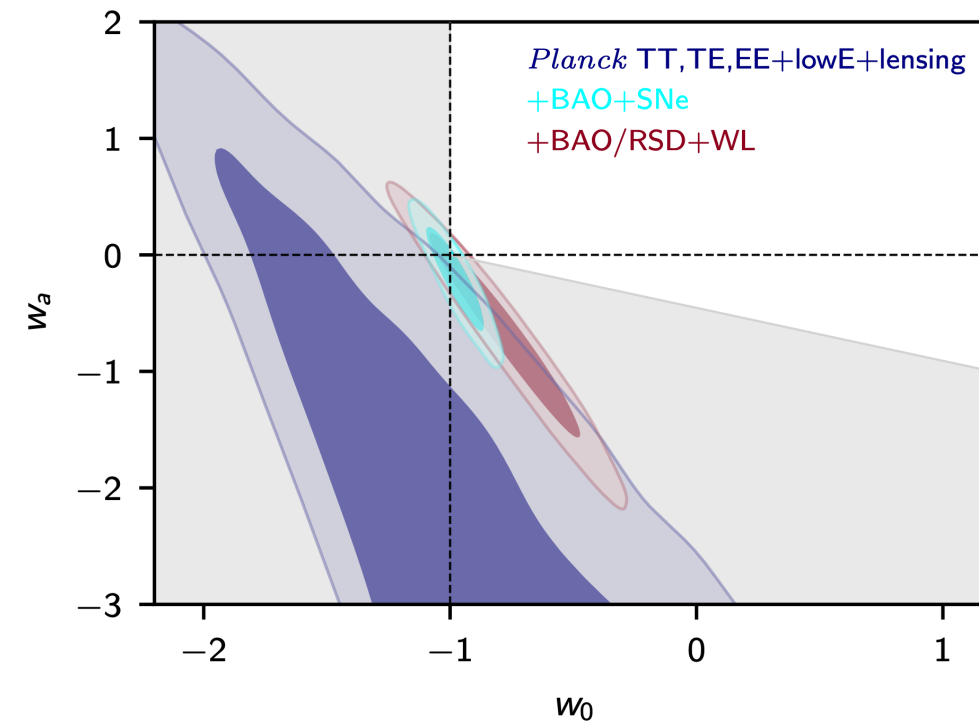


Stage III Surveys

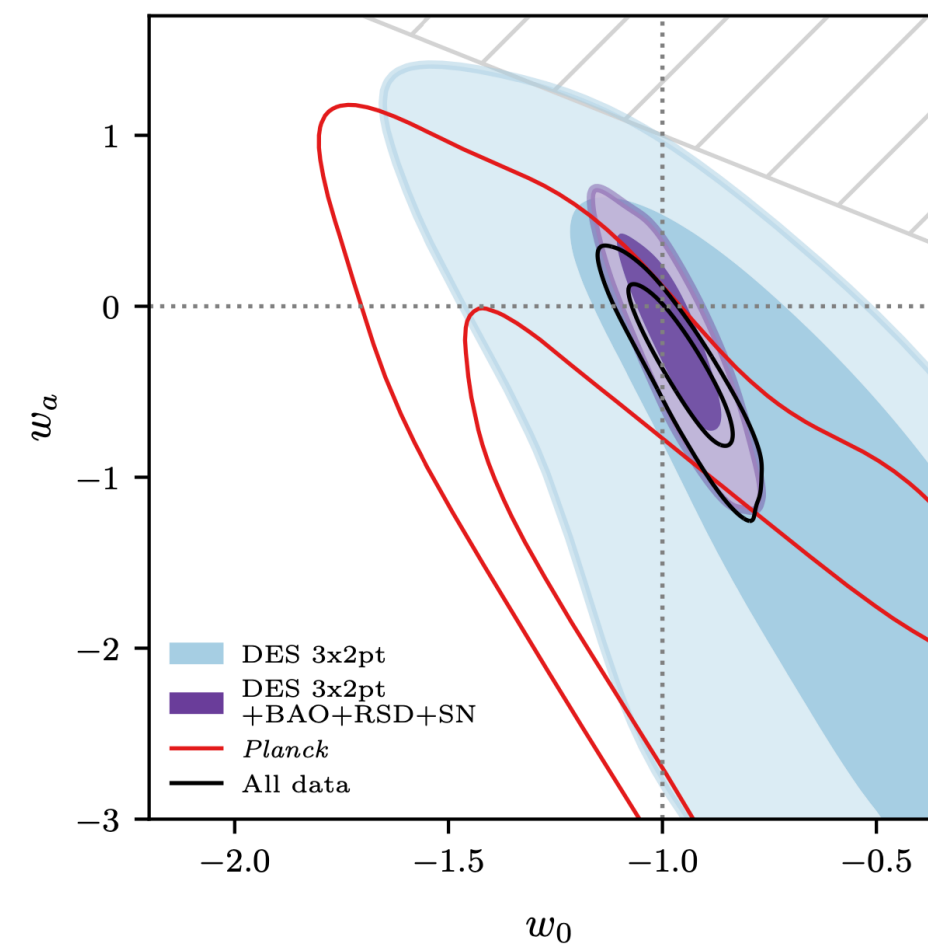
“It’s Λ CDM whether you like it or not...”



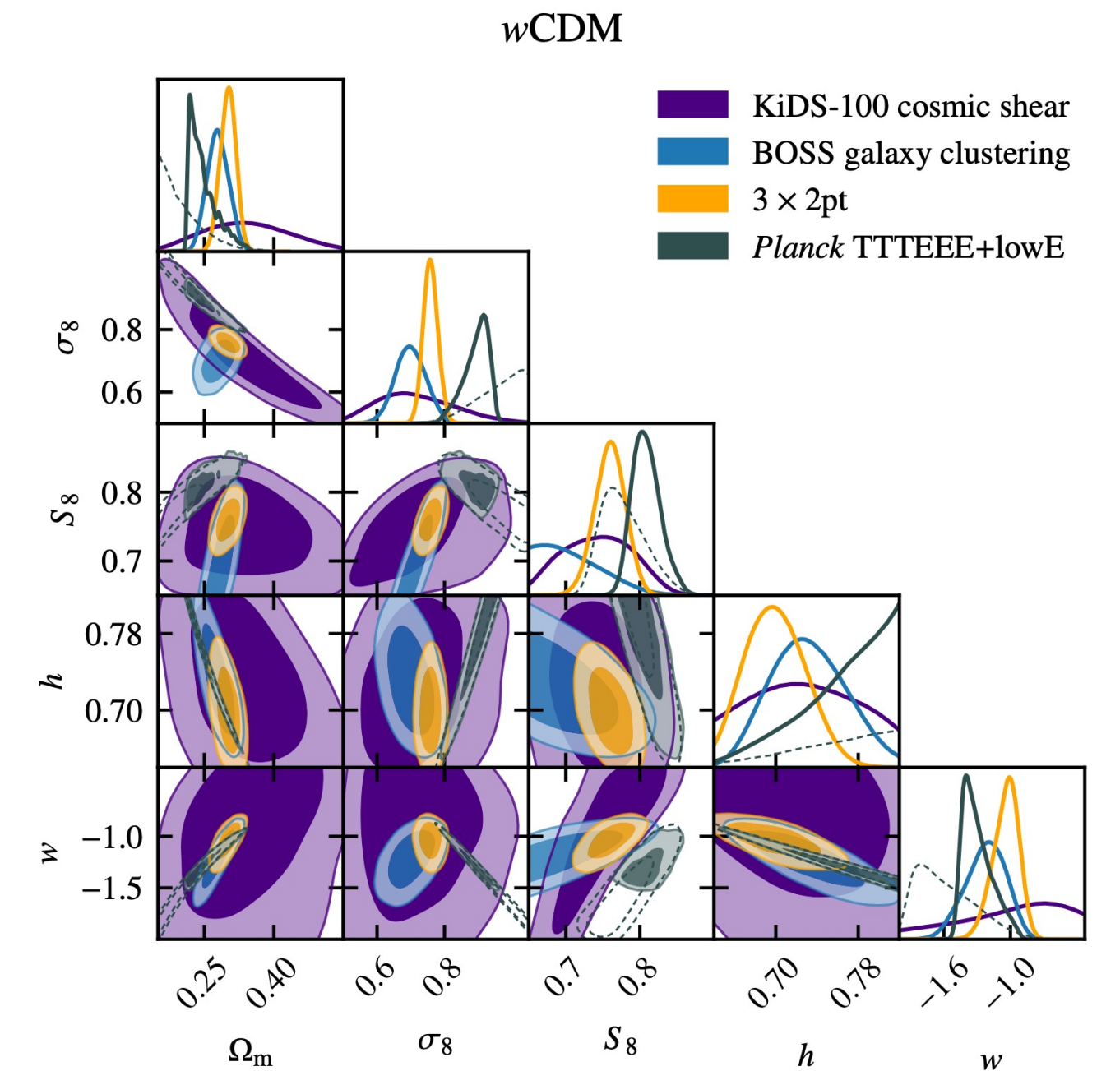
eBOSS Collaboration
(Alam et al. 2021)



Planck Collaboration, 2018



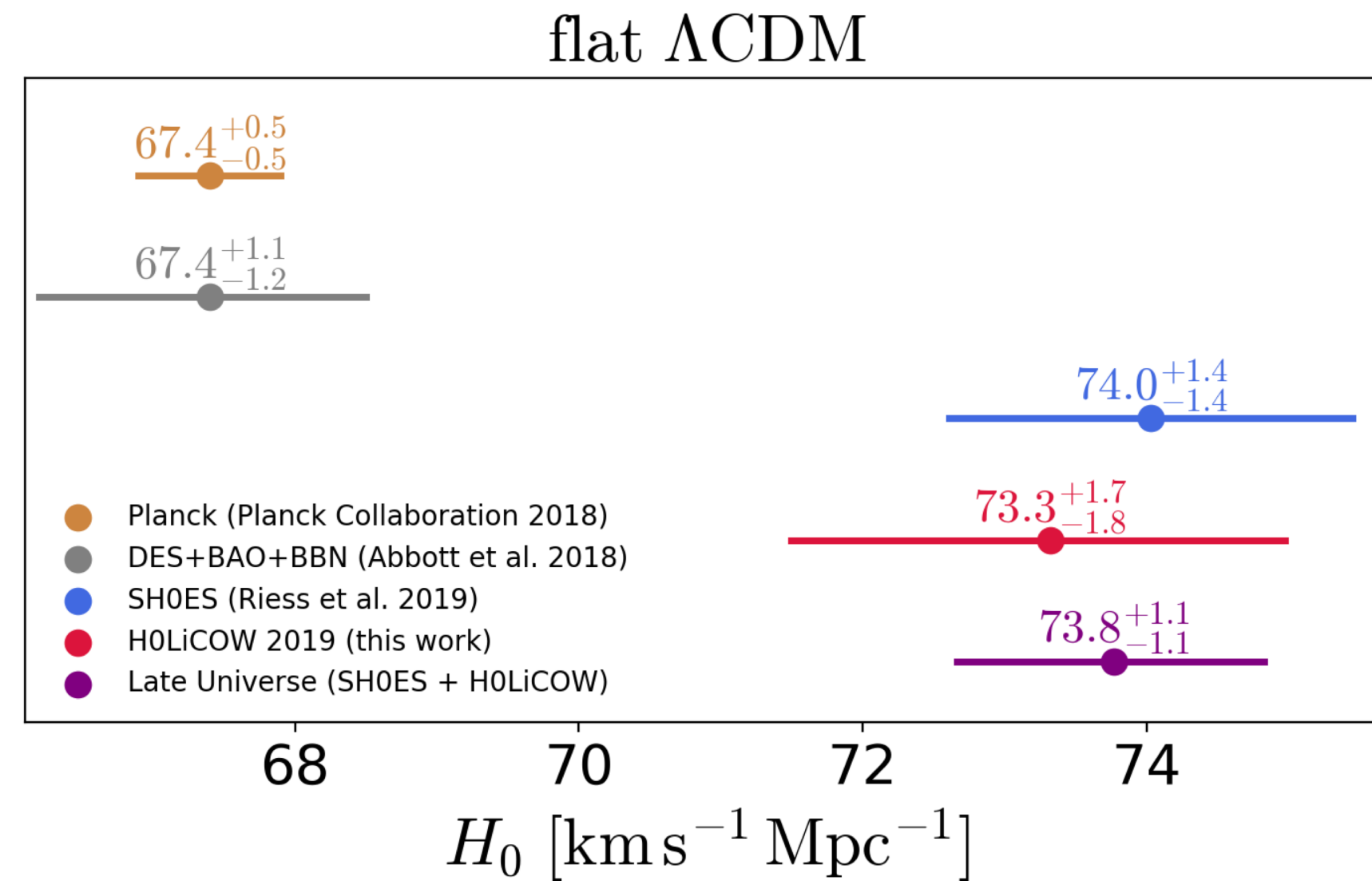
Dark Energy Survey, 2022



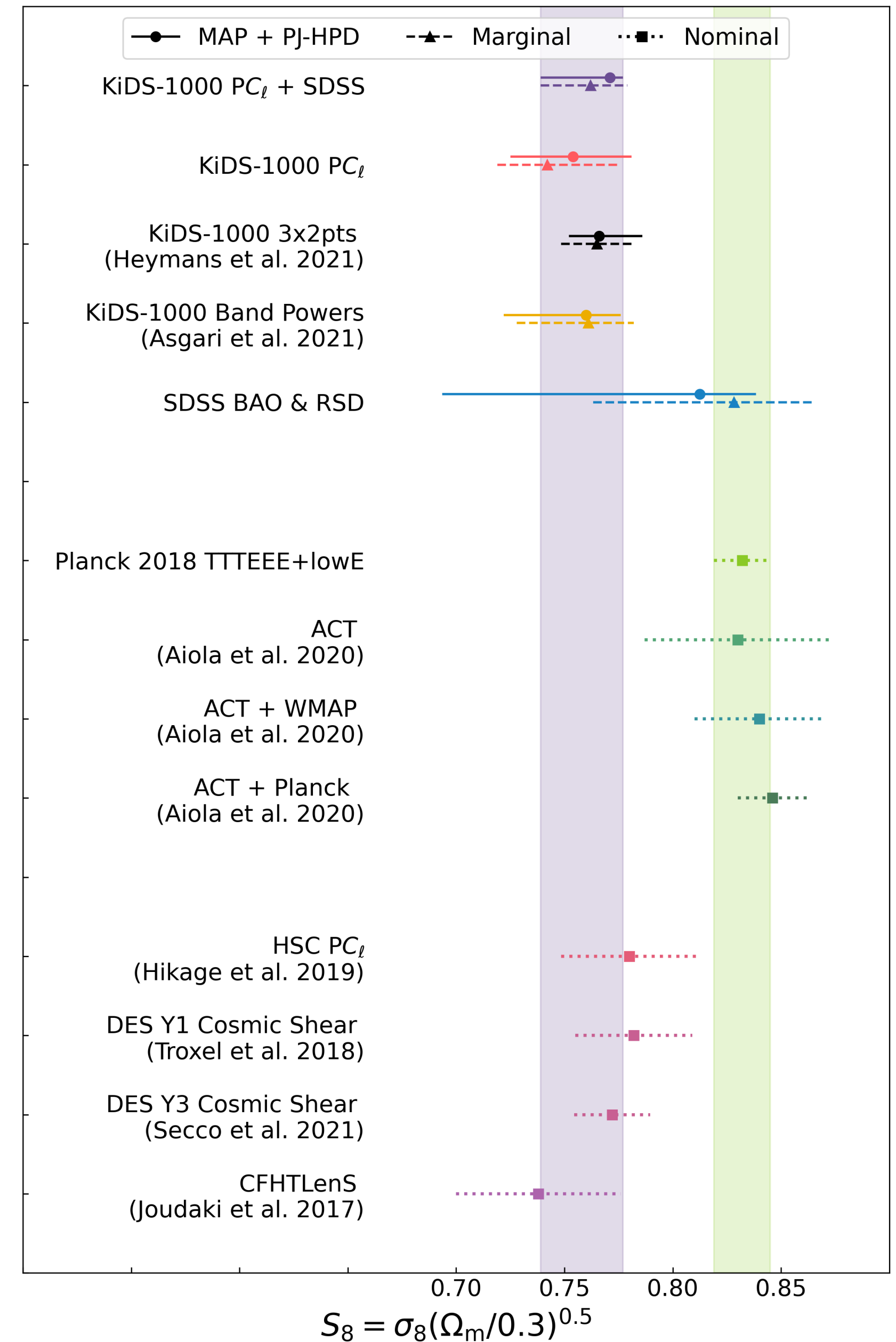
KiDS Collaboration
(Tröster et al., 2020)

Stage III Surveys

“It’s Λ CDM whether you like it or not...”
OR NOT



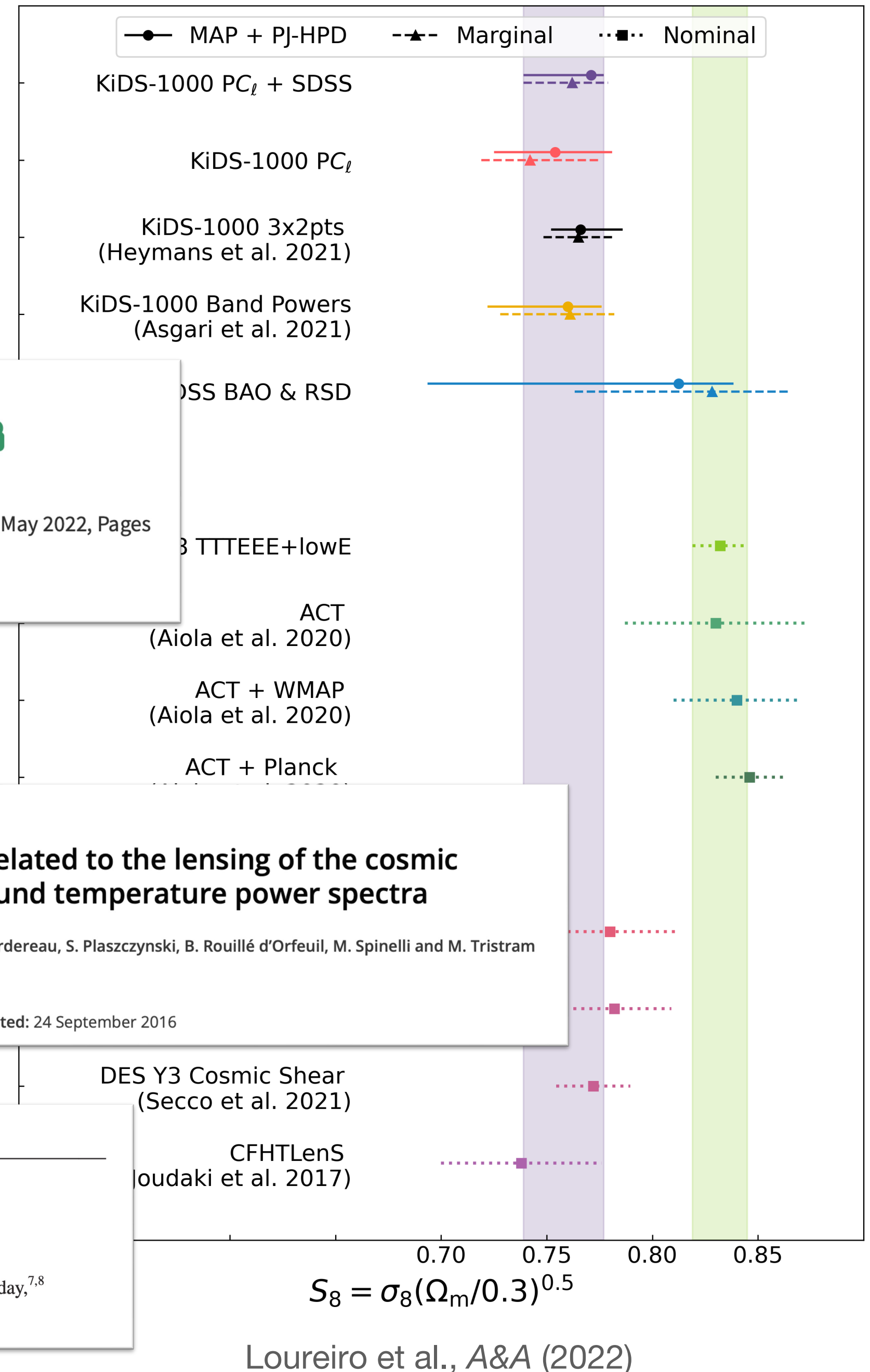
Wong et al. 2019



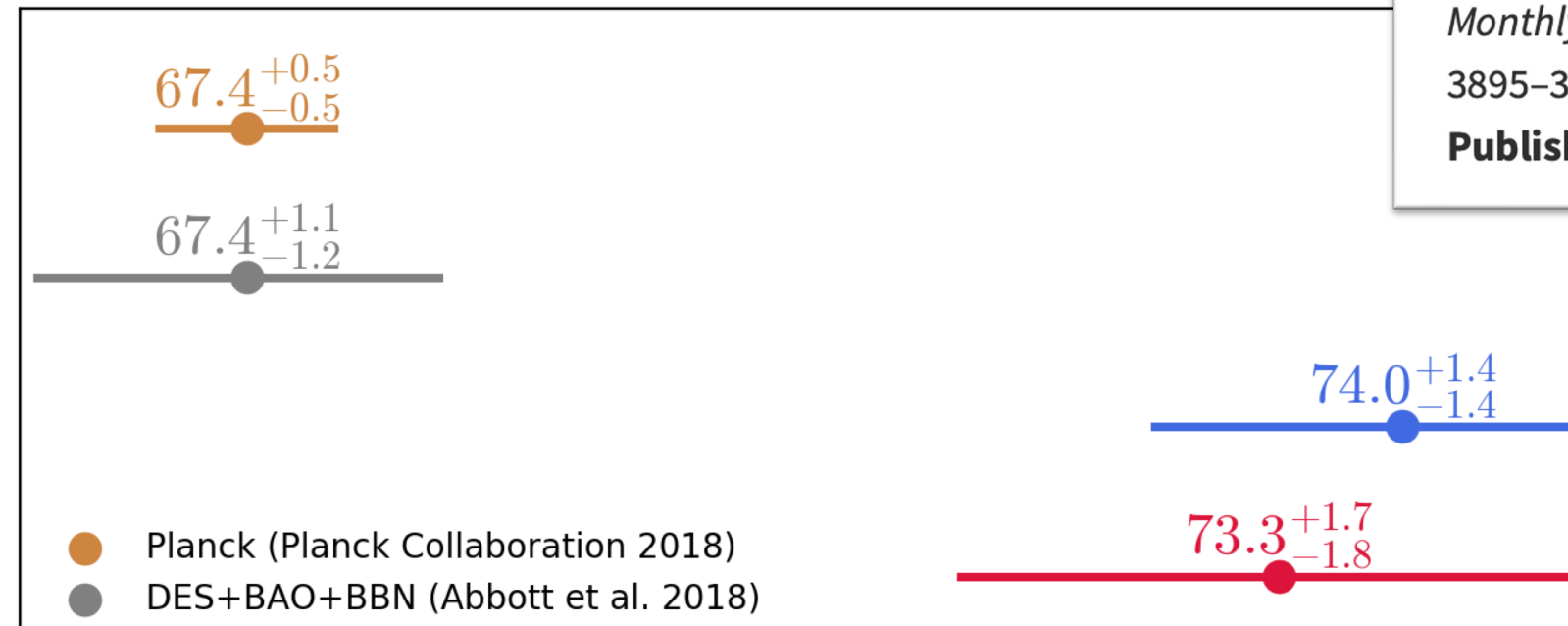
Loureiro et al., A&A (2022)

Stage III Surveys

“It’s Λ CDM whether you like it or not...”
OR NOT



flat Λ CDM



JOURNAL ARTICLE

On the kinematic cosmic dipole tension

Charles Dalang ✉, Camille Bonvin

Monthly Notices of the Royal Astronomical Society, Volume 512, Issue 3, May 2022, Pages 3895–3905, <https://doi.org/10.1093/mnras/stac726>

Published: 17 March 2022 Article history ▾

Article | Published: 04 November 2019

Planck evidence for a closed Universe and a possible crisis for cosmology

Eleonora Di Valentino, Alessandro Melchiorri ✉ & Joseph Silk

Nature Astronomy 4, 196–203 (2020) | [Cite this article](#)

A&A 597, A126 (2017)

Relieving tensions related to the lensing of the cosmic microwave background temperature power spectra

F. Couchot, S. Henrot-Versillé, O. Perdereau, S. Plaszczynski, B. Rouillé d’Orfeuil, M. Spinelli and M. Tristram

Received: 13 November 2015 | Accepted: 24 September 2016

Wong et al. 2019

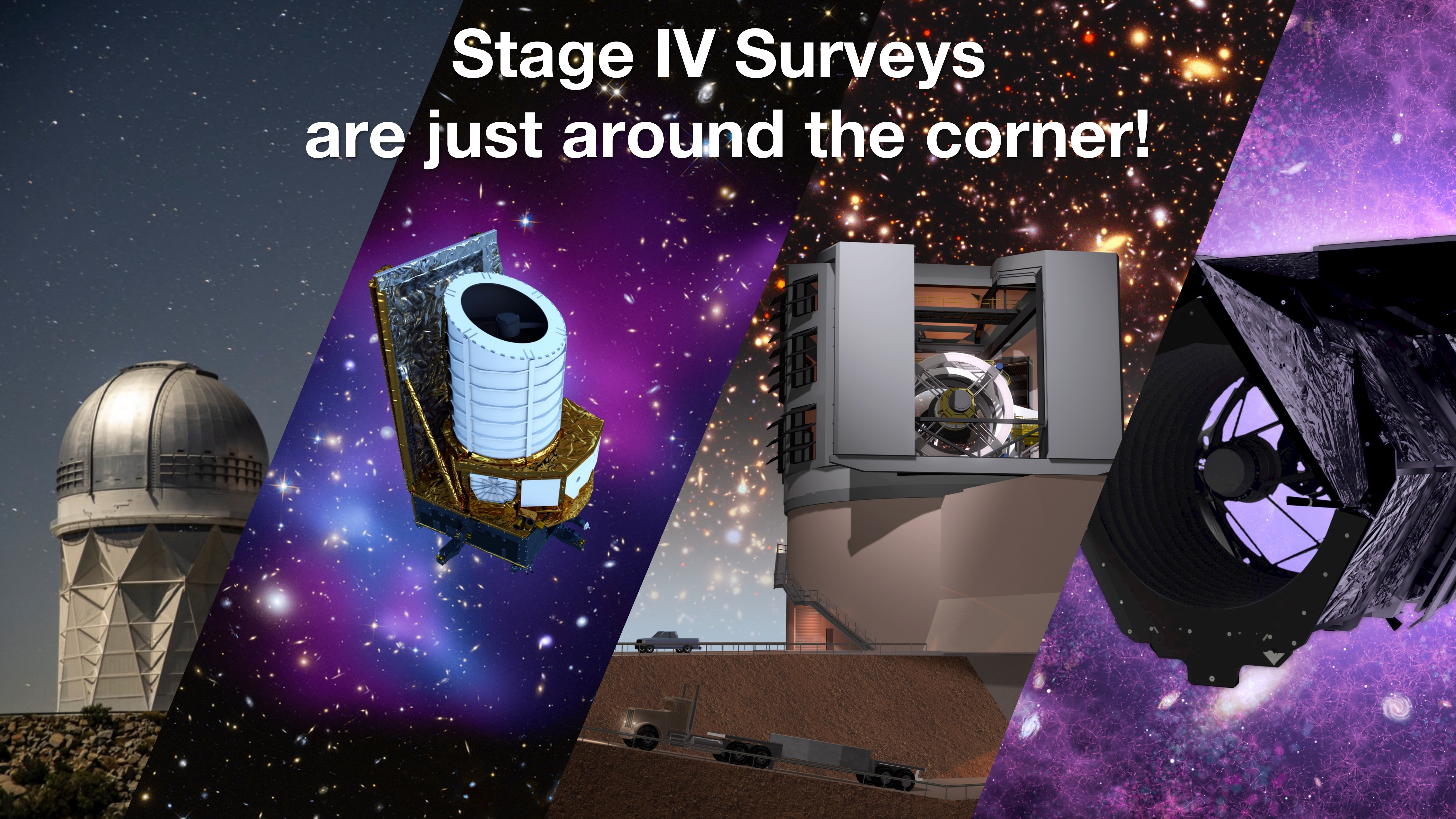
PHYSICAL REVIEW LETTERS 128, 091302 (2022)

Cosmic Birefringence from the Planck Data Release 4

P. Diego-Palazuelos,^{1,2,*} J. R. Eskilt,^{3,†} Y. Minami,⁴ M. Tristram,⁵ R. M. Sullivan,⁶ A. J. Banday,^{7,8} R. B. Barreiro,¹ H. K. Eriksen,³ K. M. Górski,^{9,10} R. Keskitalo,^{11,12} E. Komatsu,^{13,14} F. Martínez-González,¹ D. Scott,⁶ P. Vielva,¹ and I. K. Wehus,³

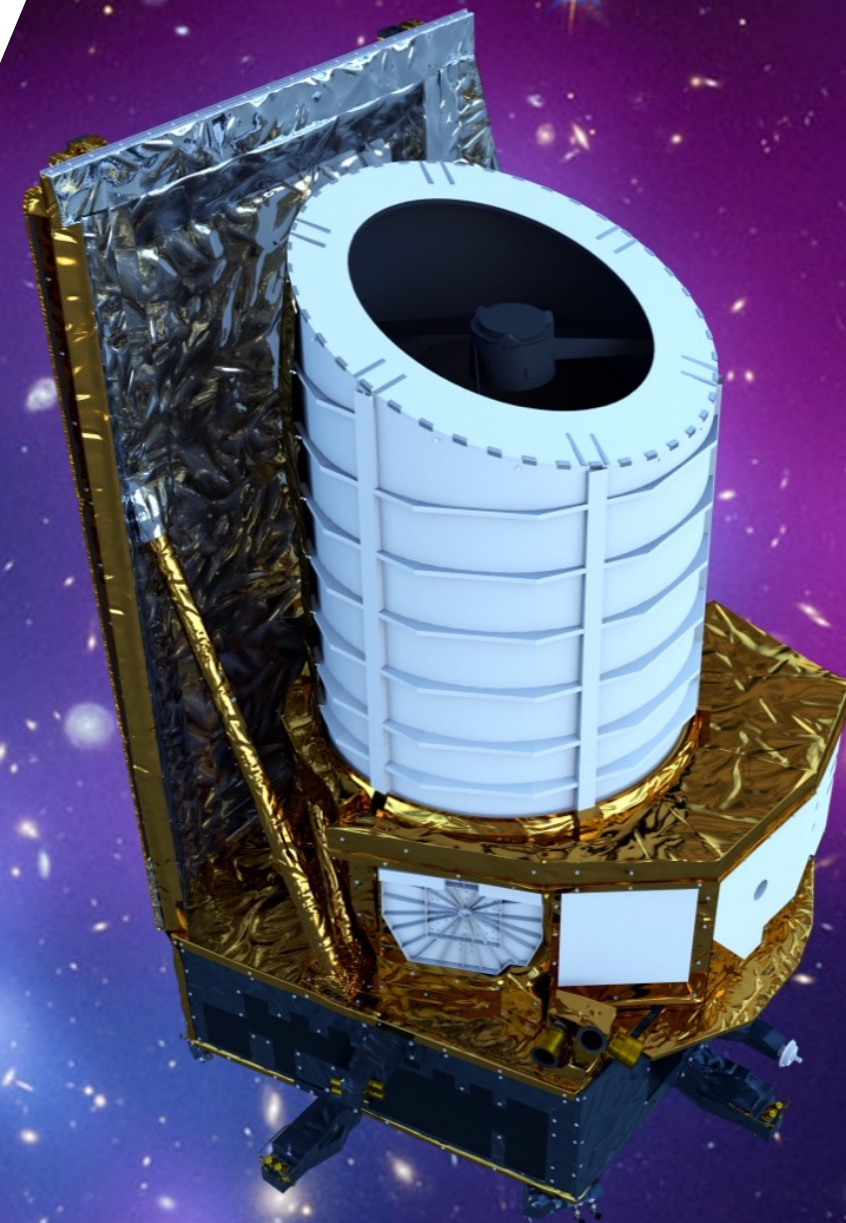
Loureiro et al., A&A (2022)

**Stage IV Surveys
are just around the corner!**



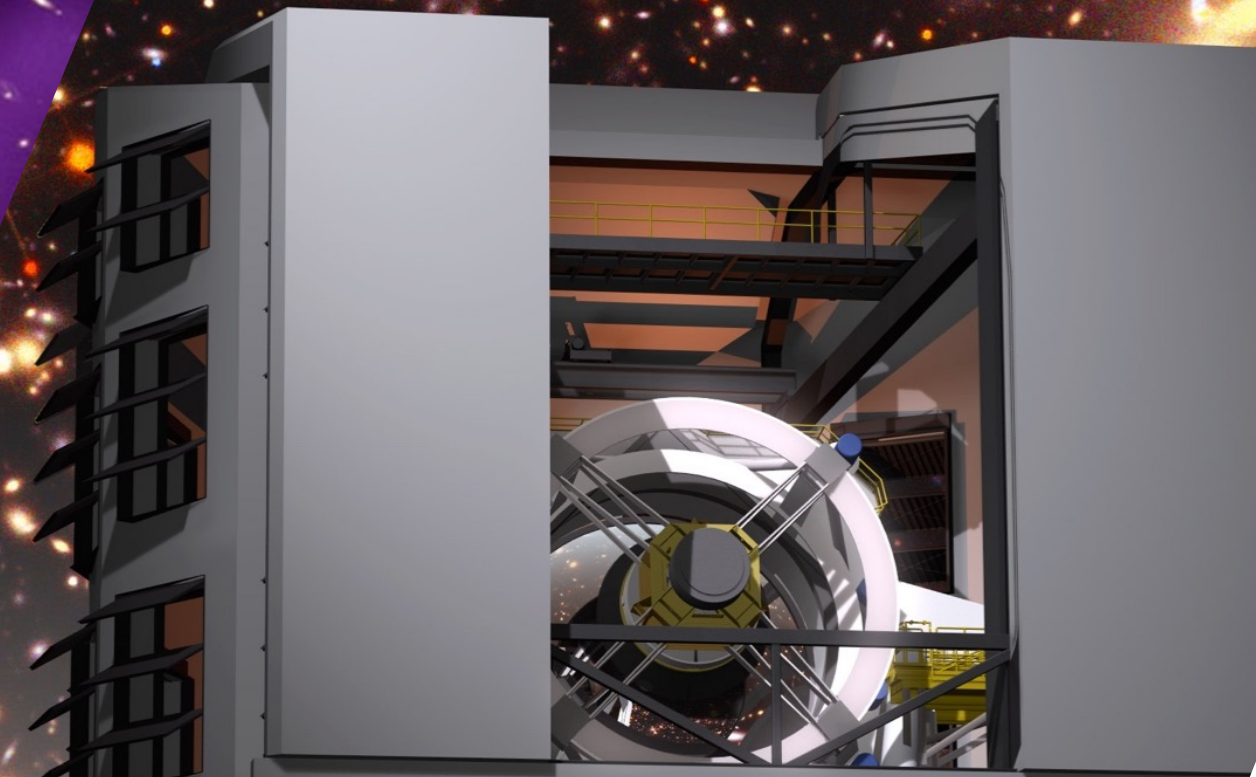
Euclid

- ~ 2 Billion galaxies for Weak Lensing
- ~ 50 Million galaxies for Galaxy Clustering
- Photometric and Spectroscopic
- 15 000 deg²
- Up to redshift of ~ 2
- Launch: 2023



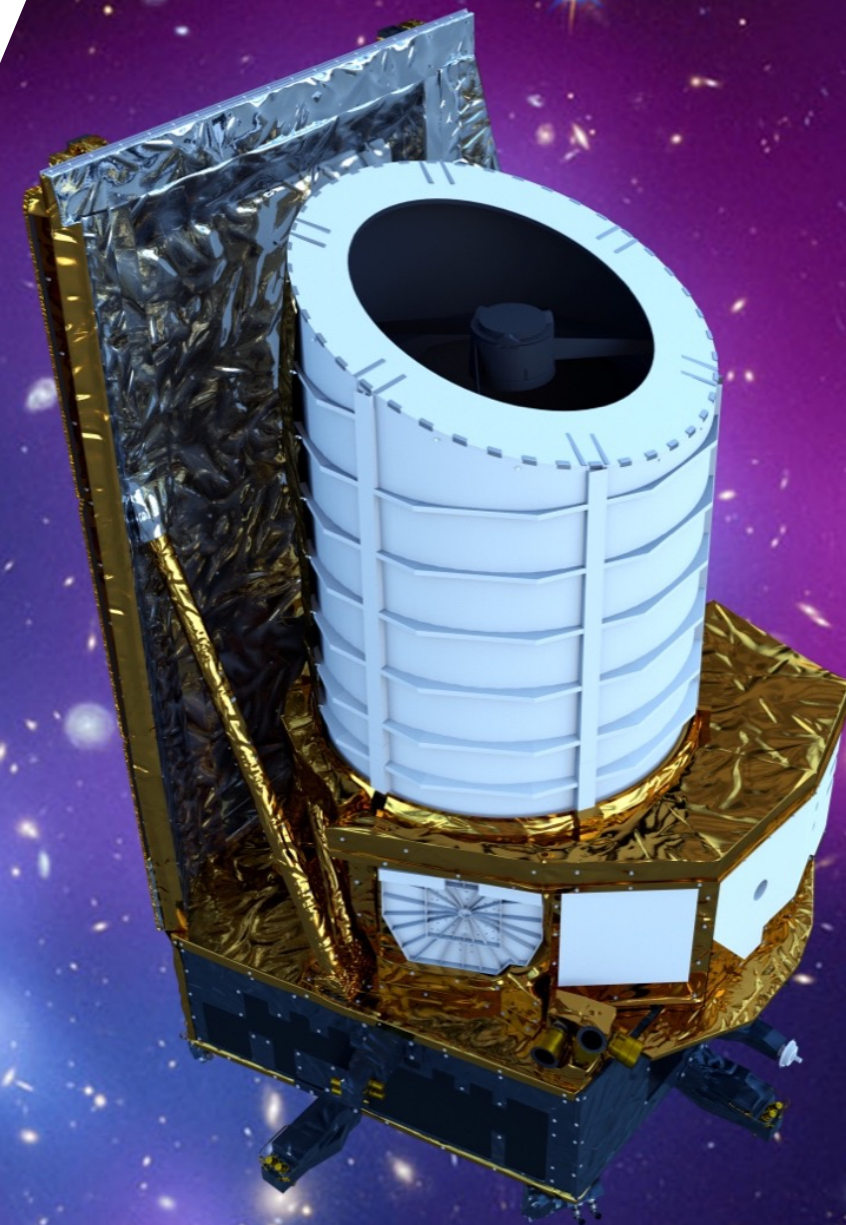
LSST

- ~ 20 Billion photometric galaxies
- ~ 10⁵ Supernovae
- Six bands (ugrizy)
- 18 000 deg²
- Up to redshift of ~ 1.2
- First Light: 2023



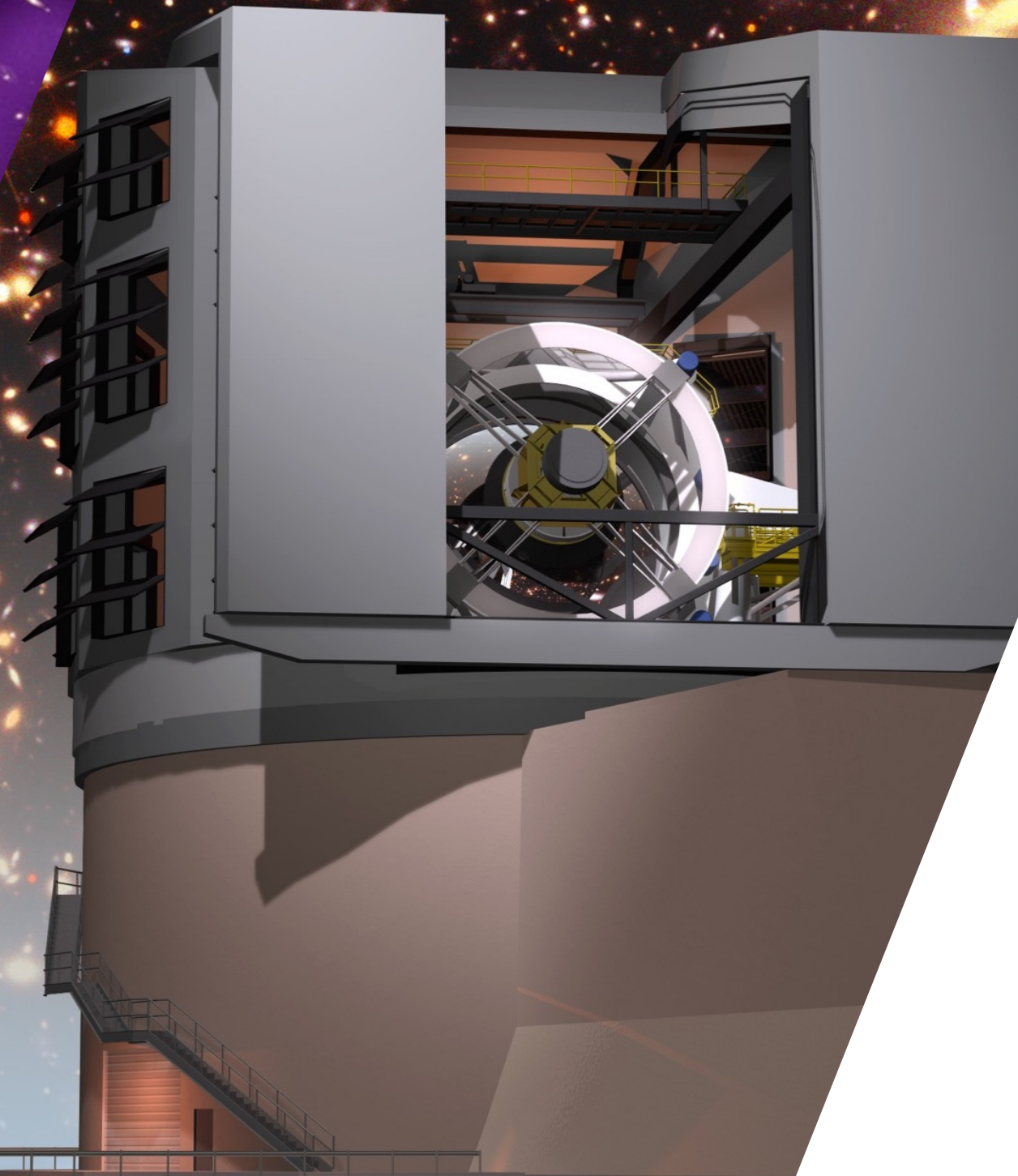
Euclid

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LSST

- ~ 20 Billion photometric galaxies
- ~ 10⁵ Supernovae
- Six bands (ugrizy)
- 18 000 deg²
- Up to redshift of ~ 1.2
- First Light: 2023



Both will be amazing for Weak Lensing



Exploring Stage-IV data will require the next generation of data analysis techniques, breaking away from outdated assumptions such as sky-flatness, gaussianity, etc.

1. Weak Lensing

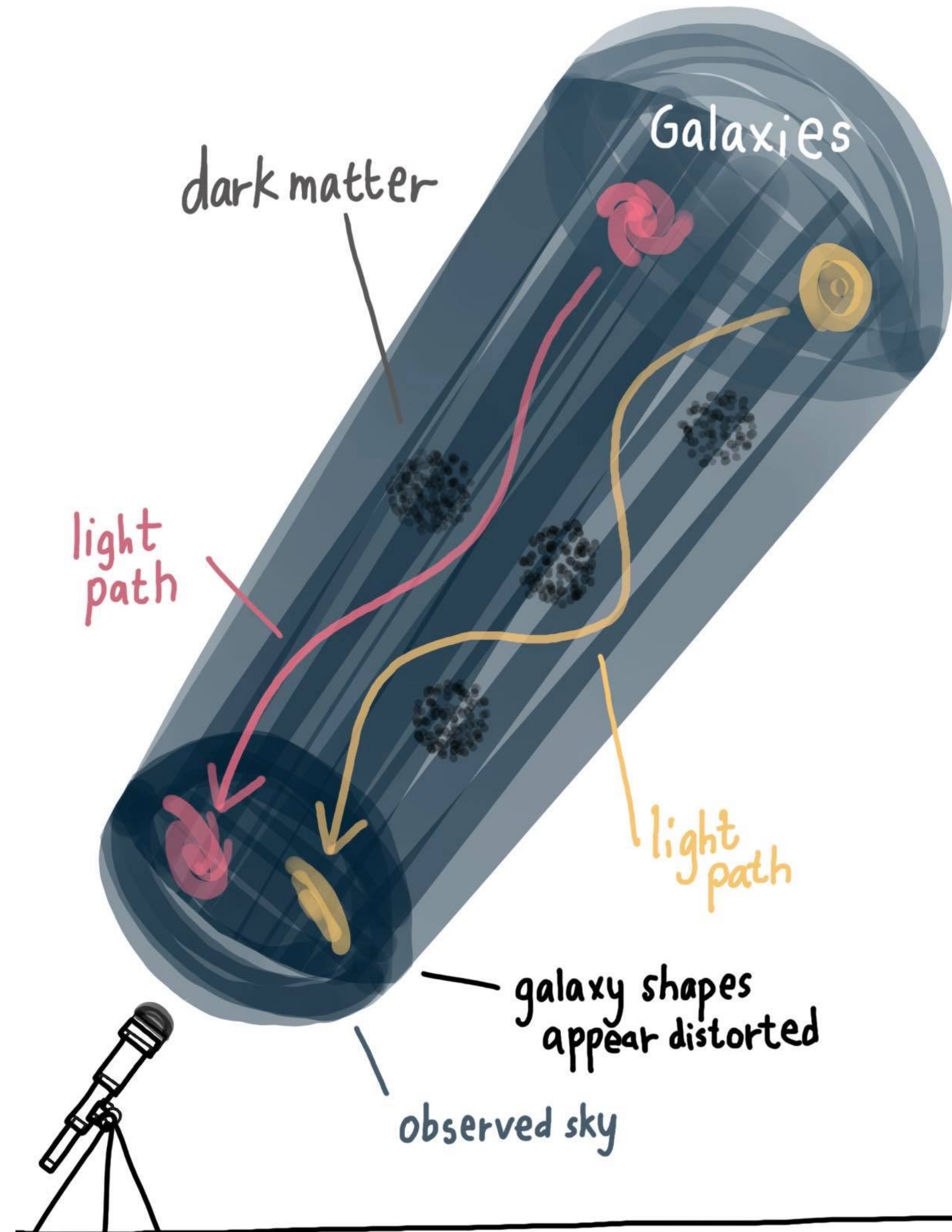
A speed-run

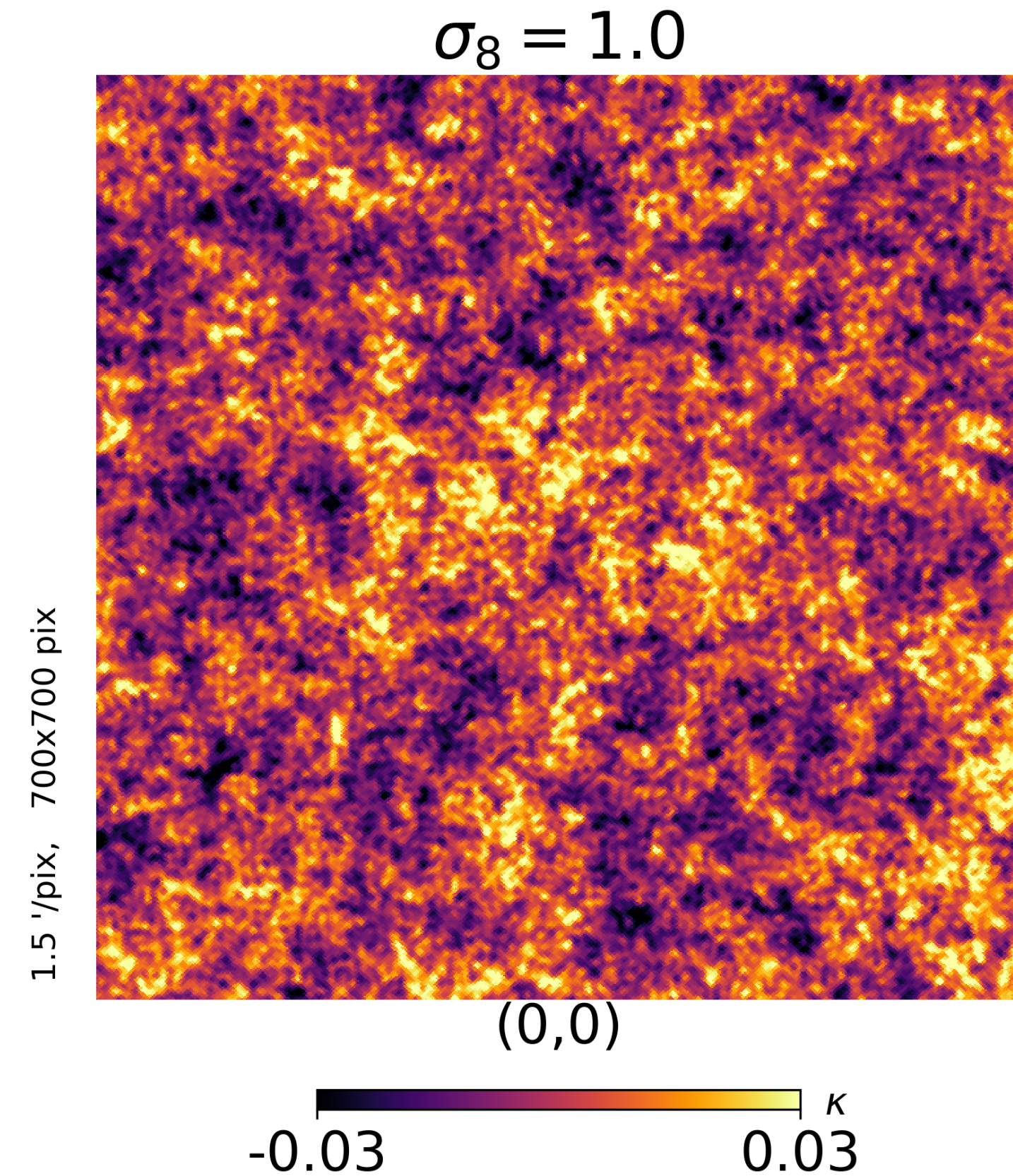
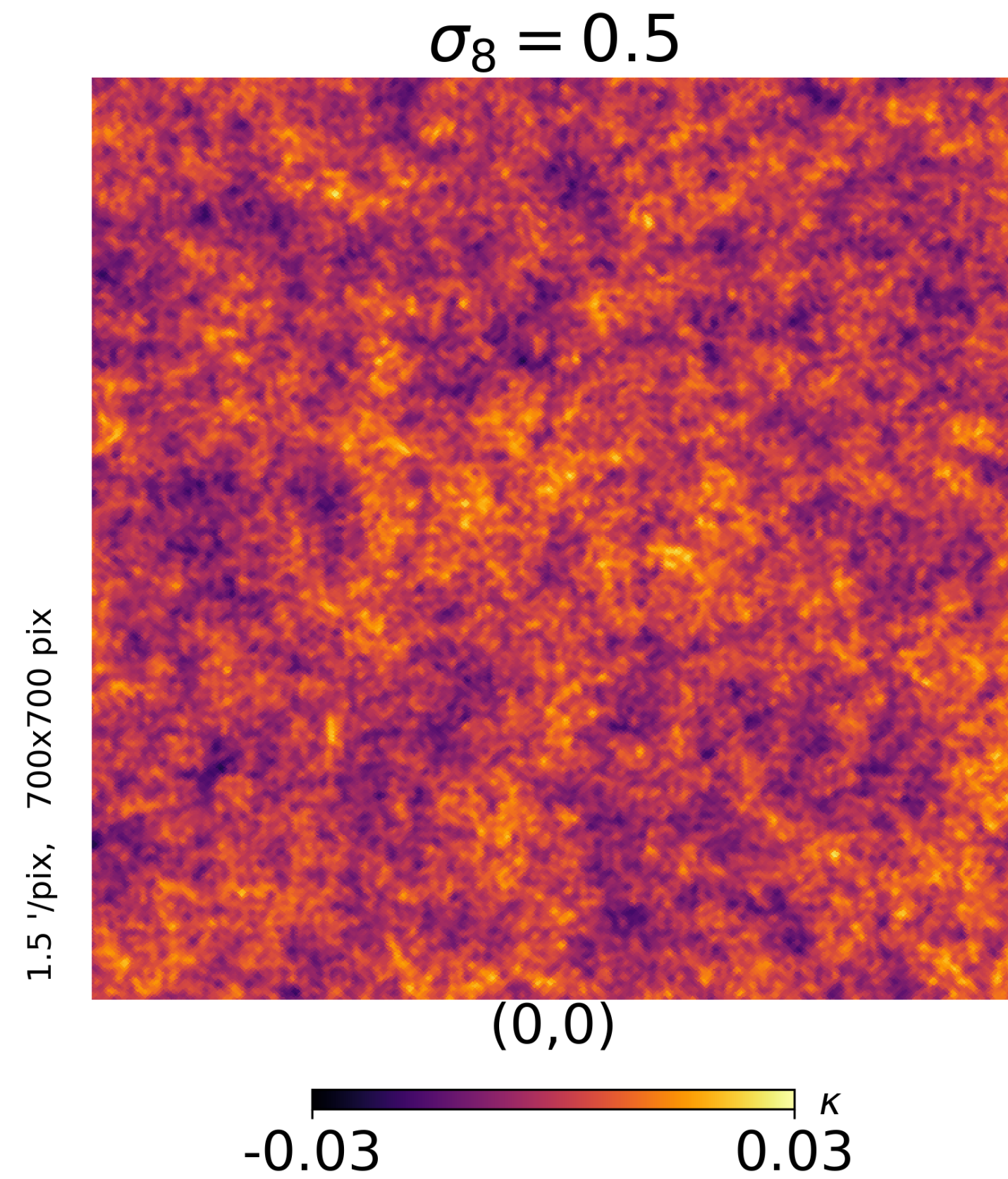
Weak Lensing (mandatory slide!)

We can probe the growth of structures in the universe using weak gravitational lensing

$$S_8 = \sigma_8 \left(\frac{\Omega_m}{0.3} \right)^{1/2}$$

as well as the distribution of matter along the line-of-sight.





The amplitude of matter density fluctuations

Weak Lensing Theory Speed-run



- The mapping between the lensing source's true angular position and the observed angular position is $\theta_{s,i} \approx A_{ij}\theta_{\text{obs},j}$, with

$$A_{ij} = \delta_{ij} - \partial_i \partial_j \tilde{\Psi}$$

where

$$\tilde{\Psi}(\chi_s, \hat{n}) = 2 \int_0^{\chi_s} d\chi \frac{f_K(\chi_s - \chi)}{f_K(\chi)f_K(\chi_s)} \Psi(\chi, \hat{n})$$

↓
Newtonian
Grav. Potential

- From these, we can define the Weak Lensing observables (in harmonic space):

- Convergence:

$$\kappa_{\ell m} = -\frac{1}{2} \ell(\ell + 1) \tilde{\Psi}_{\ell m}$$

- Shear:

$$\gamma_{\ell m} = \frac{1}{2} \sqrt{(\ell - 1)\ell(\ell + 1)(\ell + 2)} \tilde{\Psi}_{\ell m}$$

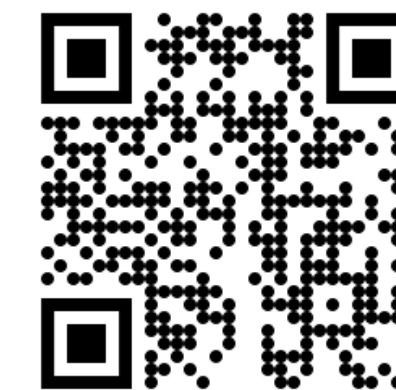
- Since shear is a spin-2 field it can be decomposed into E - and B -modes

$$E_{\ell m} = -\frac{1}{2} \int d\Omega [\gamma(\hat{n})_{+2} Y_{\ell m}^*(\hat{n}) + \gamma^*(\hat{n})_{-2} Y_{\ell m}^*(\hat{n})]$$

and

$$B_{\ell m} = \frac{i}{2} \int d\Omega [\gamma(\hat{n})_{+2} Y_{\ell m}^*(\hat{n}) - \gamma^*(\hat{n})_{-2} Y_{\ell m}^*(\hat{n})]$$

Weak Lensing Theory Speed-run



- The mapping between the lensing source's true angular position and the observed angular position is $\theta_{s,i} \approx A_{ij}\theta_{\text{obs},j}$, with
- From these, we can define the Weak Lensing observables (in harmonic space):
 - Convergence:

where

A_{ij}

$\tilde{\Psi}(\chi_s, \hat{n}) = 2$

WELL, YOU KNOW IT...

↓

Newtonian Grav. Potential

1) $\tilde{\Psi}_{\ell m}$

$\frac{1}{\ell(\ell+1)(\ell+2)} \tilde{\Psi}_{\ell m}$

it can be

modes

$$E_{\ell m} = -\frac{1}{2} \int d\Omega [\gamma(\hat{n}) {}_{+2}Y_{\ell m}^*(\hat{n}) + \gamma^*(\hat{n}) {}_{-2}Y_{\ell m}^*(\hat{n})]$$

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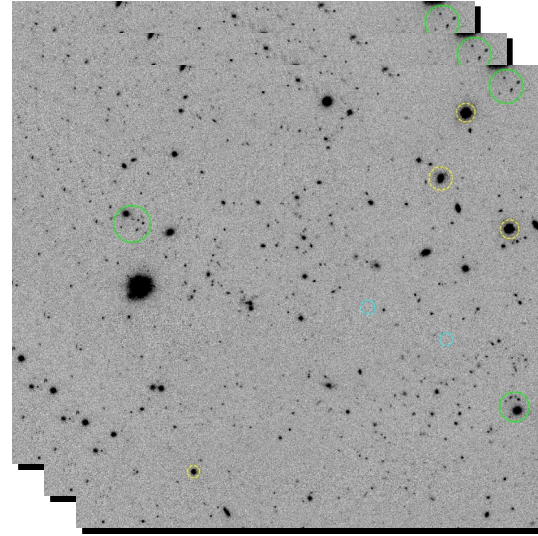
2. Field Level Inference

What is it, and Why do we care?

“Vintage” Cosmology

Ex: Weak Lensing Surveys

Galaxy Shapes

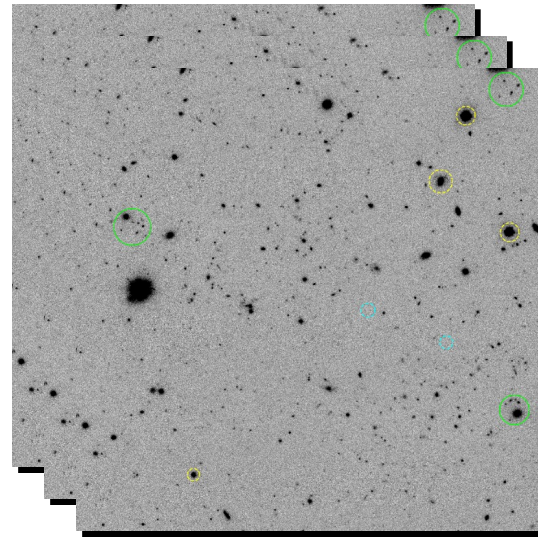


Kannawadi et al. 2018

“Vintage” Cosmology

Ex: Weak Lensing Surveys

Galaxy Shapes

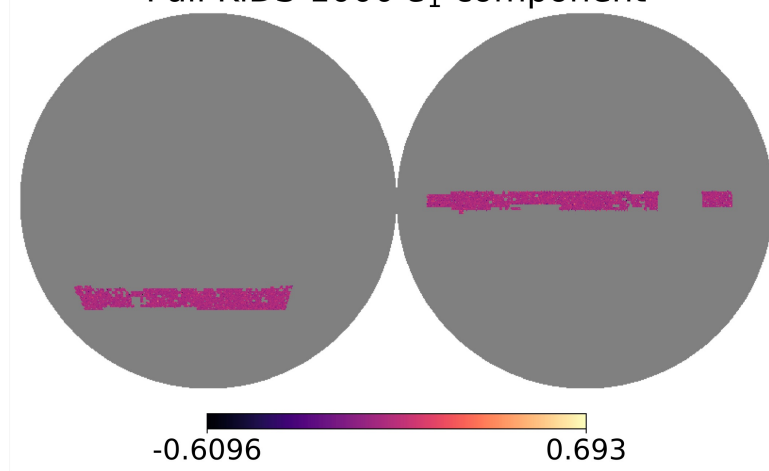


Kannawadi et al. 2018

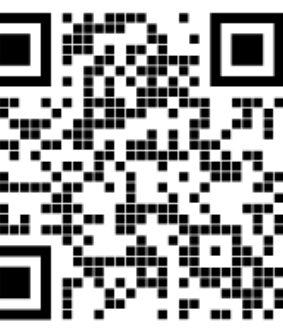


“Estimator”

Full KiDS-1000 e_1 component



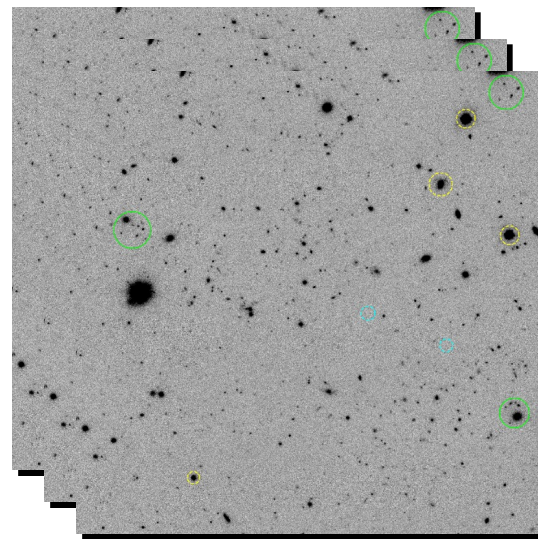
Galaxy shear maps



“Vintage” Cosmology

Ex: Weak Lensing Surveys

Galaxy Shapes

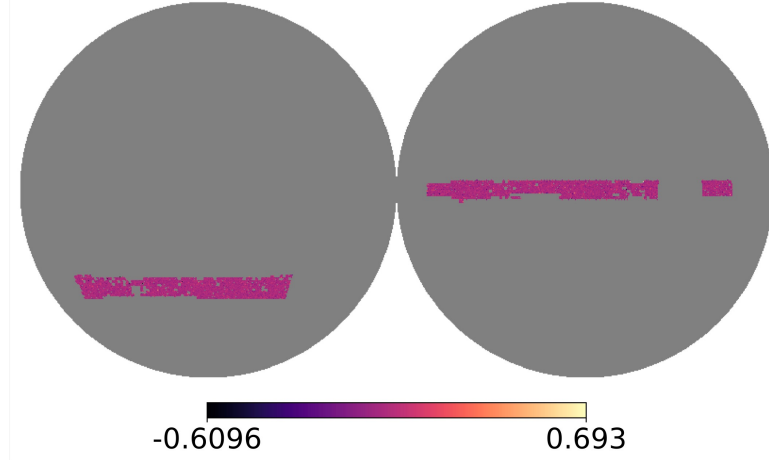


Kannawadi et al. 2018



“Estimator”

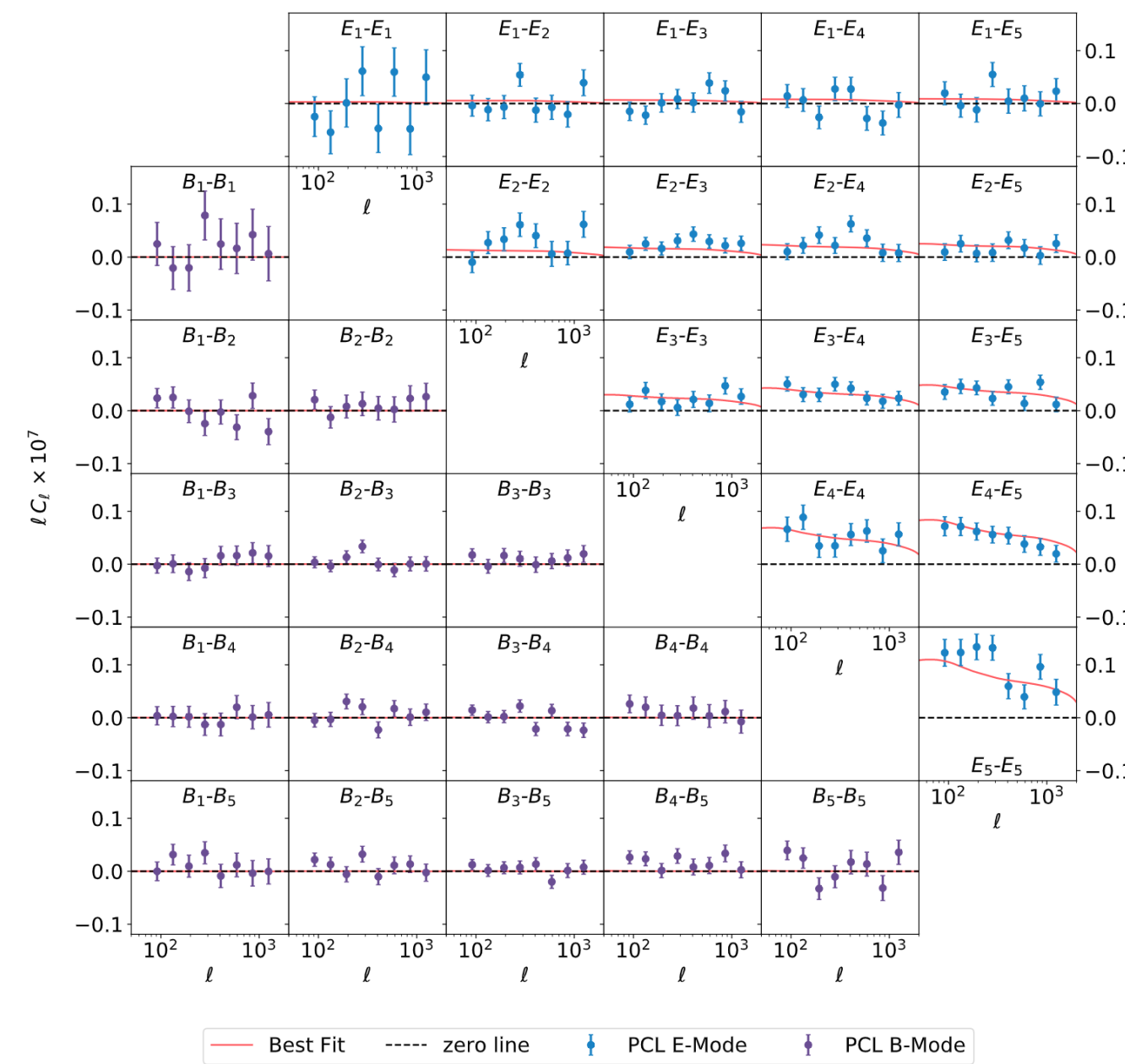
Full KiDS-1000 e_1 component

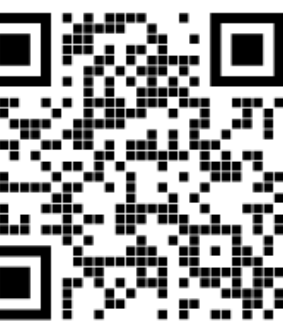


Galaxy shear maps



Estimator

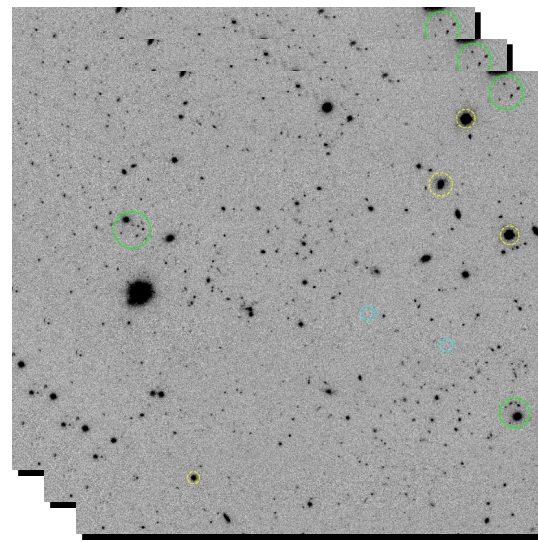




“Vintage” Cosmology

Ex: Weak Lensing Surveys

Galaxy Shapes

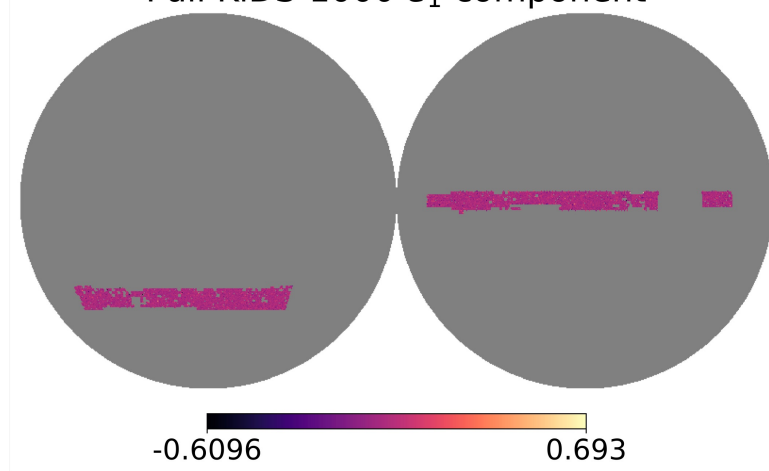


Kannawadi et al. 2018

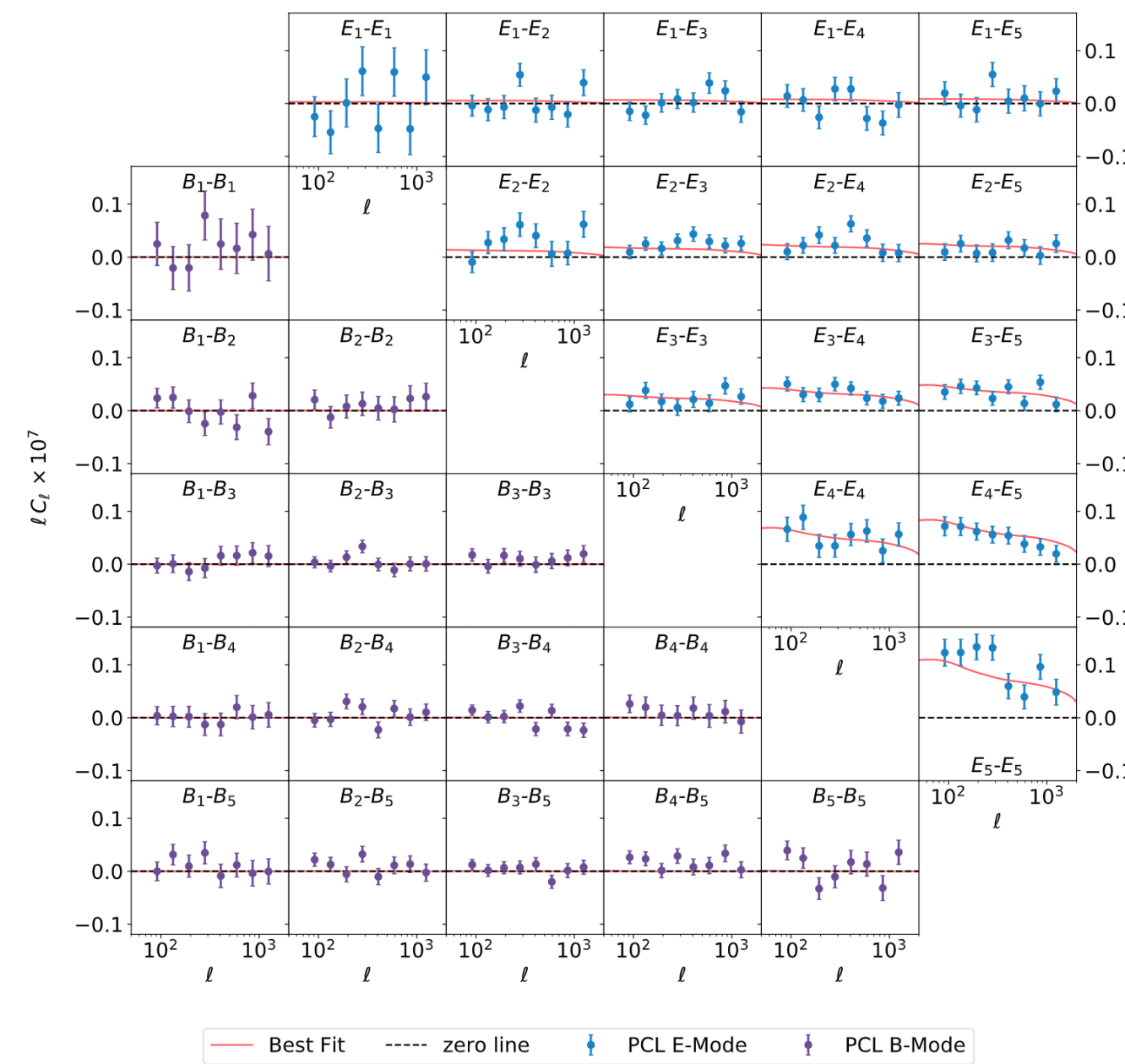
“Estimator”



Full KiDS-1000 e_1 component



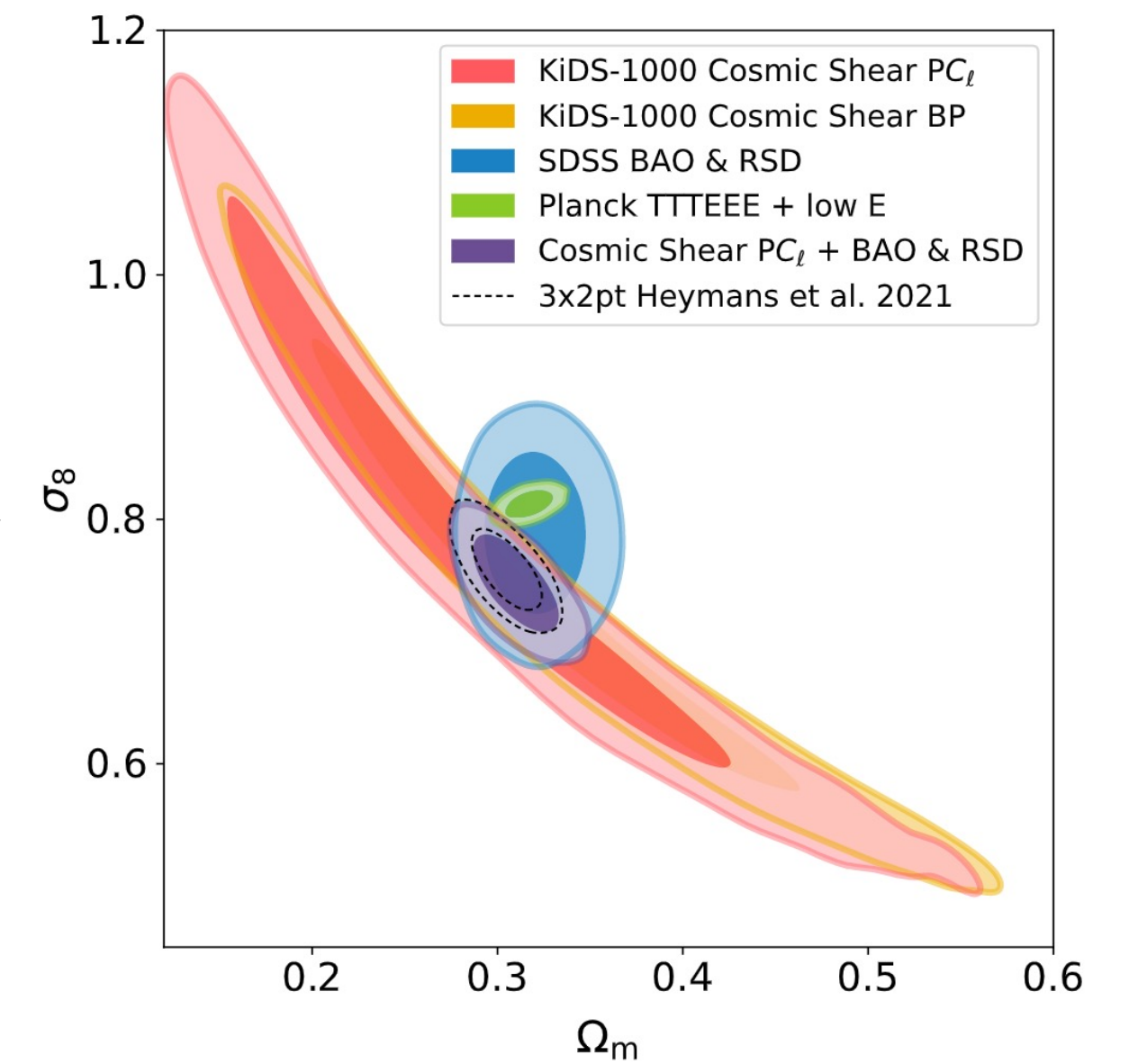
Galaxy shear maps



Bayesian Inference



Loureiro et al. 2021 (2110.06947)



Cosmological Parameters

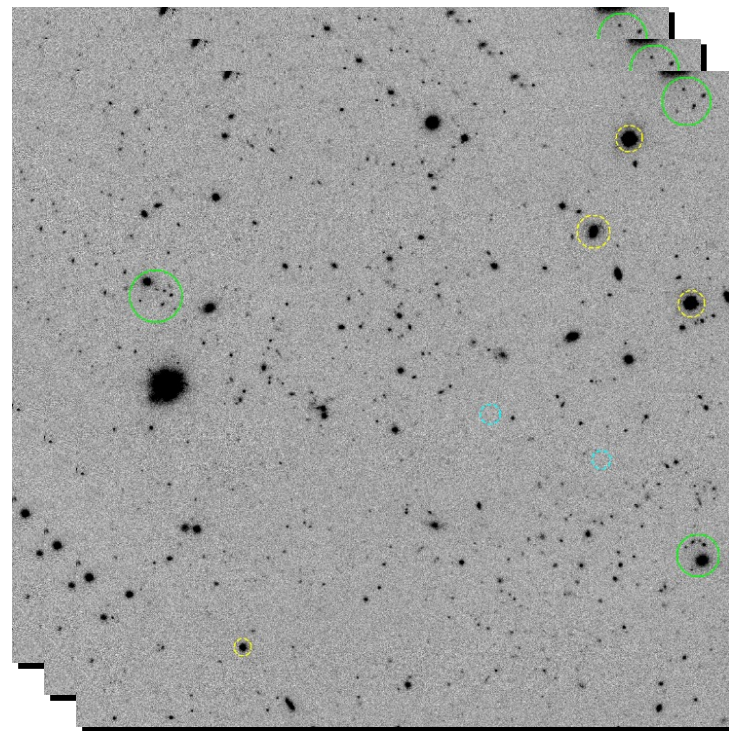
Estimator



Bayesian Hierarchical Cosmology

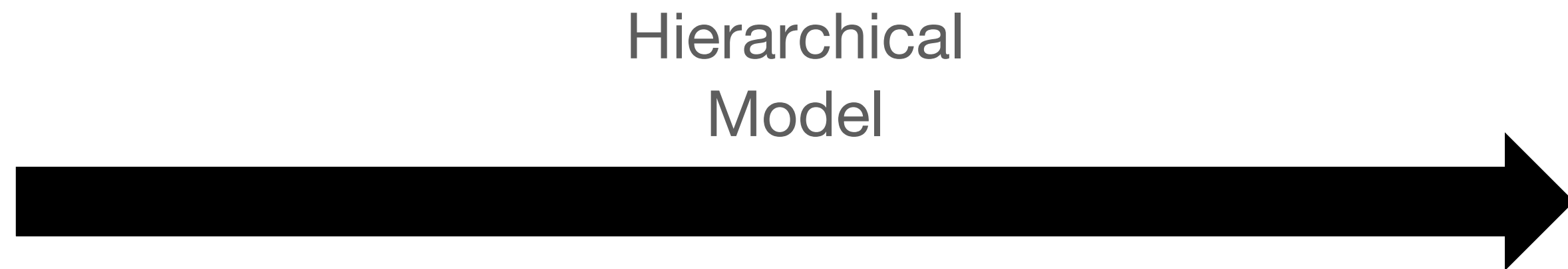
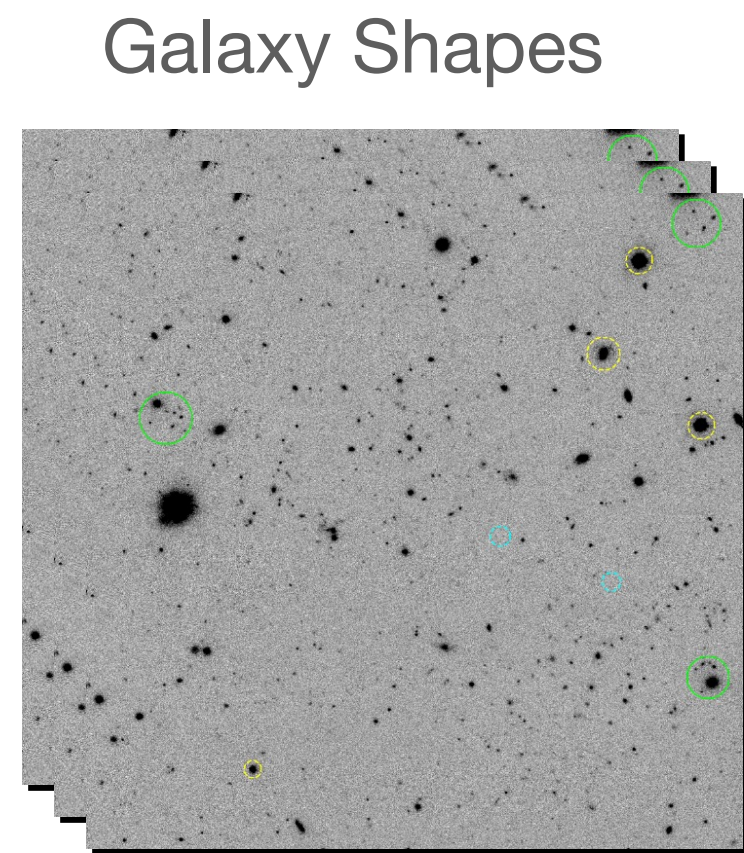
Ex: Weak Lensing

Galaxy Shapes

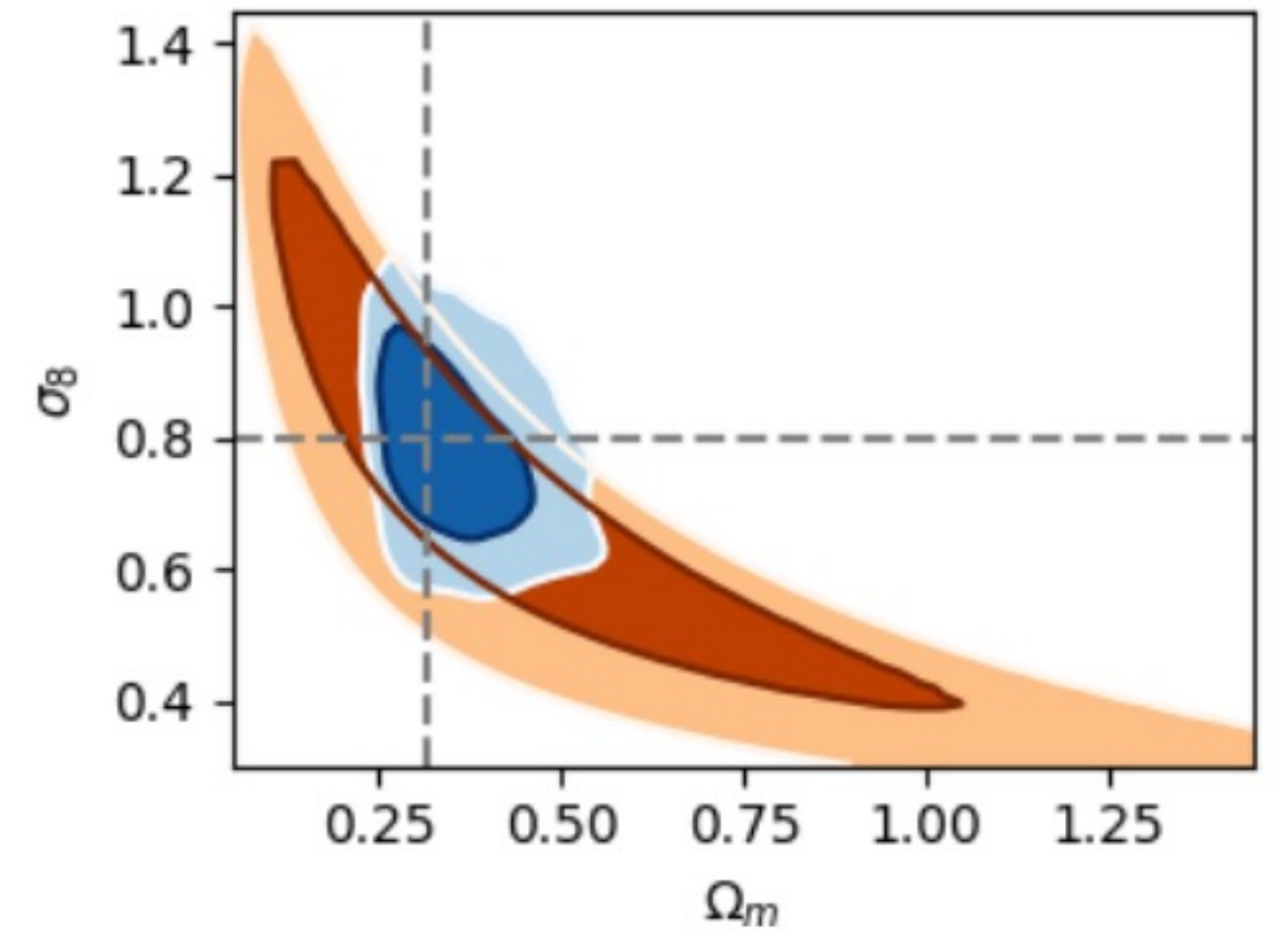


Bayesian Hierarchical Cosmology

Ex: Weak Lensing



Porqueres et al. 2021(2108.04825)

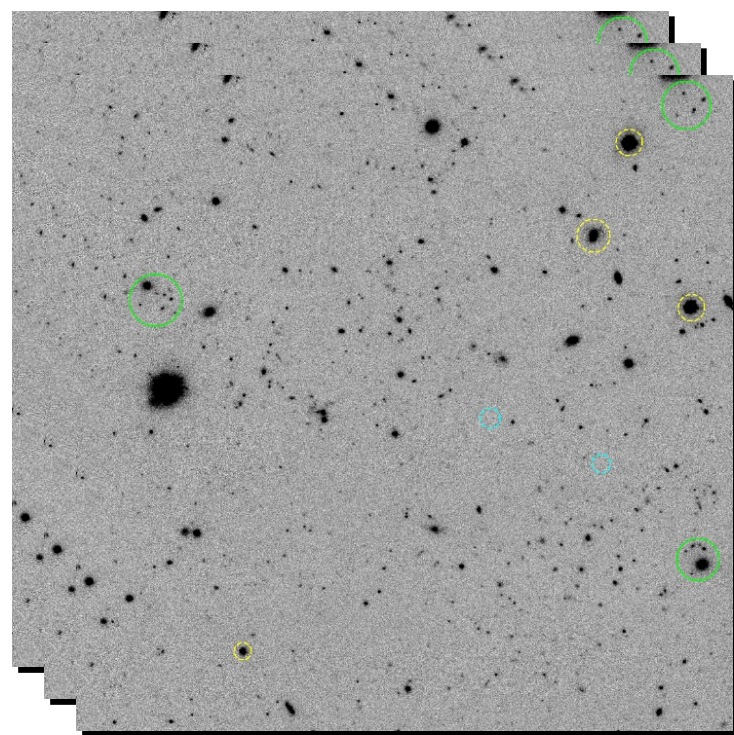


Cosmological Parameters

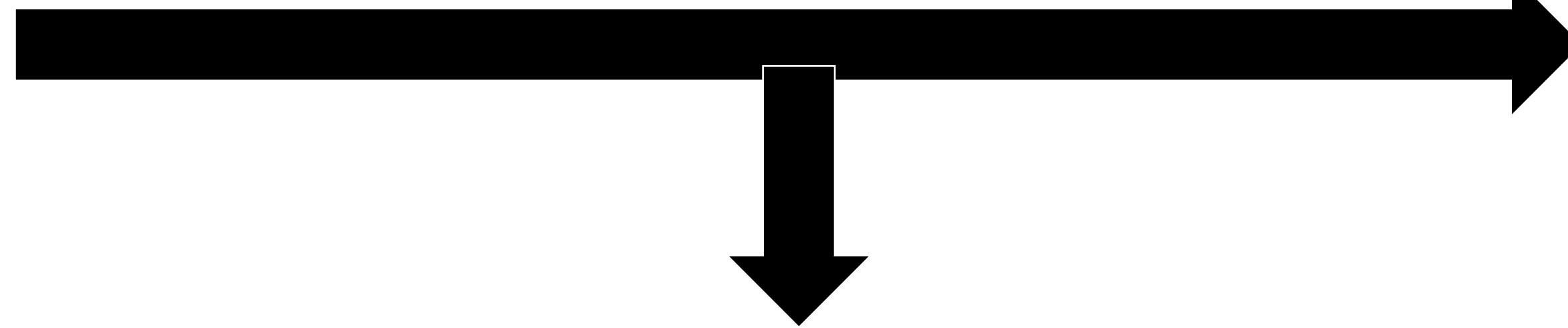
Bayesian Hierarchical Cosmology

Ex: Weak Lensing

Galaxy Shapes

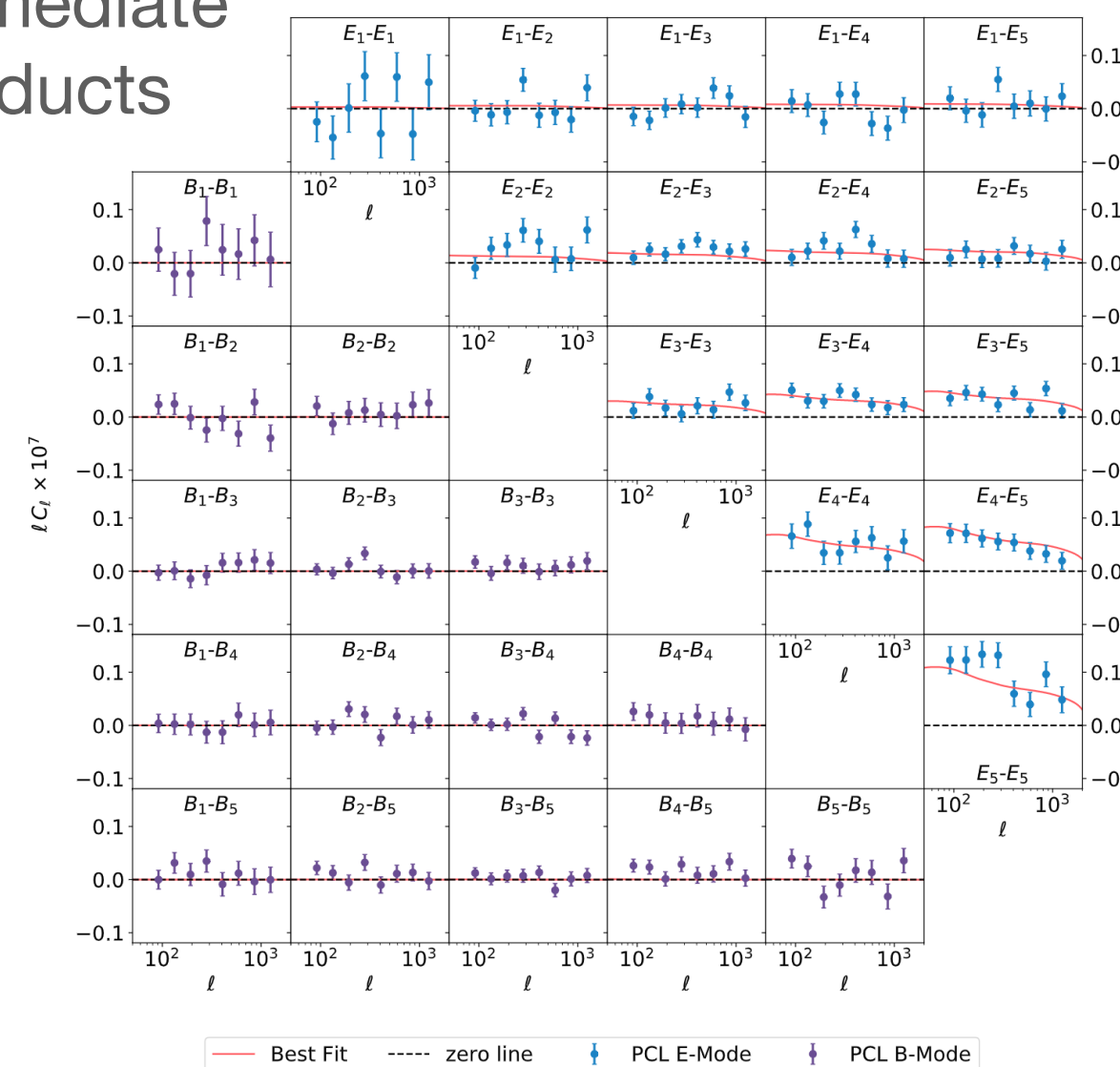
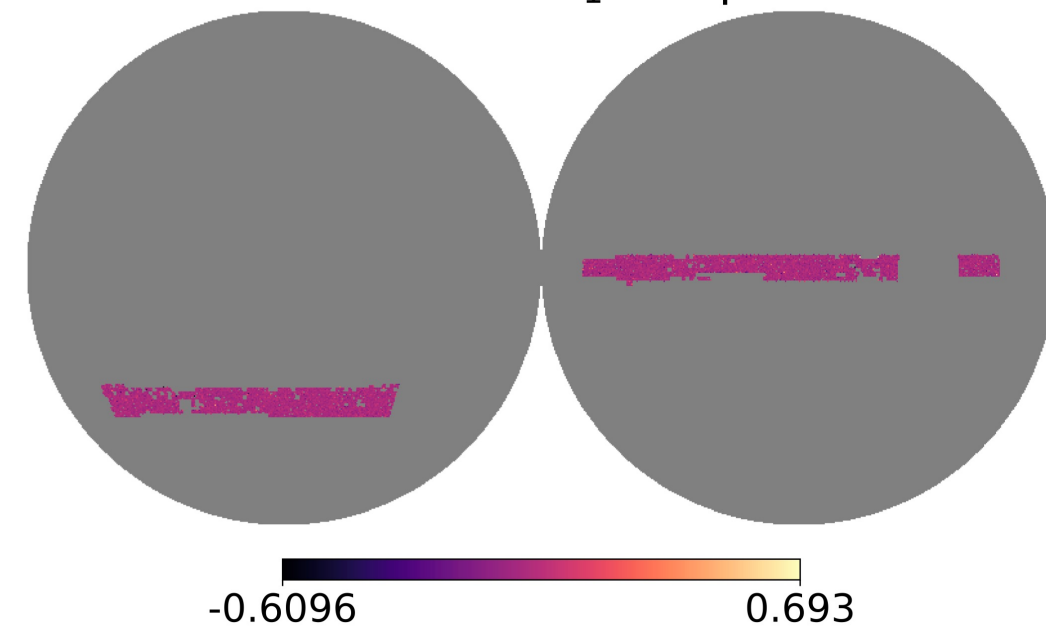


Hierarchical Model

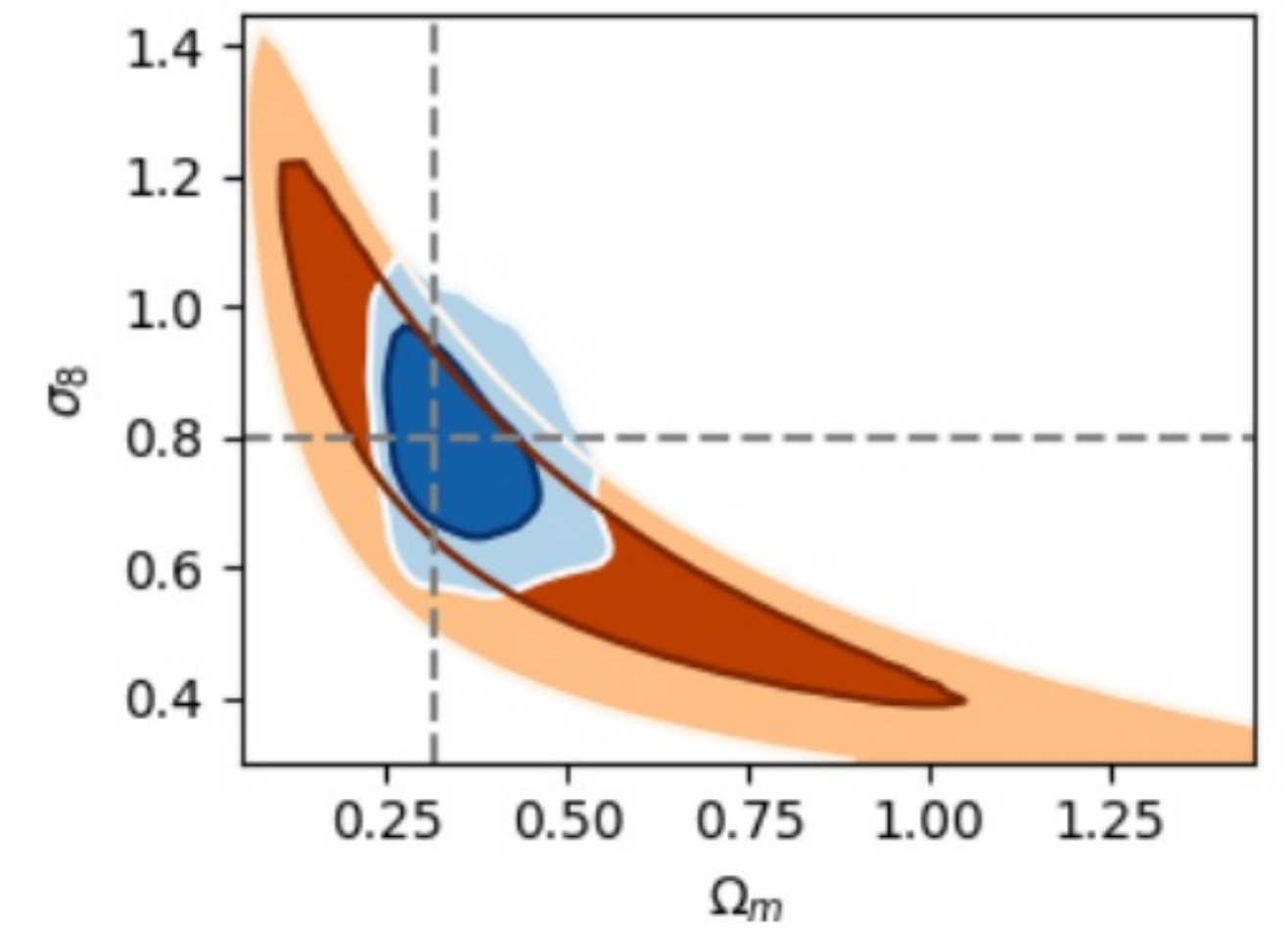


Intermediate products

Full KiDS-1000 e_1 component



Porqueres et al. 2021(2108.04825)

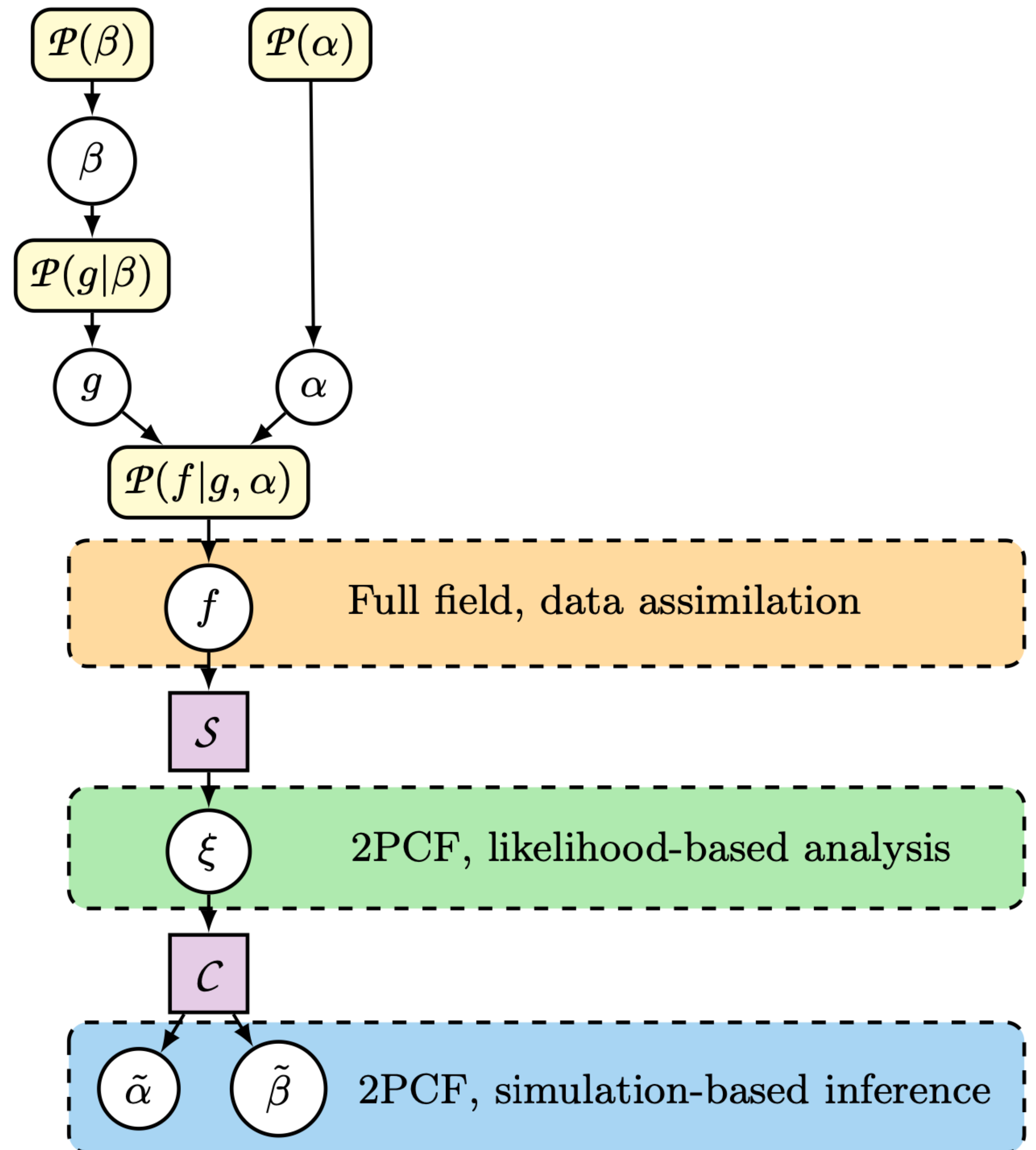


Cosmological Parameters

Field Level Inference

Compared to other methods

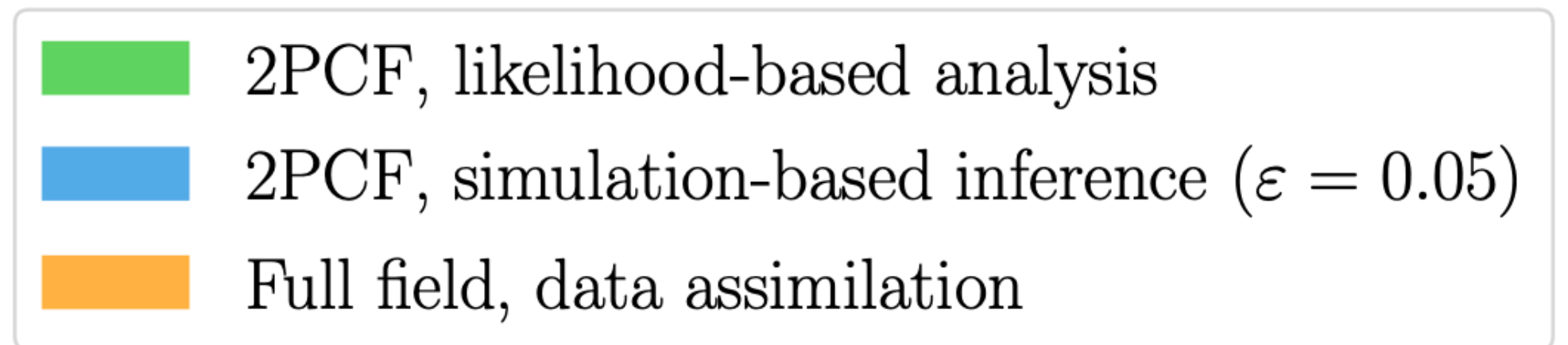
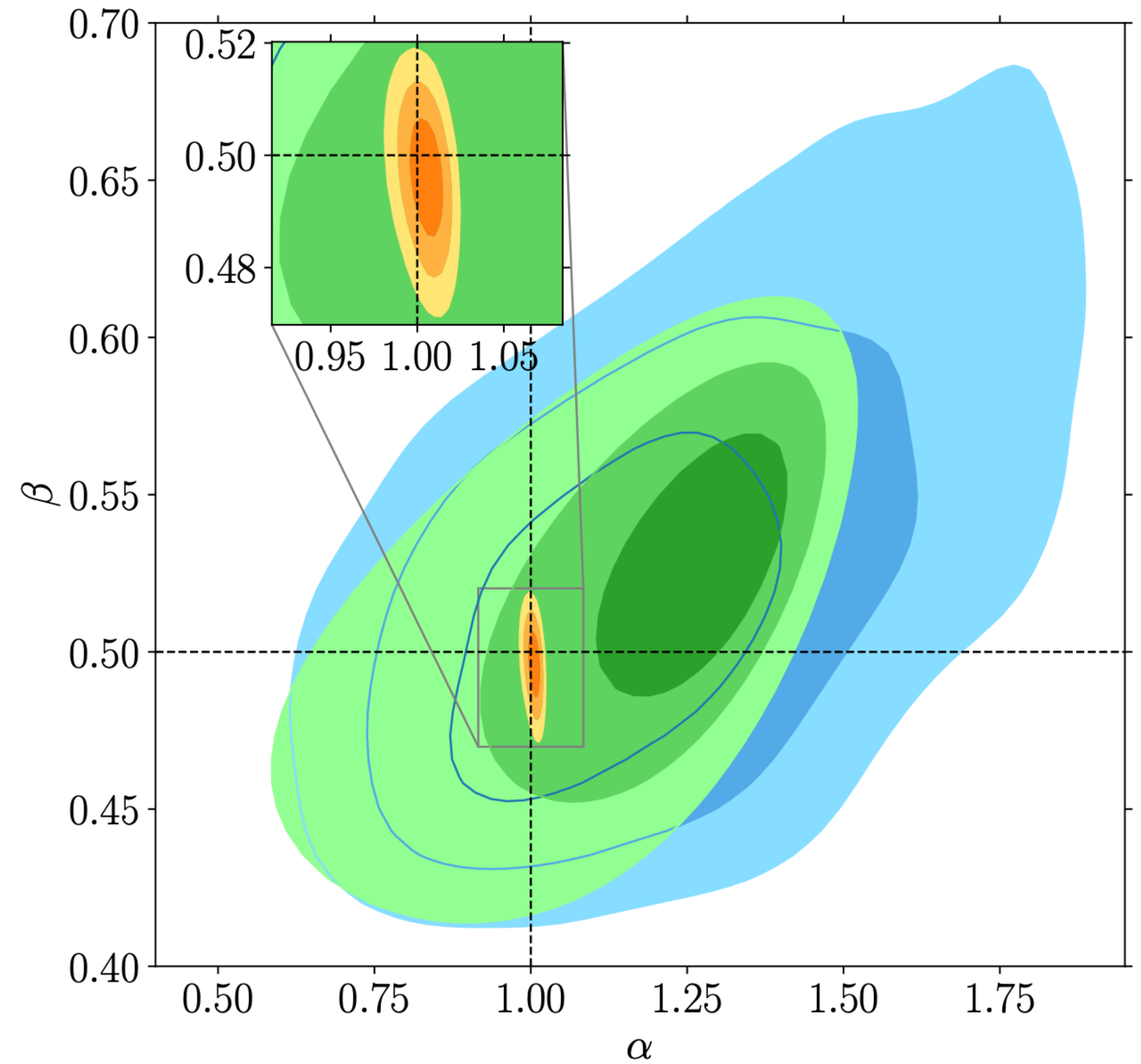
Leclercq & Heavens 2021 (2103.04158)



Field Level Inference

Compared to other methods

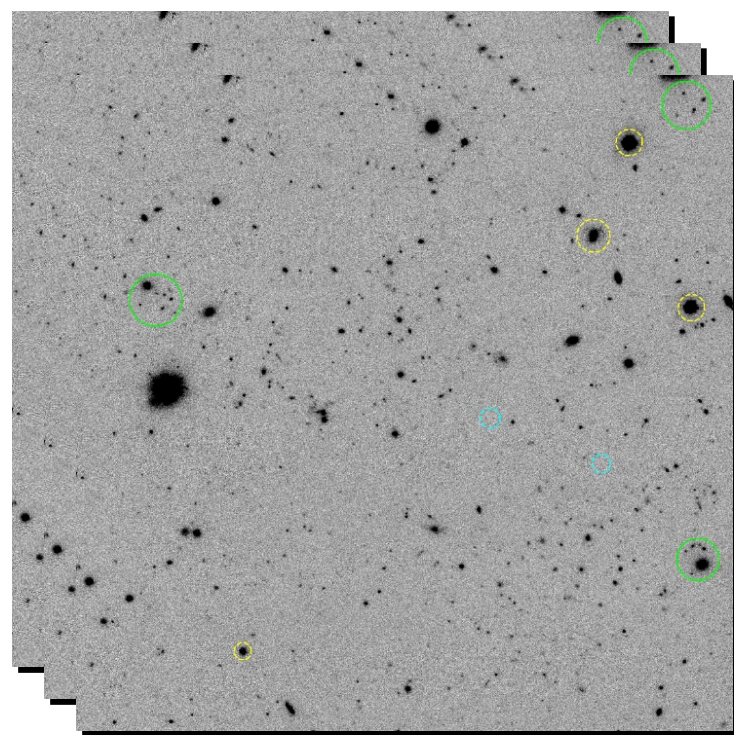
Leclercq & Heavens 2021 (2103.04158)



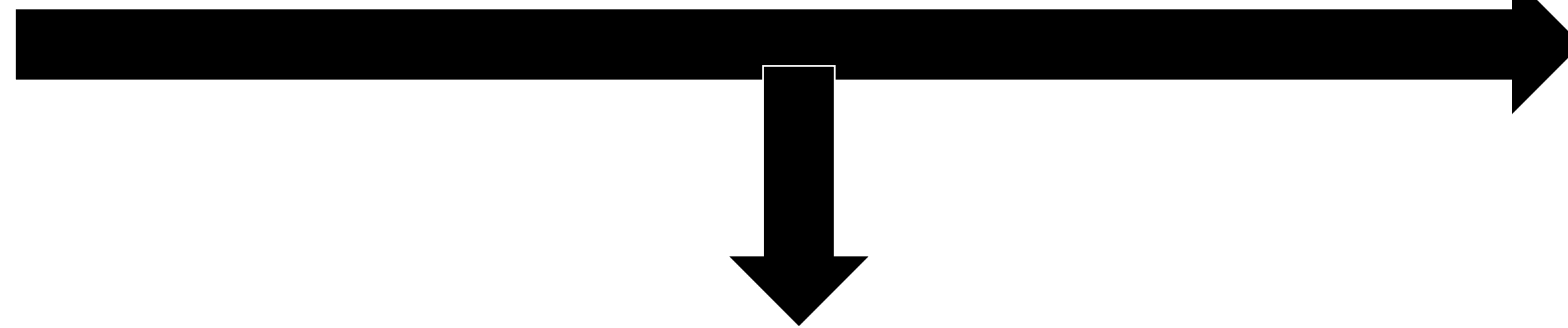
Bayesian Hierarchical Cosmology

Ex: Weak Lensing

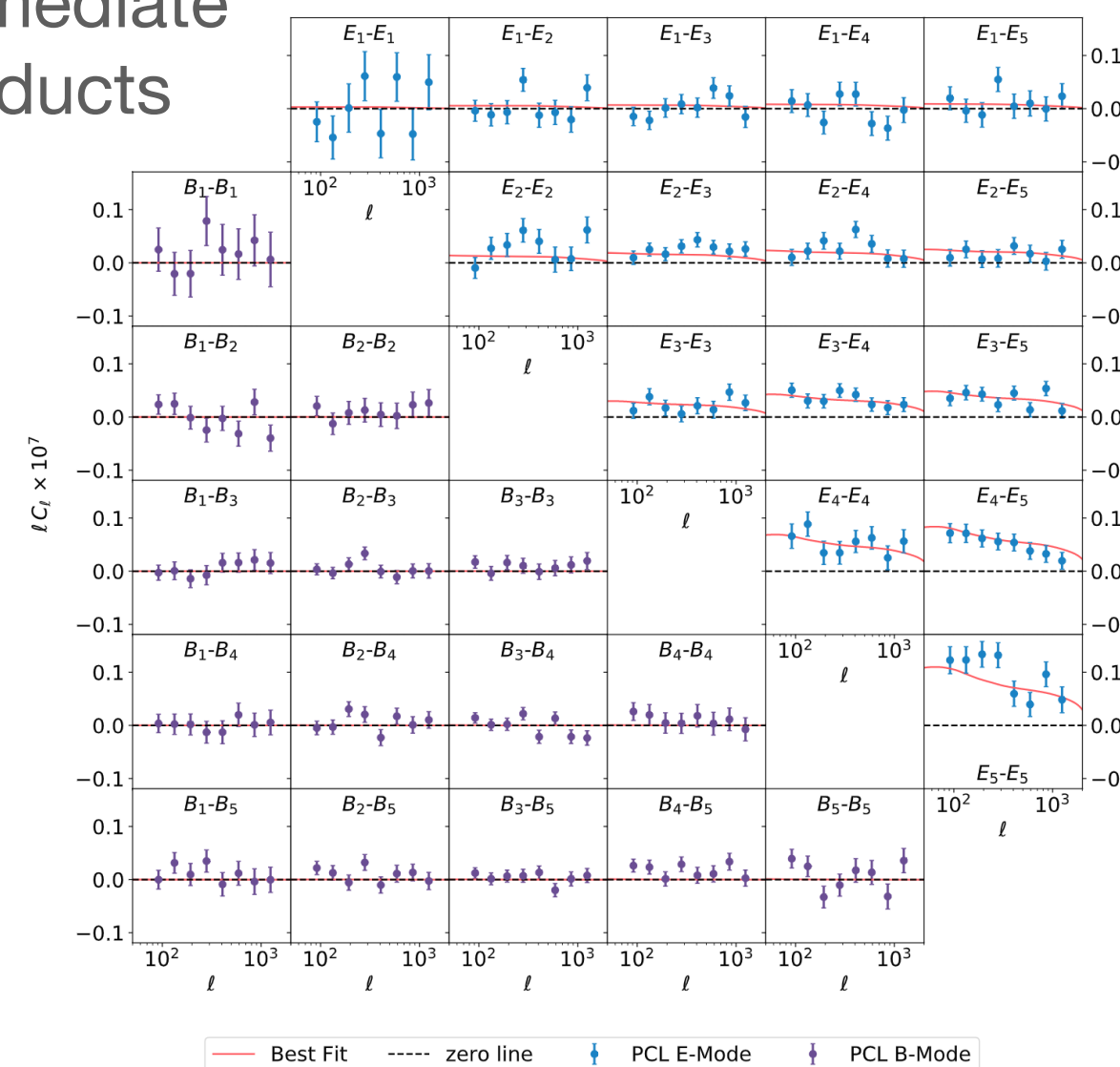
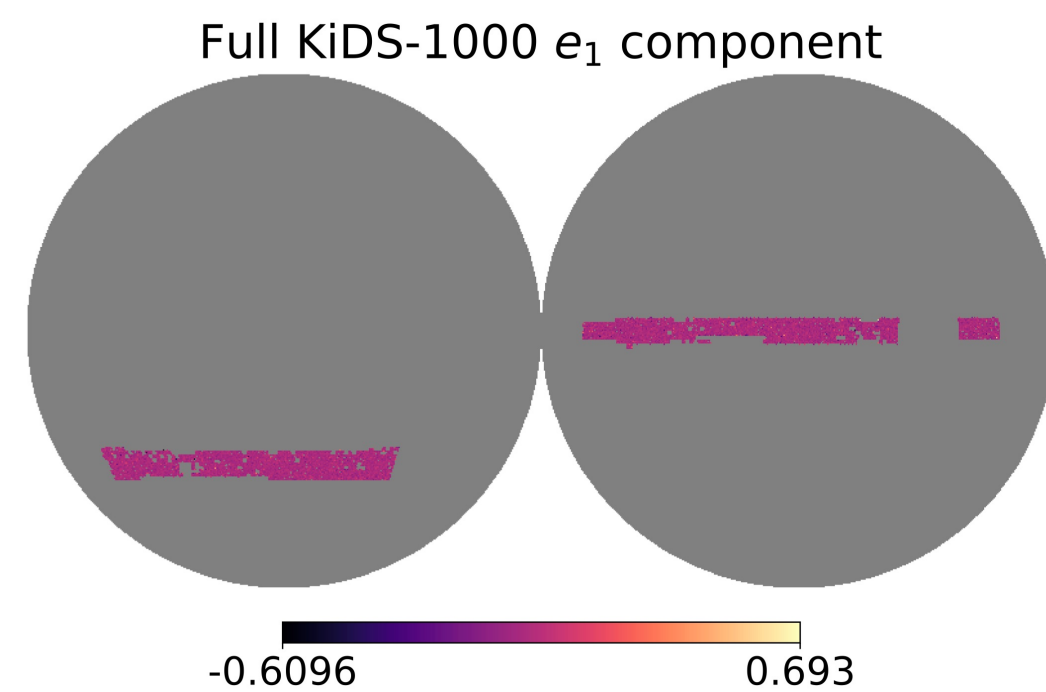
Galaxy Shapes



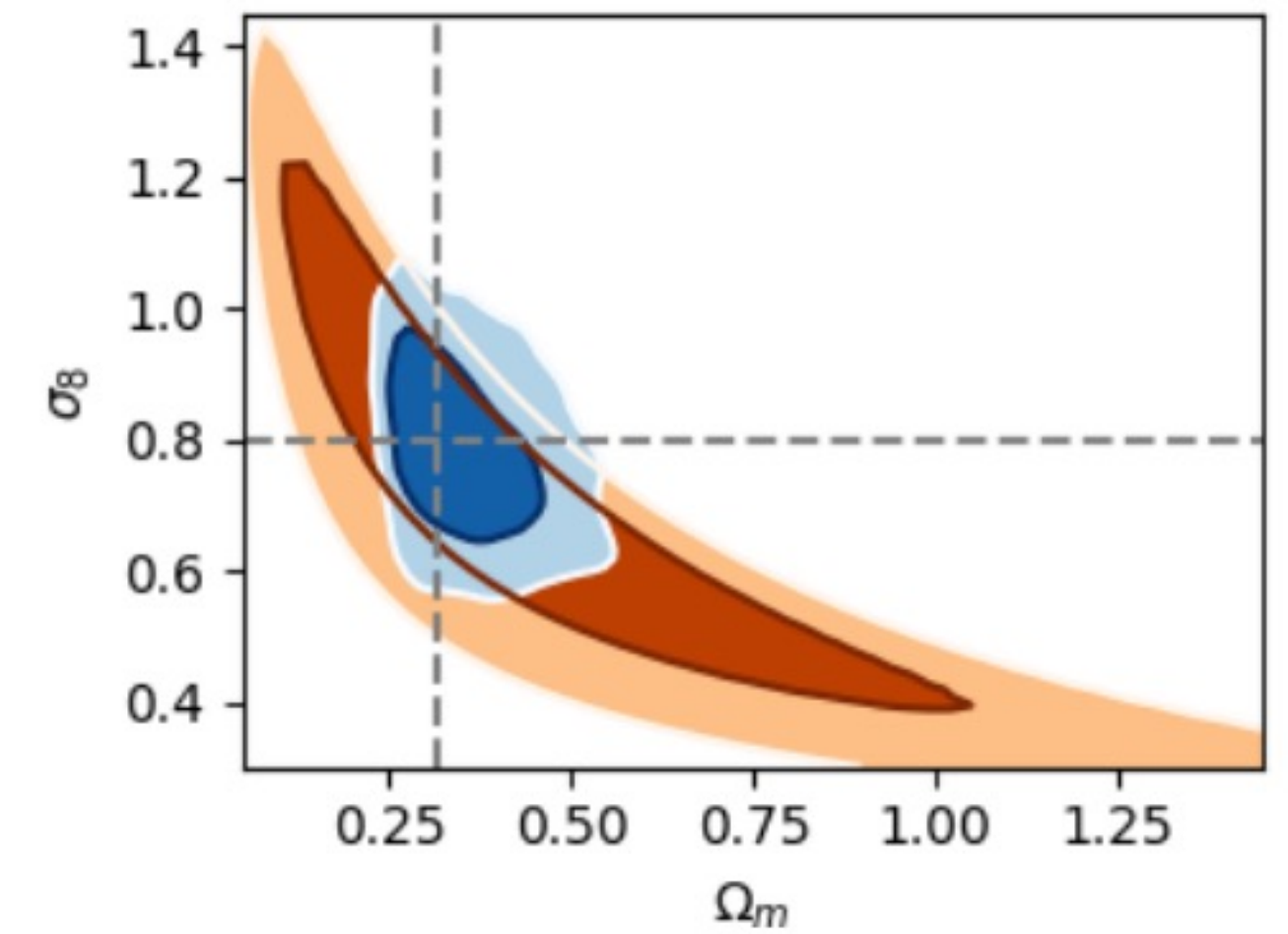
Hierarchical Model



Intermediate products



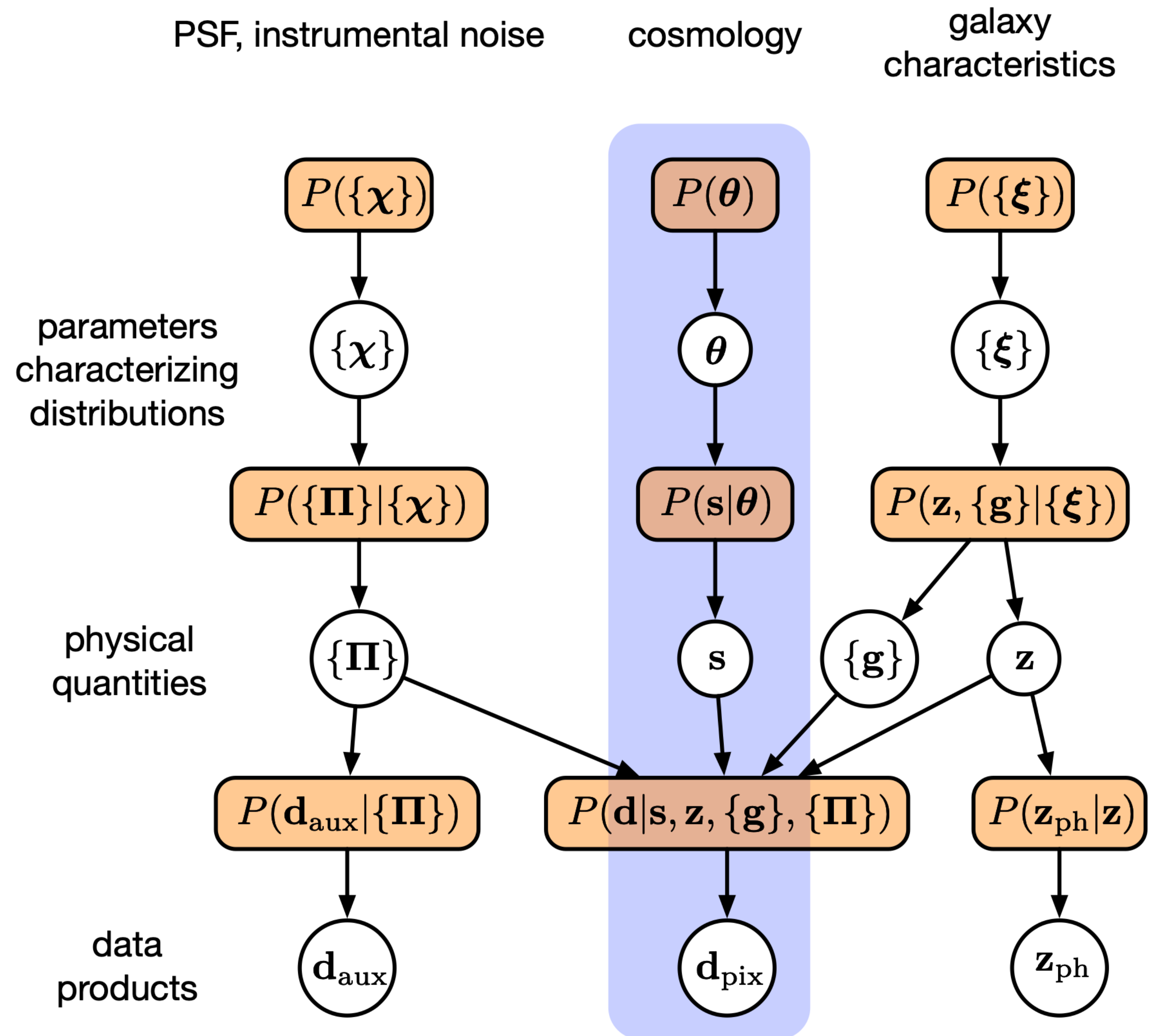
Porqueres et al. 2021(2108.04825)

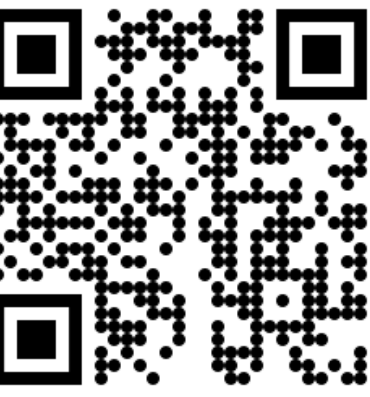


Cosmological Parameters

Ideal Bayesian Hierarchical Model For Weak Lensing Analysis

Alsing et al. 2015 (1505.078400)





3. Almanac

Sampling full sky cosmological fields and their power spectra

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Spin-0 and Spin-2 Cosmological Fields

An arbitrary spin- s field can be represented in the basis of spin- s spherical harmonics

$$f(\hat{n}) = \sum_{\ell m} f_{\ell m} {}_s Y_{\ell m}(\hat{n})$$

With

$$f_{\ell m} = \int d\Omega f(\hat{n}) {}_s Y_{\ell m}^*(\hat{n})$$

And covariance

$$\mathbf{C} \equiv \langle f_{\ell m} f_{\ell' m'}^* \rangle \delta_{\ell \ell'} \delta_{m m'}$$

Almanac

Spin-0 and Spin-2 Cosmological Fields

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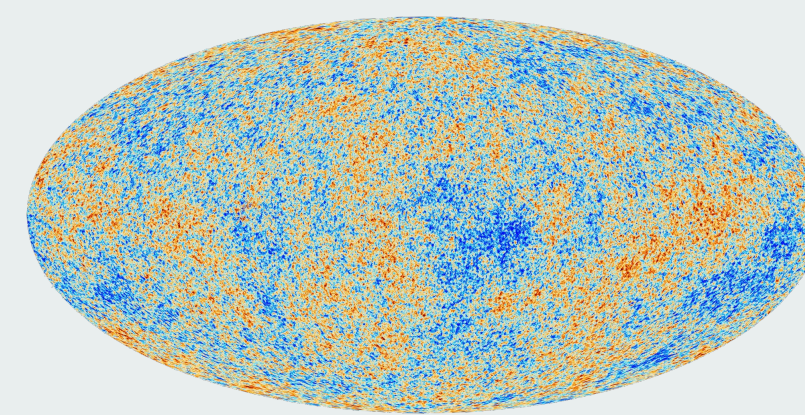
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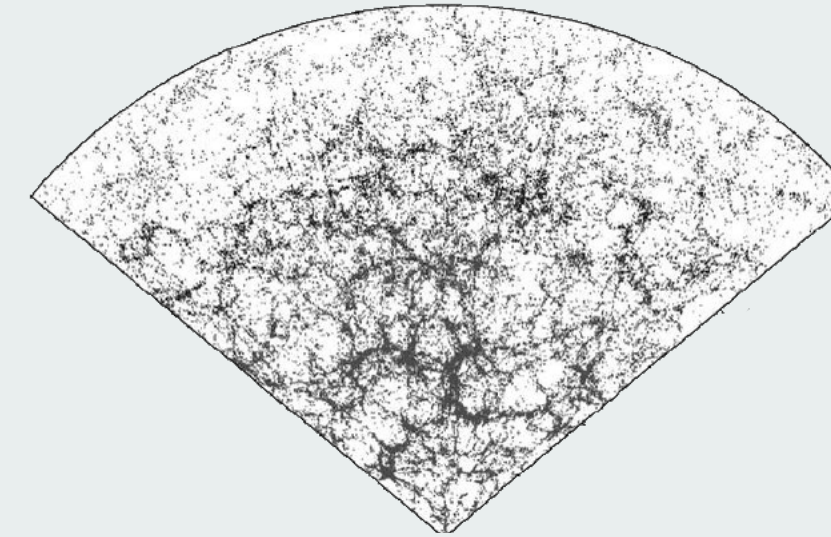
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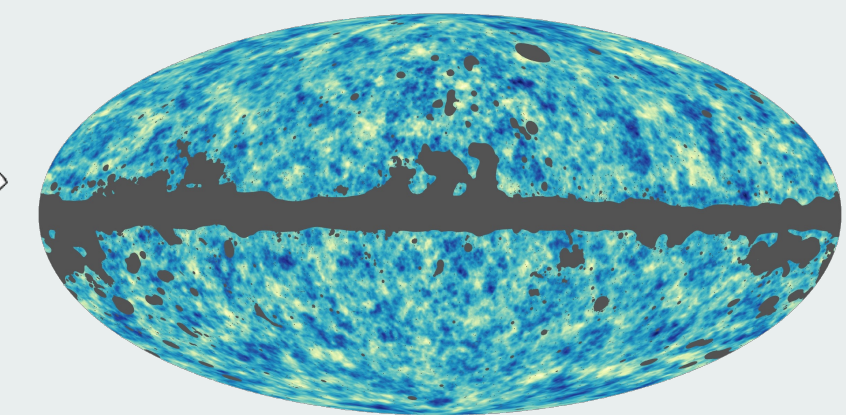
Spin-0 Fields



CMB Temperature



Galaxy Clustering



Lensing Convergence

Almanac

Spin-0 and Spin-2 Cosmological Fields

An arbitrary spin- s field can be represented in the basis of spin- s spherical harmonics

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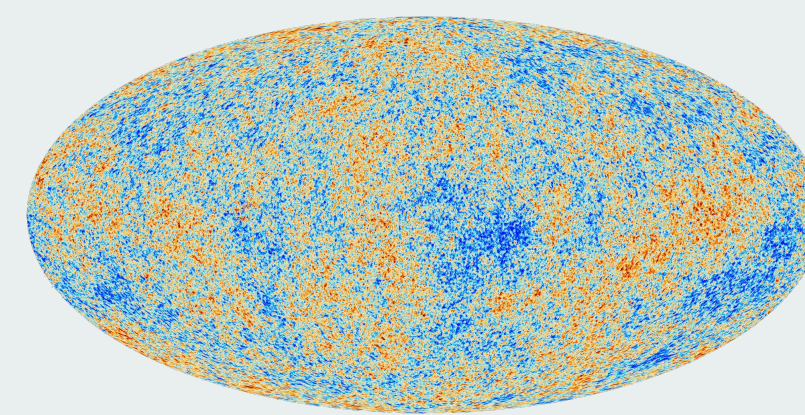
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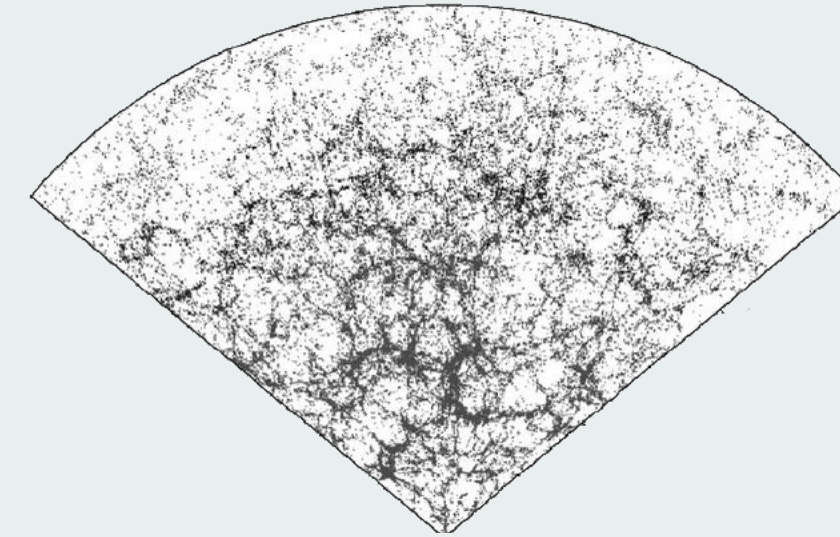
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$$\mathbf{C} \equiv \langle f_{\ell m} f_{\ell' m'}^* \rangle \delta_{\ell \ell'} \delta_{m m'}$$

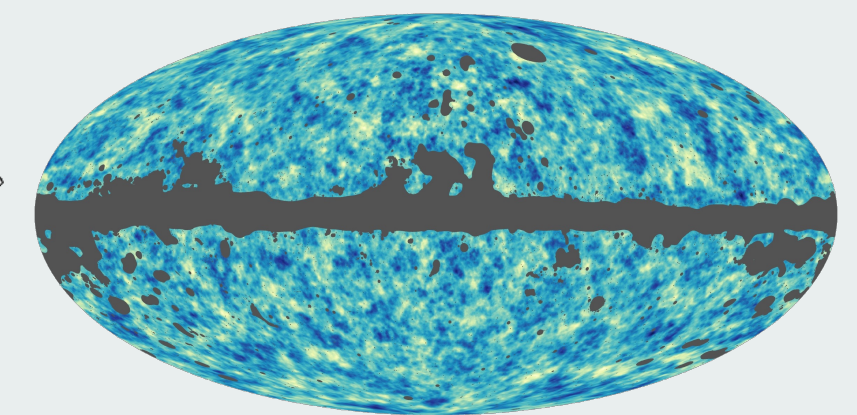
Spin-0 Fields



CMB Temperature

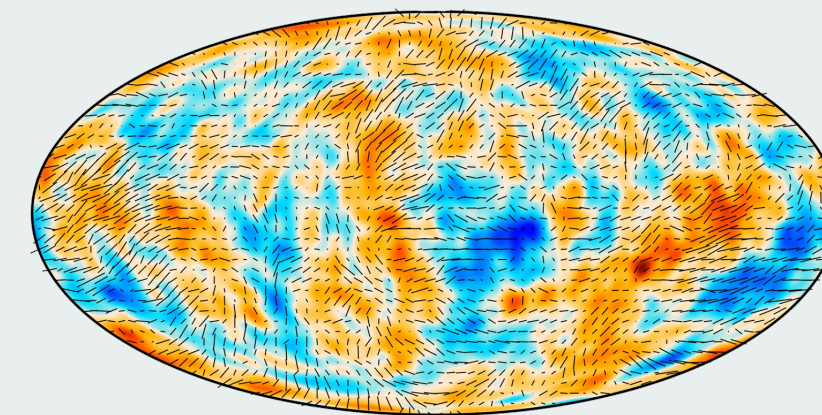


Galaxy Clustering

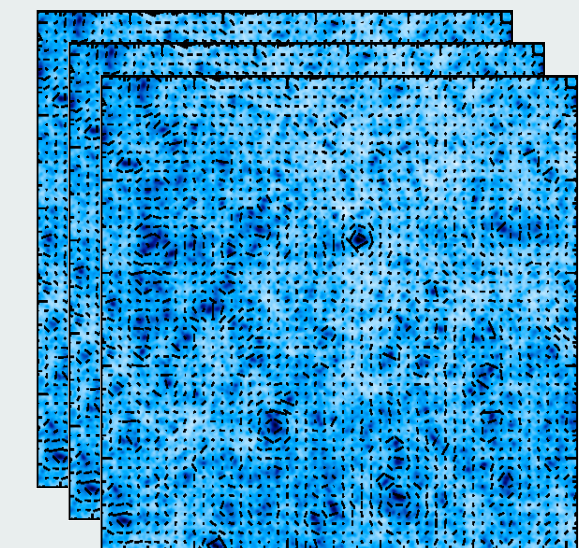


Lensing Convergence

Spin-2 Fields



CMB Polarisation

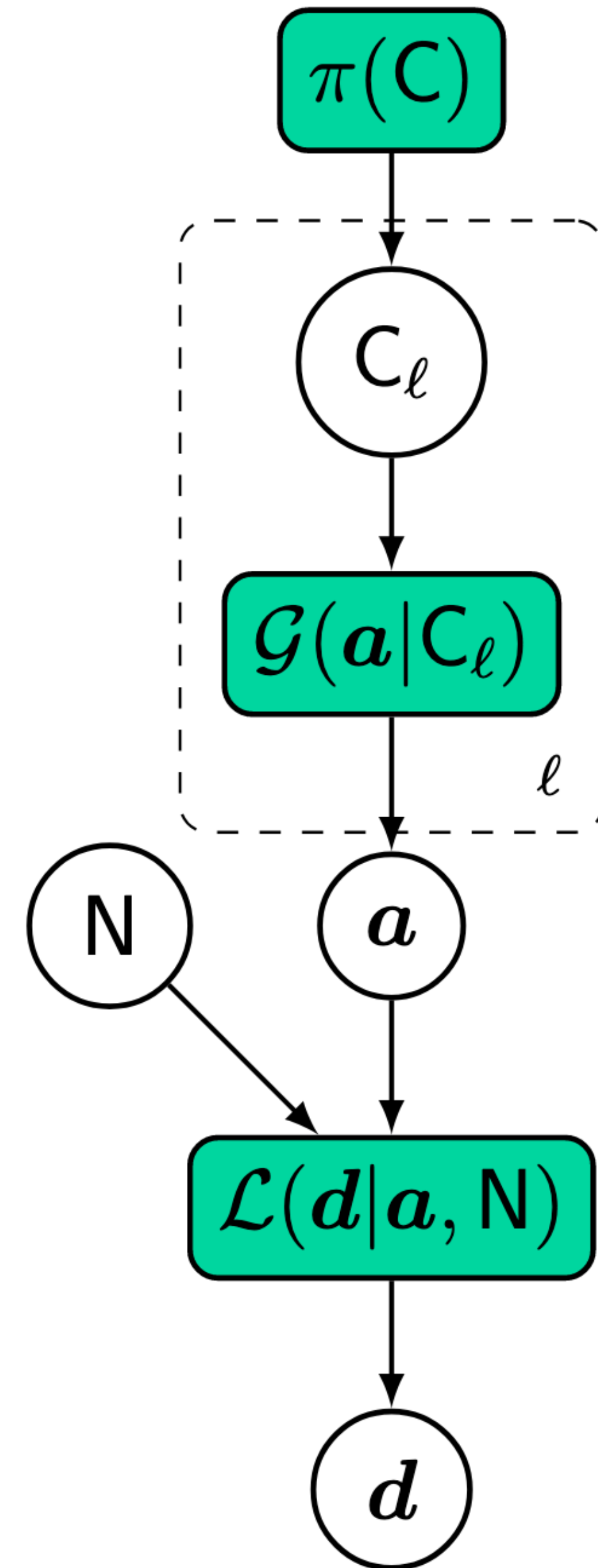


Cosmic Shear

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Directed Acyclical
Graph & posterior

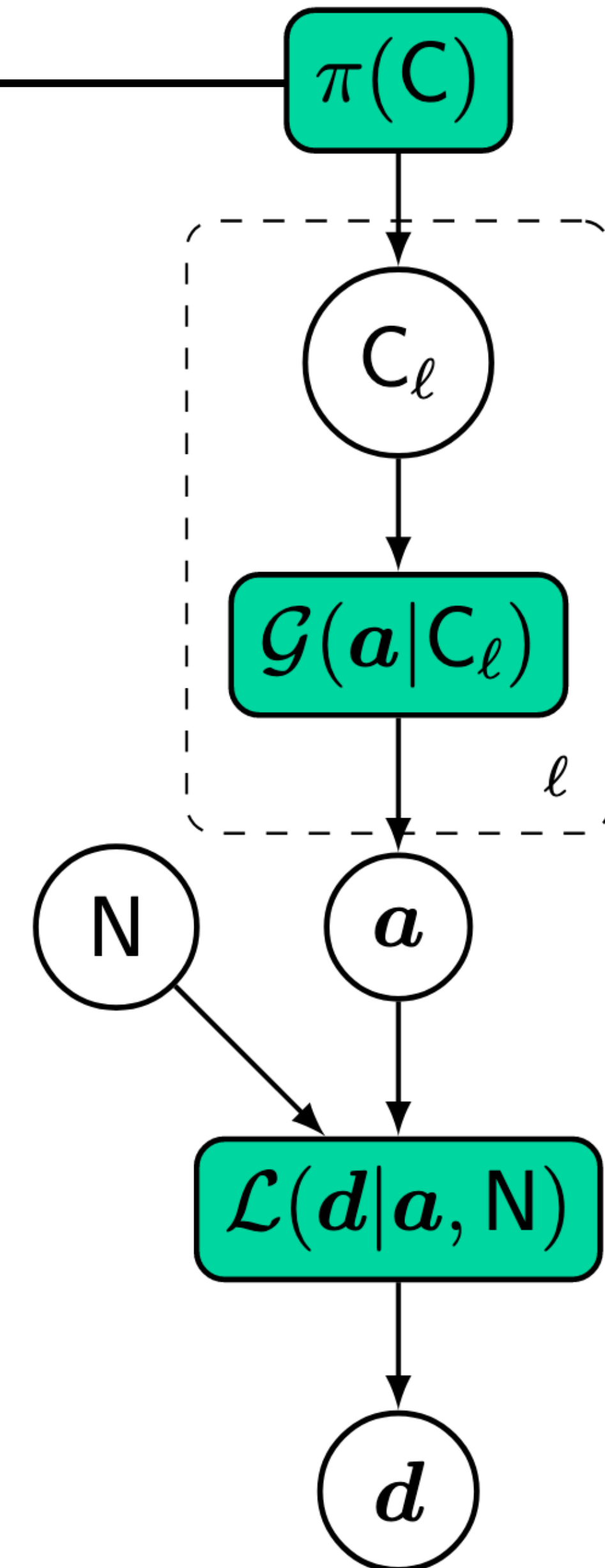
$$\mathcal{P}(\mathbf{C}, \mathbf{a} | \mathbf{d}, \mathbf{N}) \propto \mathcal{L}(\mathbf{d} | \mathbf{a}, \mathbf{N}) \mathcal{G}(\mathbf{a} | \mathbf{C}) \pi(\mathbf{C})$$



Almanac

Directed Acyclical Graph & posterior

$$\pi(\mathbf{C}) = |\mathbf{C}|^q$$

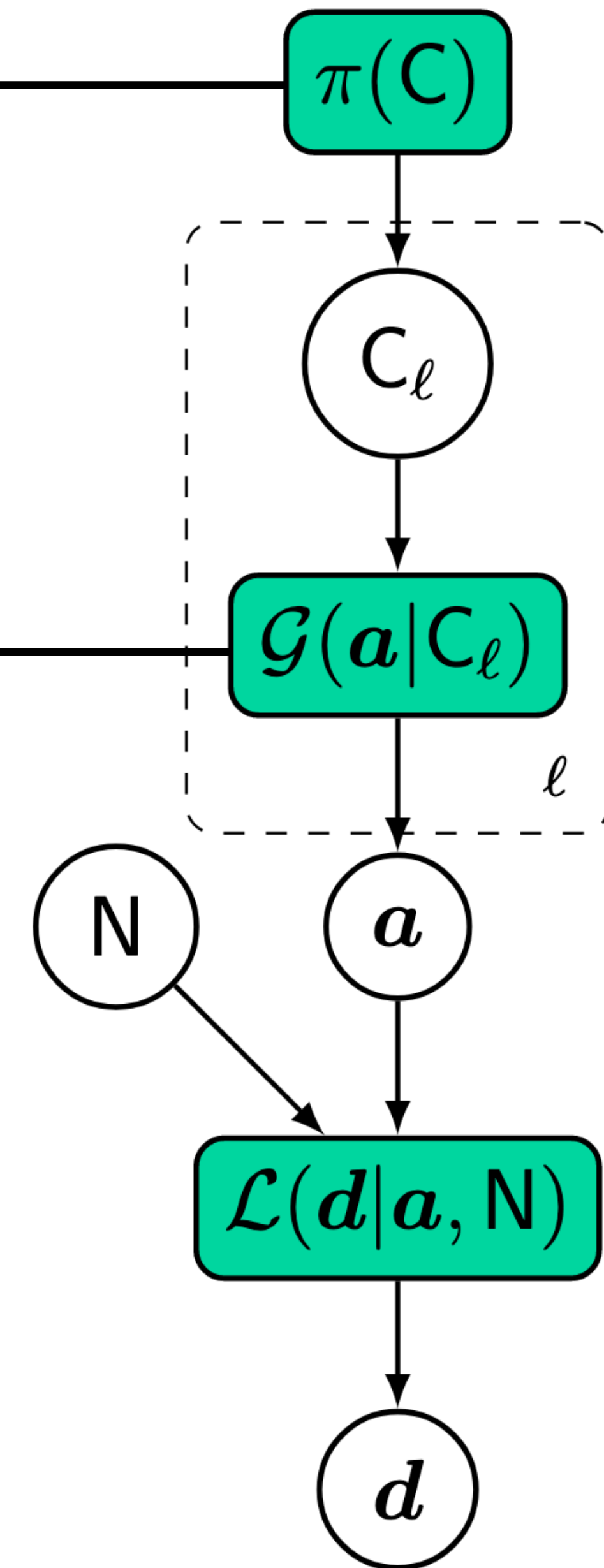


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Directed Acyclical Graph & posterior

$$\mathcal{G}(\mathbf{a}|\mathbf{C}) = \frac{1}{\sqrt{|2\pi\mathbf{C}|}} \exp\left(-\frac{1}{2}\mathbf{a}^T\mathbf{C}^{-1}\mathbf{a}\right)$$

$$\pi(\mathbf{C}) = |\mathbf{C}|^q$$



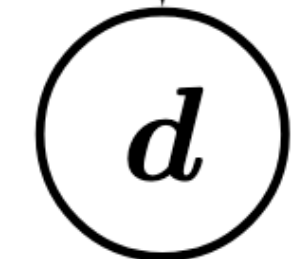
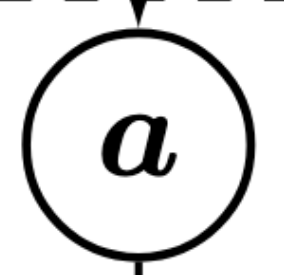
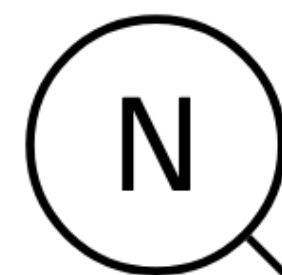
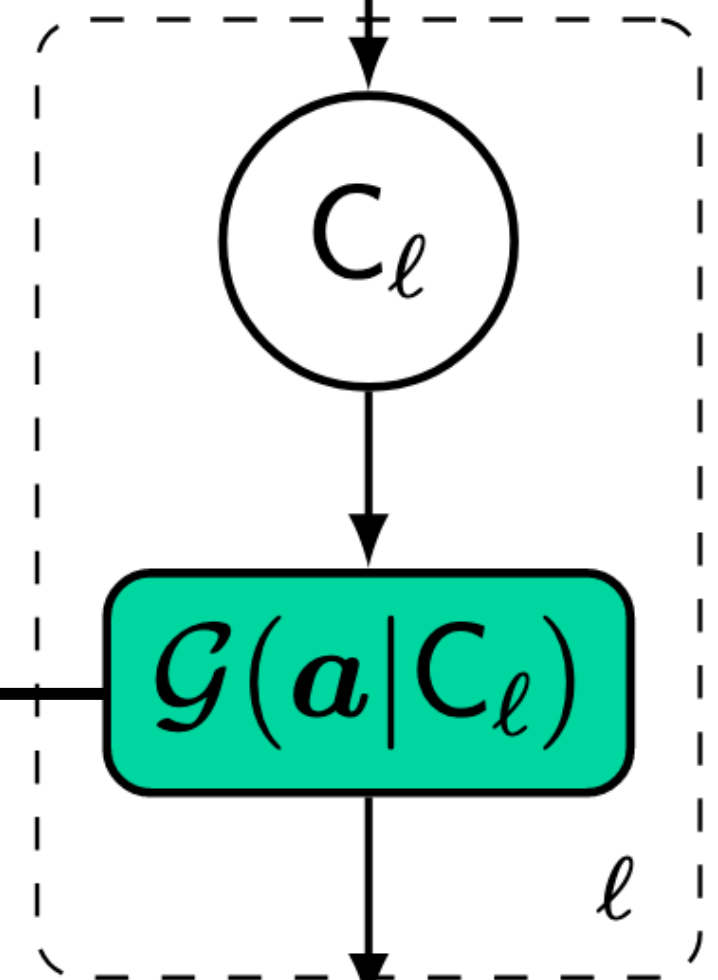
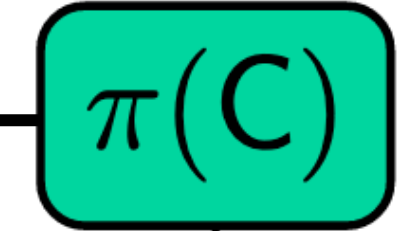
Almanac

Directed Acyclical Graph & posterior

$$\pi(\mathbf{C}) = |\mathbf{C}|^q$$

$$\mathcal{G}(\mathbf{a}|\mathbf{C}) = \frac{1}{\sqrt{|2\pi\mathbf{C}|}} \exp\left(-\frac{1}{2}\mathbf{a}^T\mathbf{C}^{-1}\mathbf{a}\right)$$

$$\mathcal{L}(\mathbf{d}|\mathbf{a}, \mathbf{N}) \propto \exp\left[-\frac{1}{2}(\mathbf{d} - \mathbf{Y}\mathbf{a})^T\mathbf{N}^{-1}(\mathbf{d} - \mathbf{Y}\mathbf{a})\right]$$



Almanac

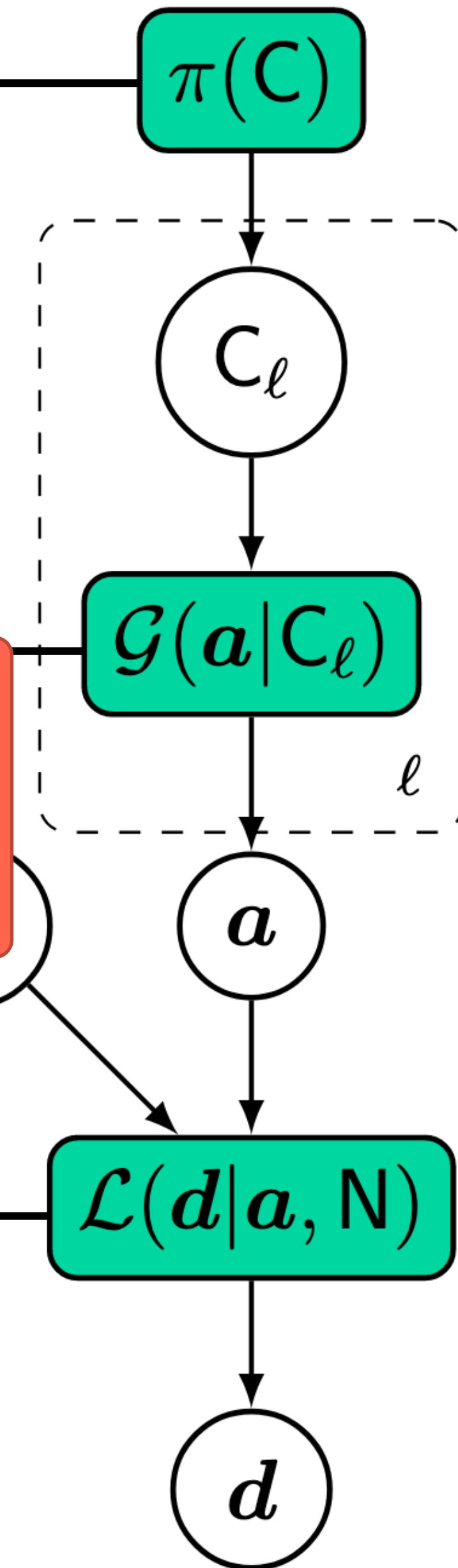
Directed Acyclical Graph & posterior

$$\pi(\mathbf{C}) = |\mathbf{C}|^q$$

$$\mathcal{G}(\mathbf{a}|\mathbf{C}) \propto \prod_{i=1}^n \left(\prod_{j=1}^{T_{\mathbf{C}-1}} \right)$$

Gaussian Prior DOES NOT mean a Gaussian posterior!!!

$$\mathcal{L}(\mathbf{d}|\mathbf{a}, \mathbf{N}) \propto \exp \left[-\frac{1}{2} (\mathbf{d} - \mathbf{Y}\mathbf{a})^T \mathbf{N}^{-1} (\mathbf{d} - \mathbf{Y}\mathbf{a}) \right]$$

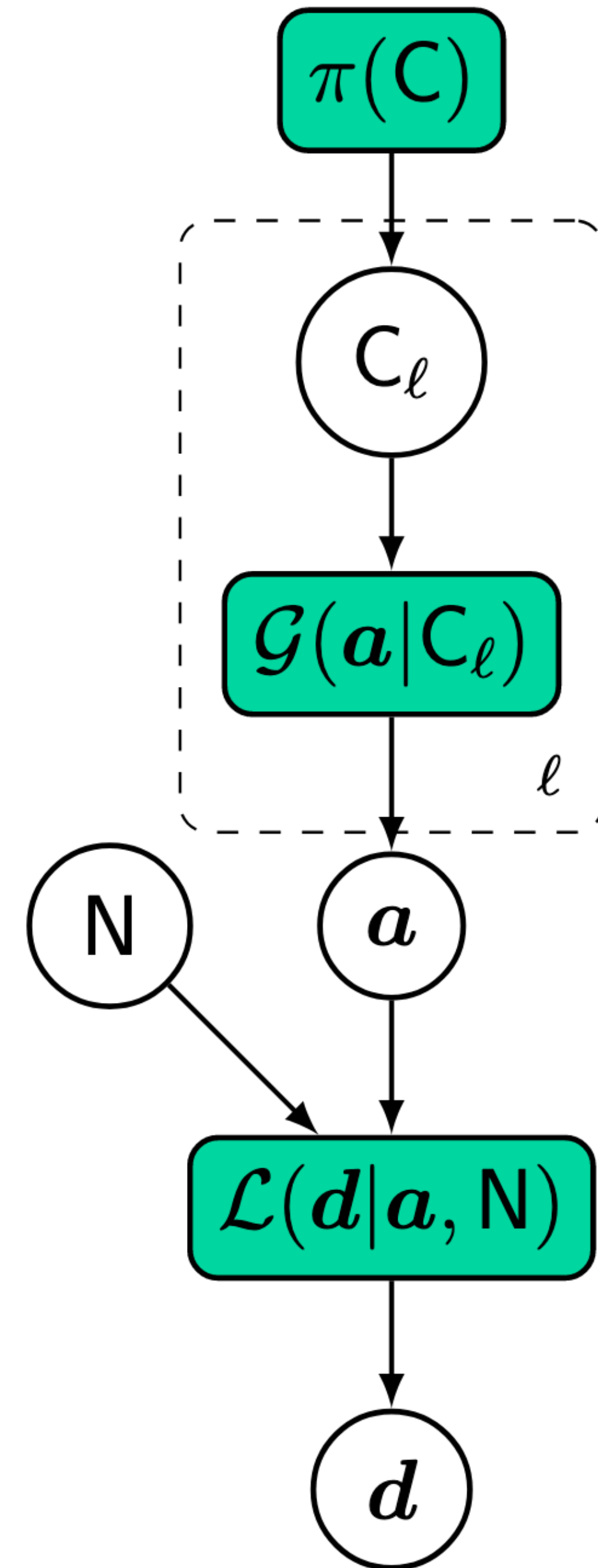


Almanac

Directed Acyclical
Graph & posterior

$$\mathcal{P}(\mathbf{C}, \mathbf{a} | \mathbf{d}, \mathbf{N}) \propto \mathcal{L}(\mathbf{d} | \mathbf{a}, \mathbf{N}) \mathcal{G}(\mathbf{a} | \mathbf{C}) \pi(\mathbf{C})$$

$\sim 10^6 - 10^8$ parameters



4. Sampling High Dimensional Posteriors

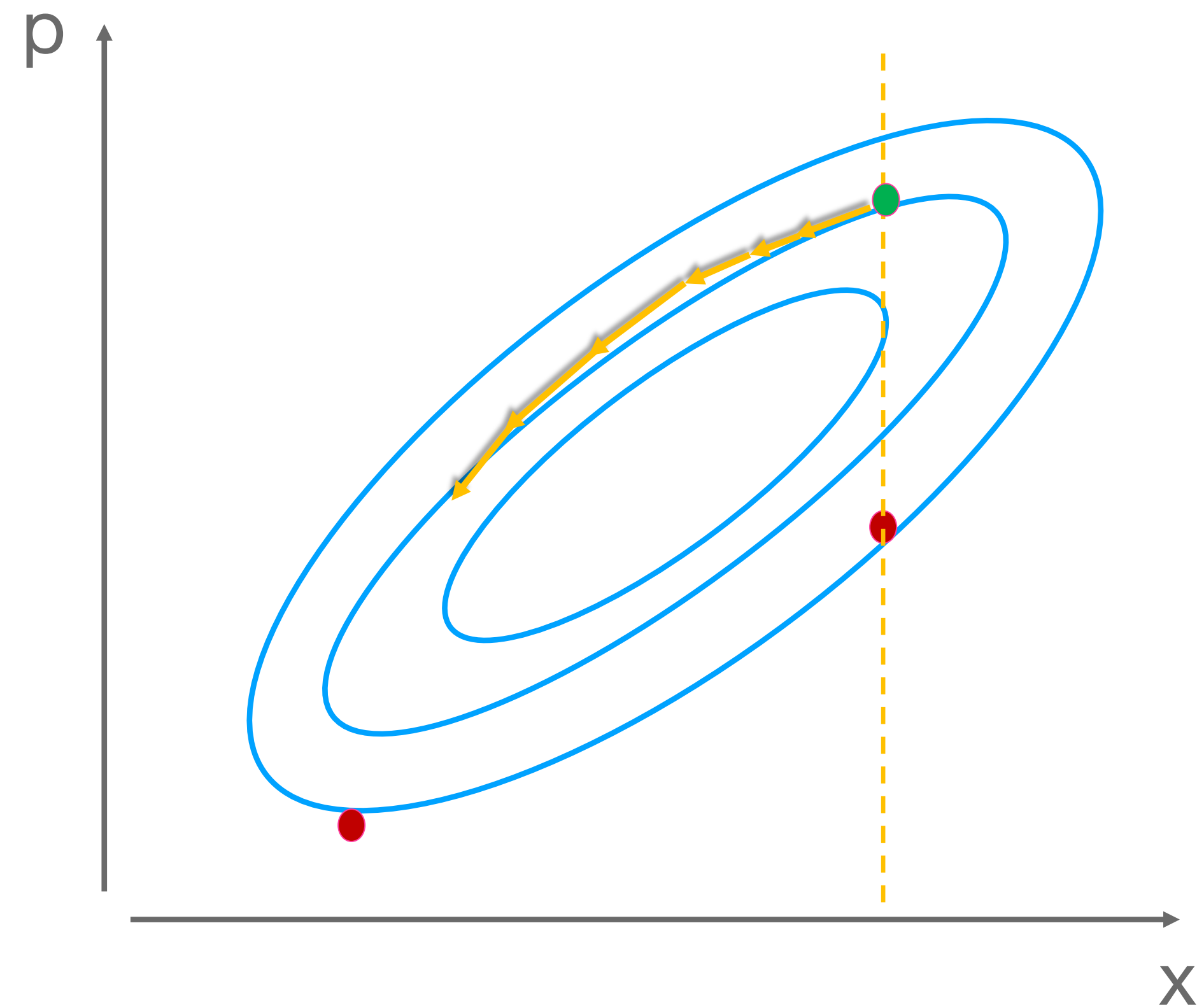
Coordinate Transformations & the Tuned Hamiltonian Monte-Carlo

Hamiltonian Monte Carlo

- Explores the phase space using an analogy with dynamical systems with our parameters being the positions

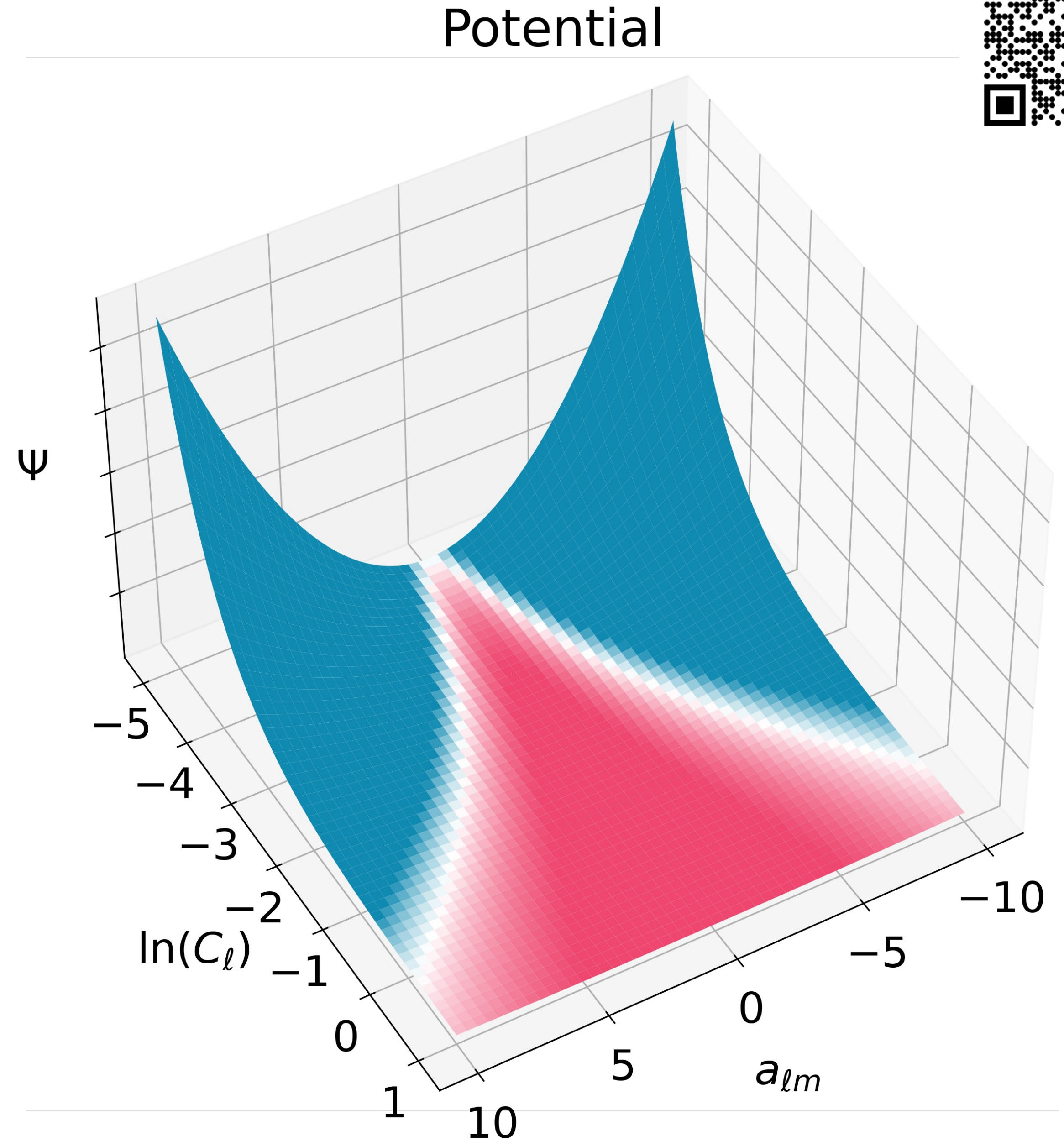
$$\mathcal{H} = \sum_i^N \frac{p_i^2}{2m_i} + \Psi(\mathbf{a}, \mathbf{C}_\ell)$$

- The potential is related to the posterior:
$$\Psi(\mathbf{a}, \mathbf{C}_\ell) = -\ln p(\mathbf{a}, \mathbf{C}_\ell | \mathbf{d}, \mathbf{N})$$
- Evolves as a dynamical system with the momenta marginalized over



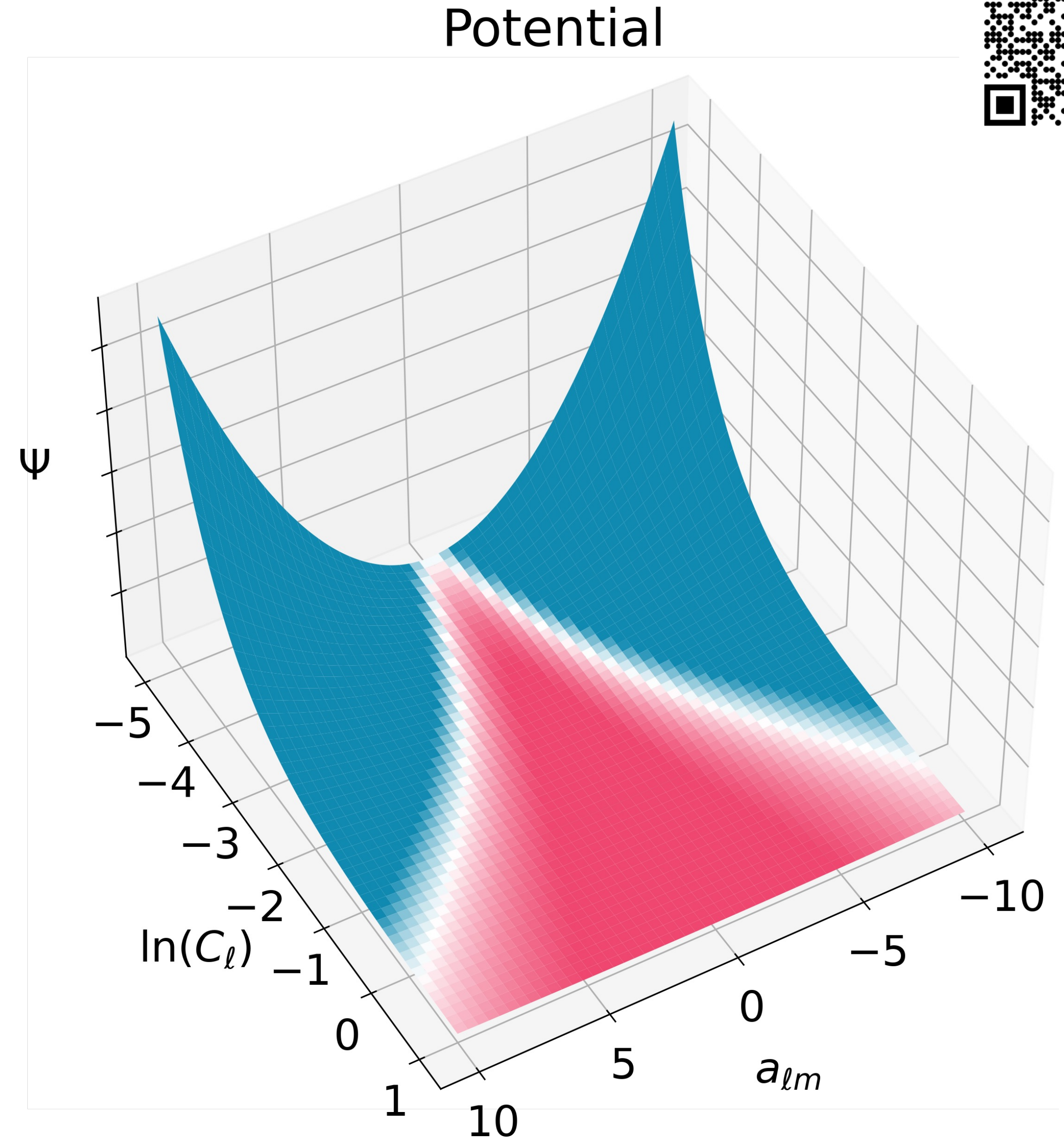
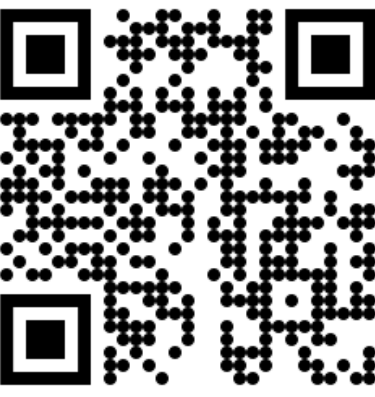
The sting-ray problem

- The C matrix needs to be positive definite



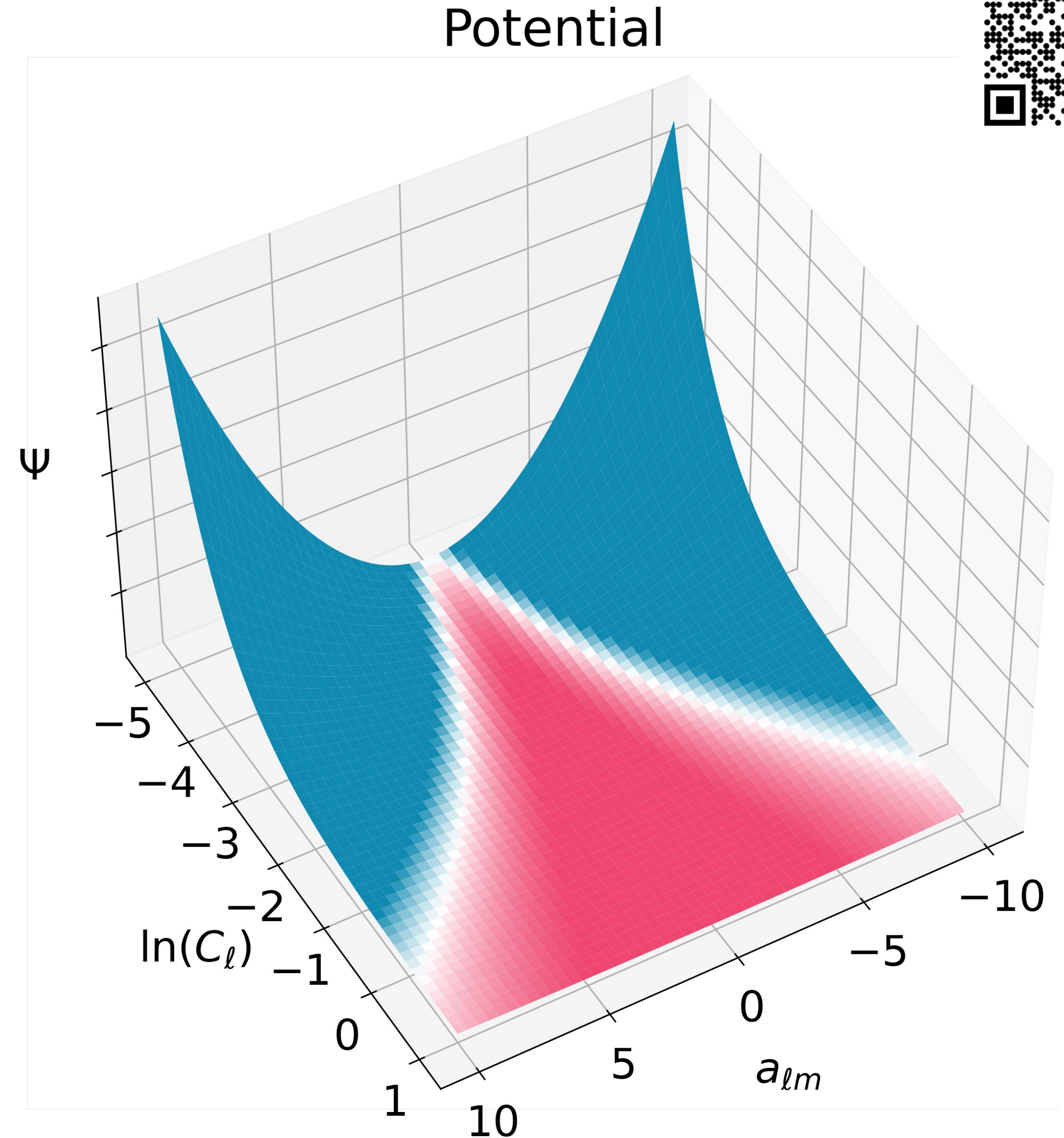
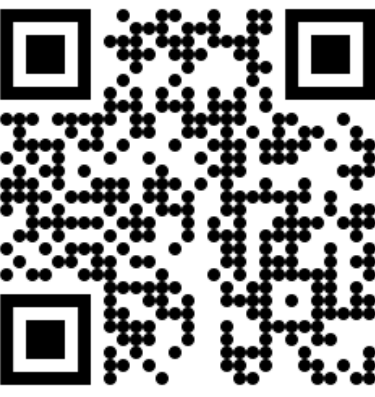
The sting-ray problem

- The C matrix needs to be positive definite
- The most straightforward coordinate system to ensure this is using \mathbf{a} and $G = \ln(C)$.



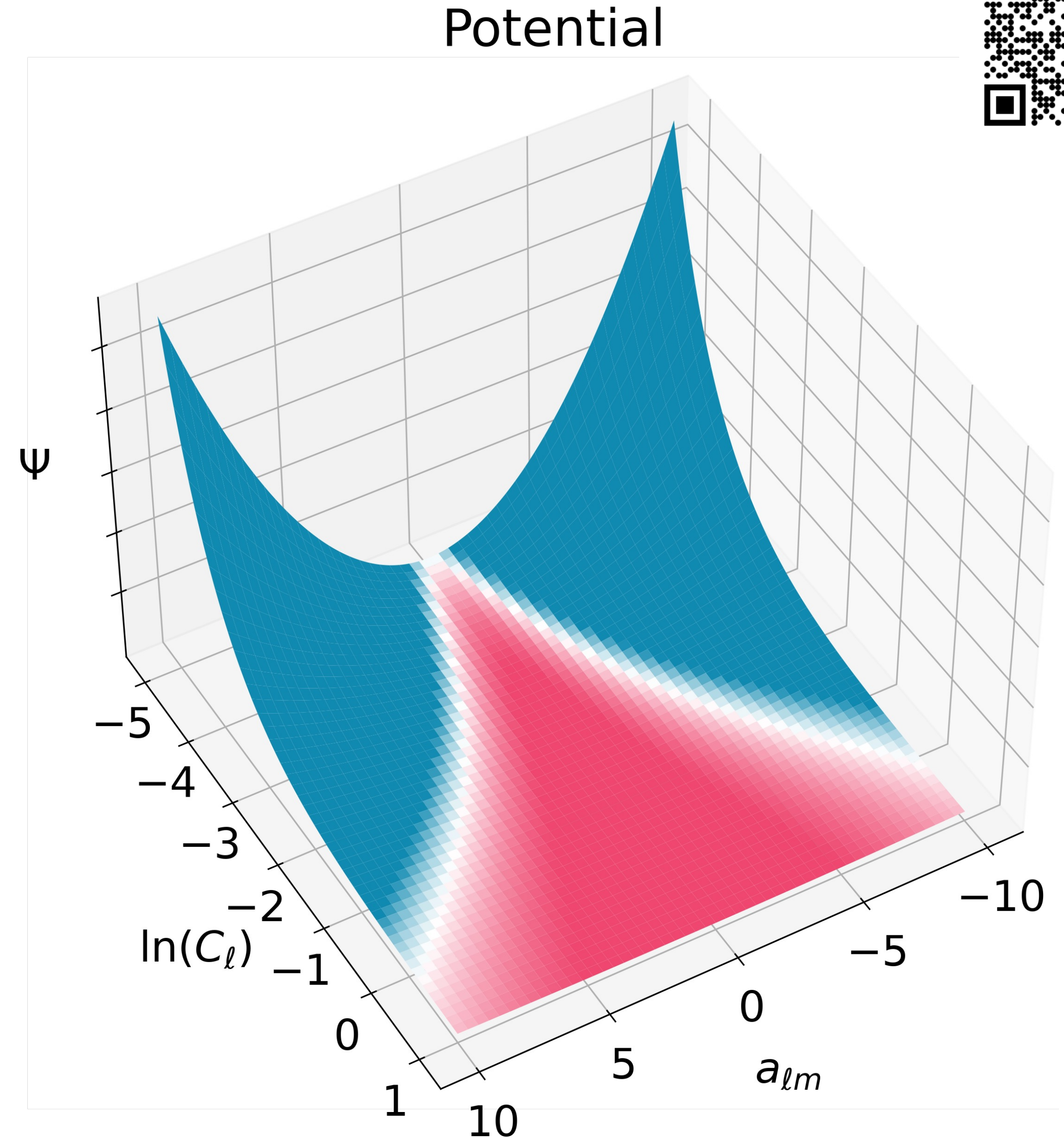
The sting-ray problem

- The C matrix needs to be positive definite
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- However, we fall into the Sting-Ray (Neil's Funnel) posterior problem



The sting-ray problem

- The C matrix needs to be positive definite
- The most straightforward coordinate system to ensure this is using \mathbf{a} and $G = \ln(C)$.
- However, we fall into the Sting-Ray (Neil's Funnel) posterior problem
- Sampler becomes inefficient



The sting-ray problem: SOLVED

- Rescaling the fields by their standard deviation

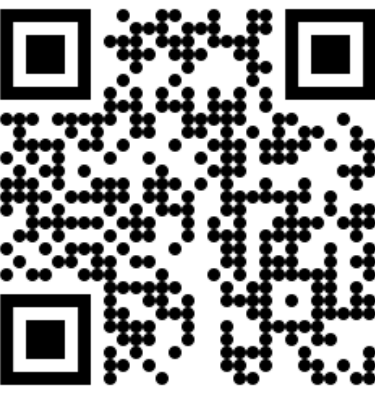
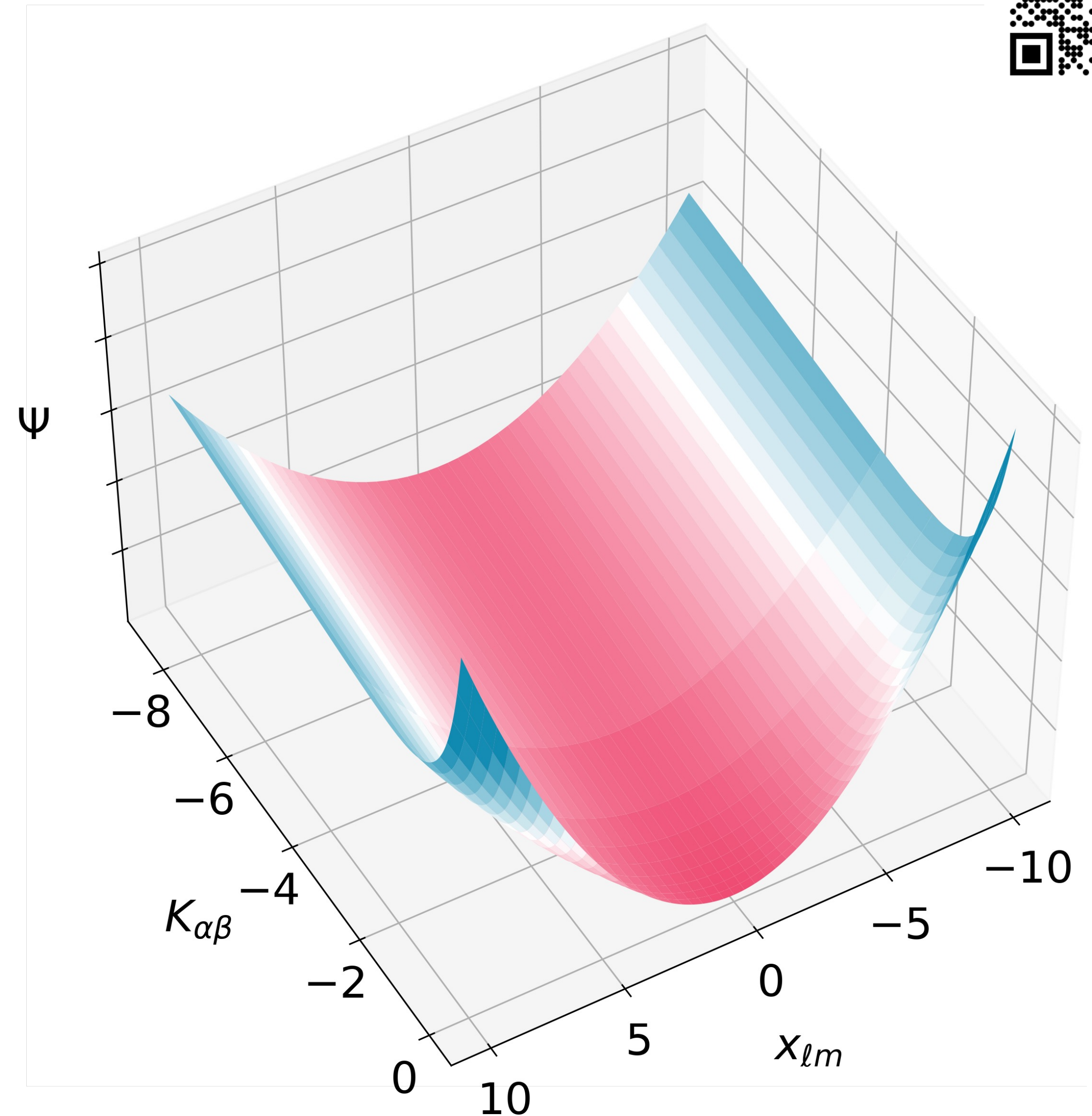
$$\mathbf{x} = \mathbf{L}^{-1} \mathbf{a}$$

where $\mathbf{C} = \mathbf{L}\mathbf{L}^T$

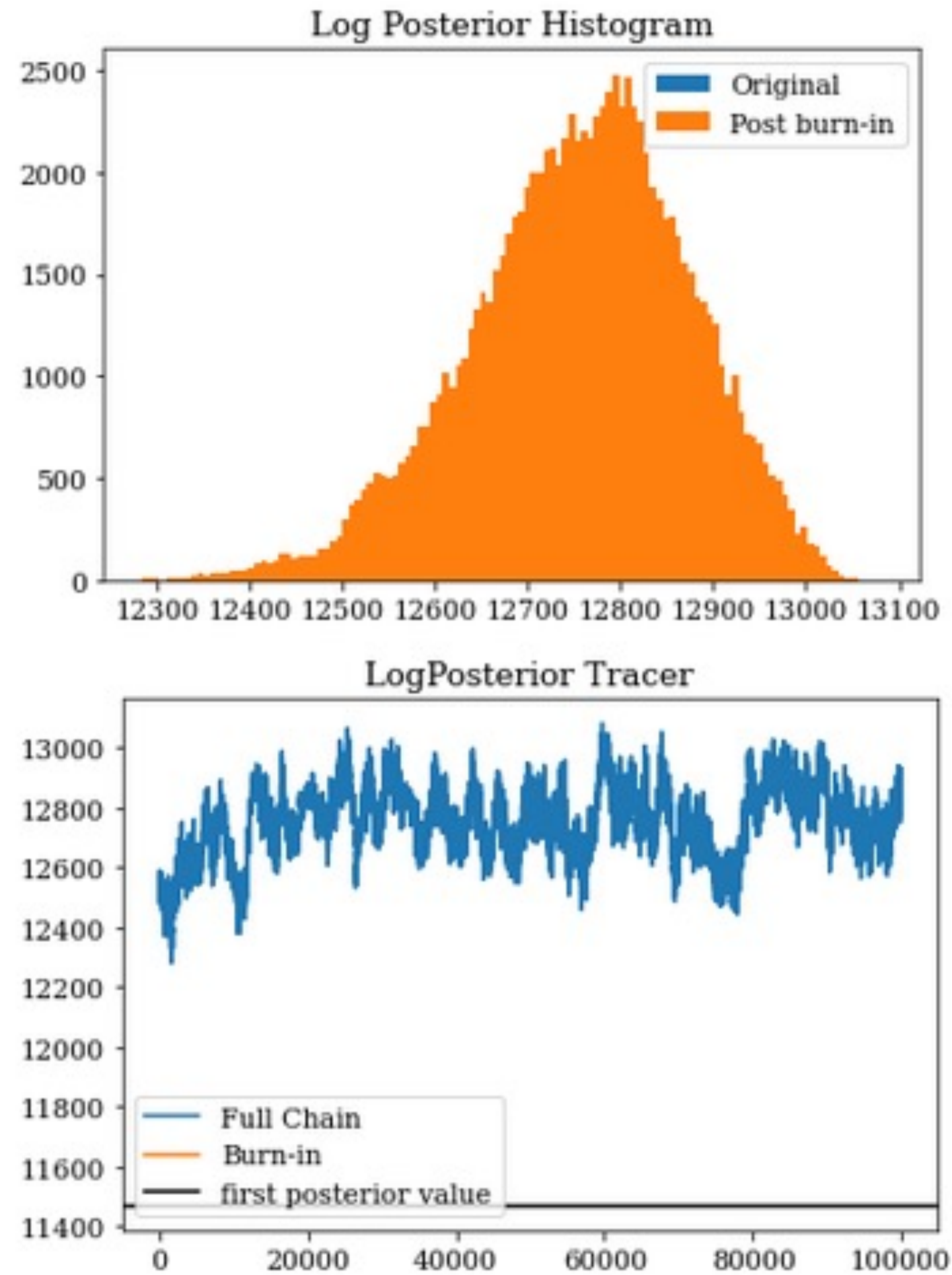
- Taking the diagonal-log of the Cholesky decomposed covariance

$$K_{\alpha\beta} = \begin{cases} \ln(L_{\alpha\beta}) & \text{if } \alpha = \beta, \\ L_{\alpha\beta} & \text{otherwise.} \end{cases}$$

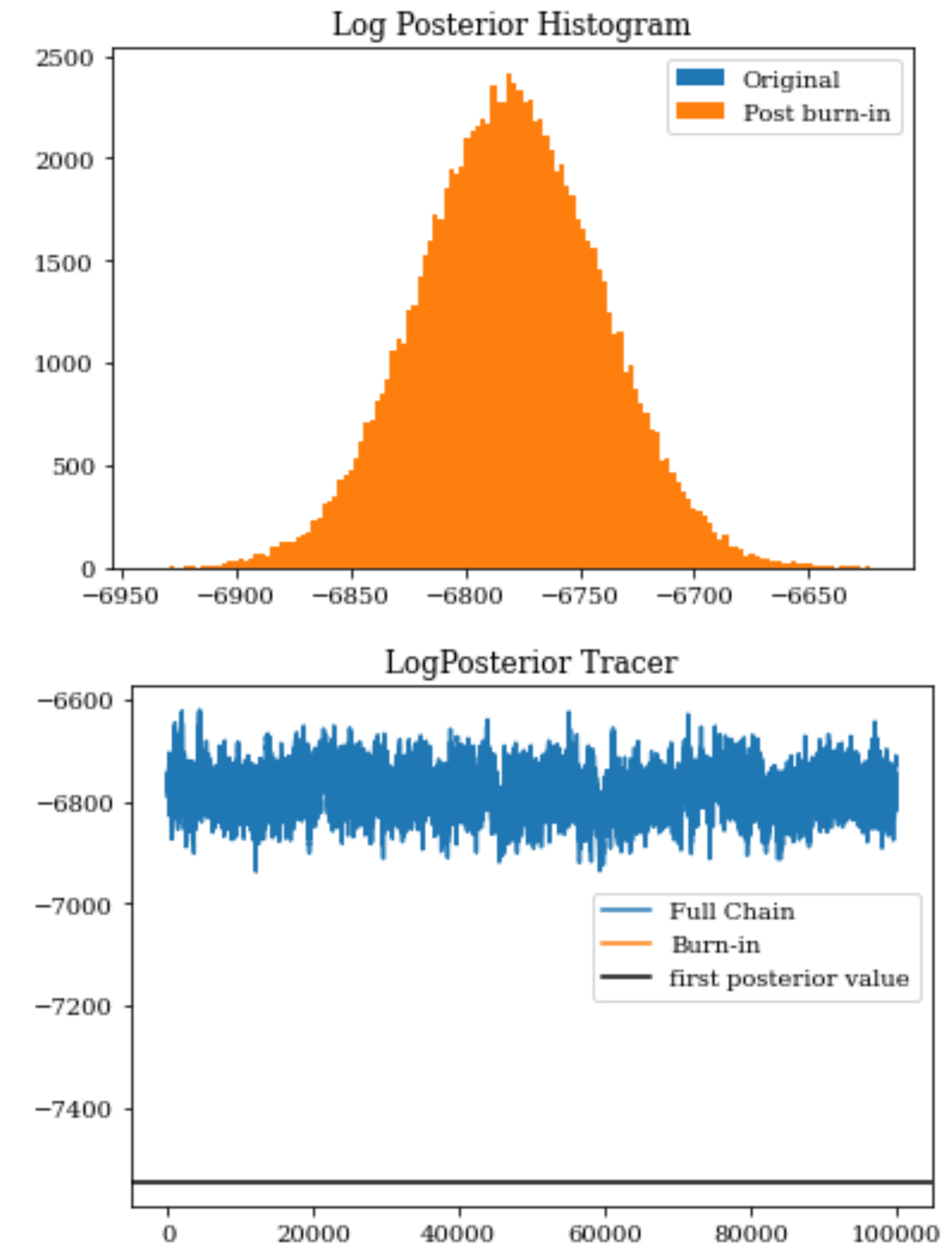
Potential



Coordinate System comparison



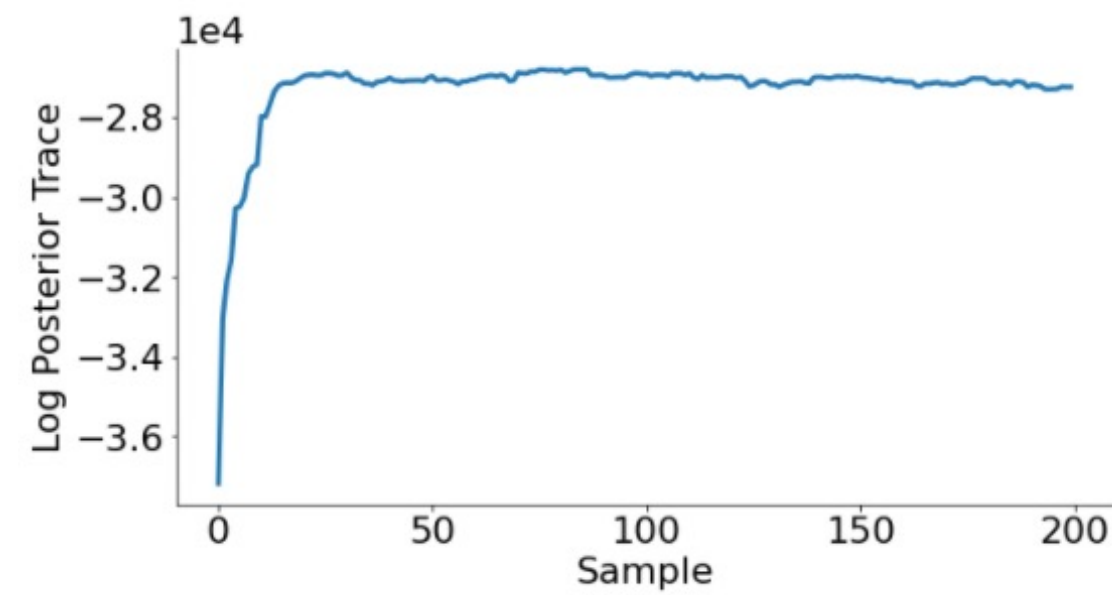
Naïve: $G_\ell = \log(C_\ell)$ & $a_{\ell m}$



Cholesky: K_{ij} & $x_{\ell m} = L^{-1} a_{\ell m}$

Tuned HMC

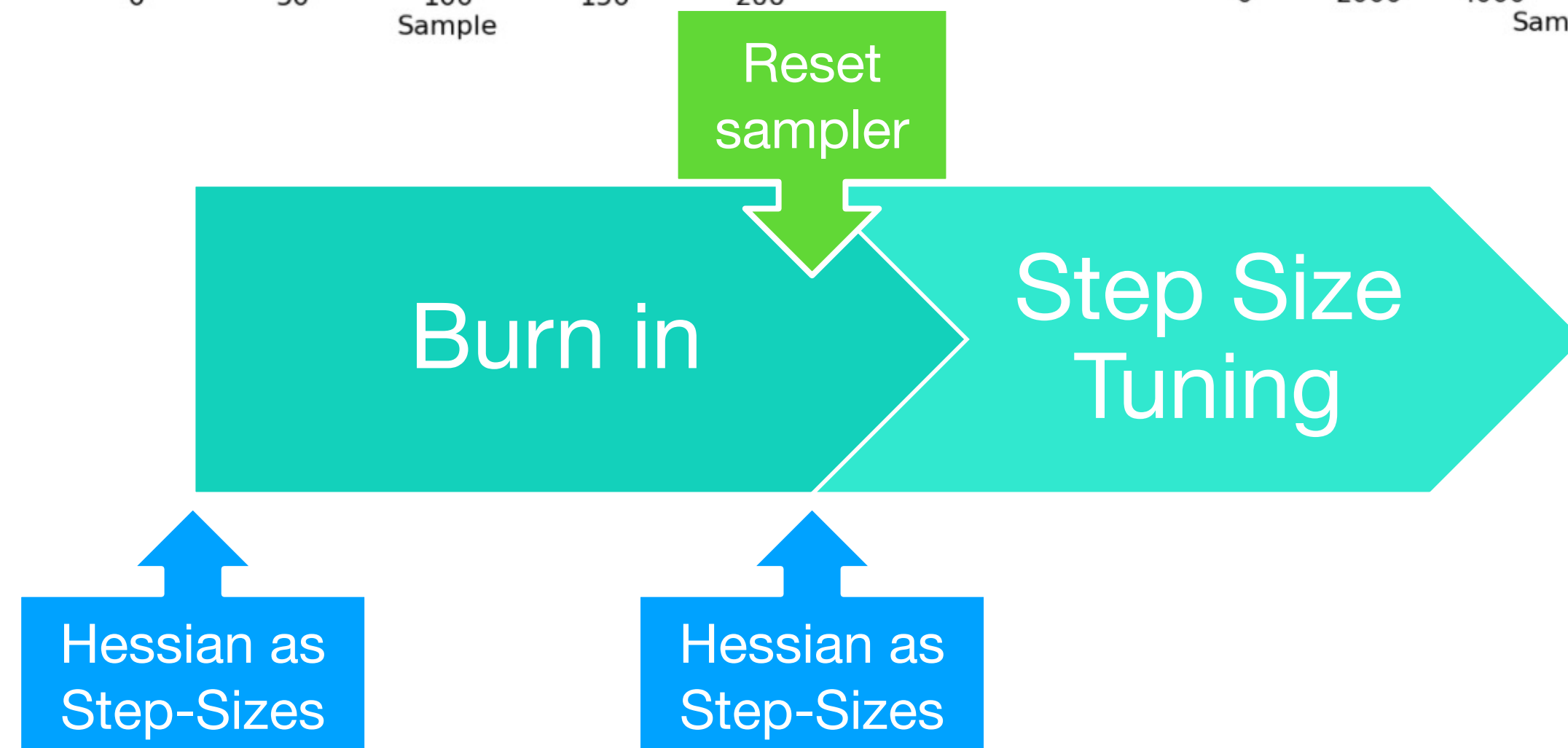
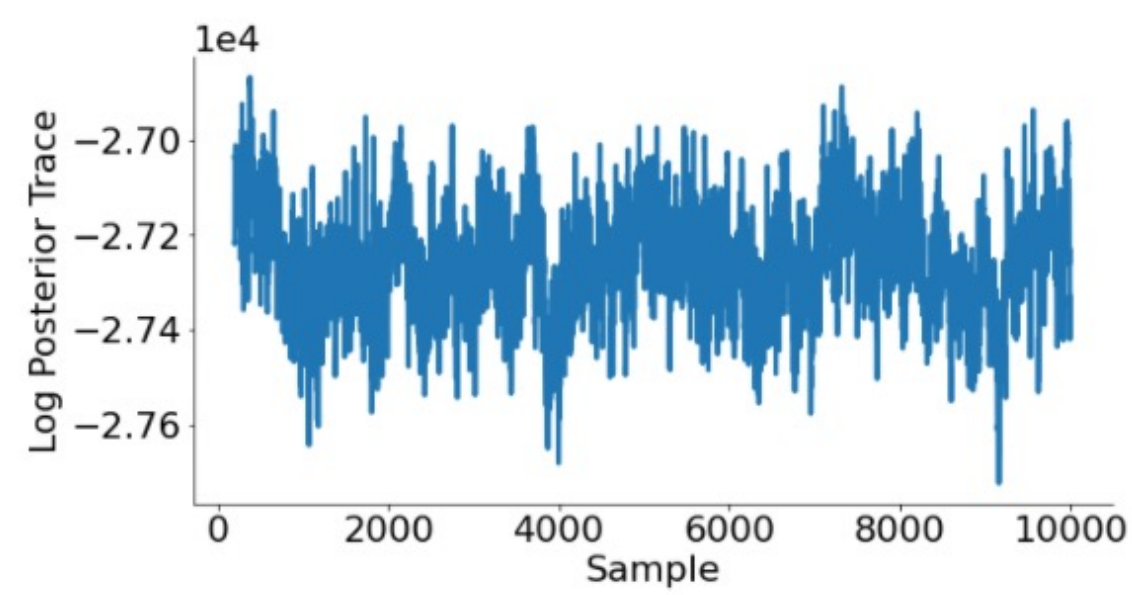
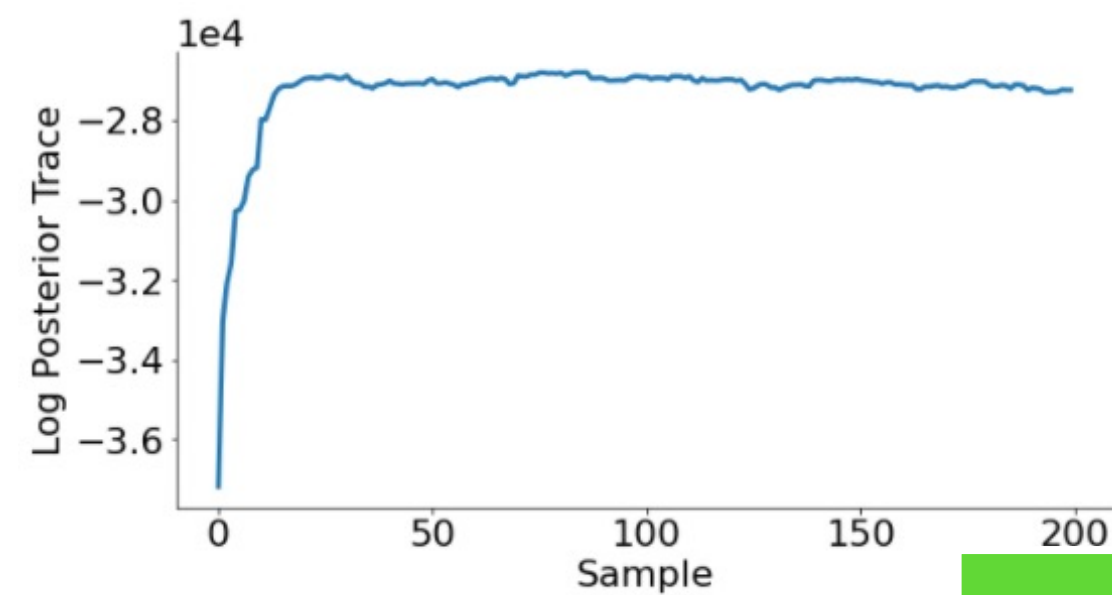
Three phase tuning



$$\mathcal{E} = \eta \left(\frac{\partial^2 \psi}{\partial \mathbf{x}^2} \right)^{-1/2}$$

Tuned HMC

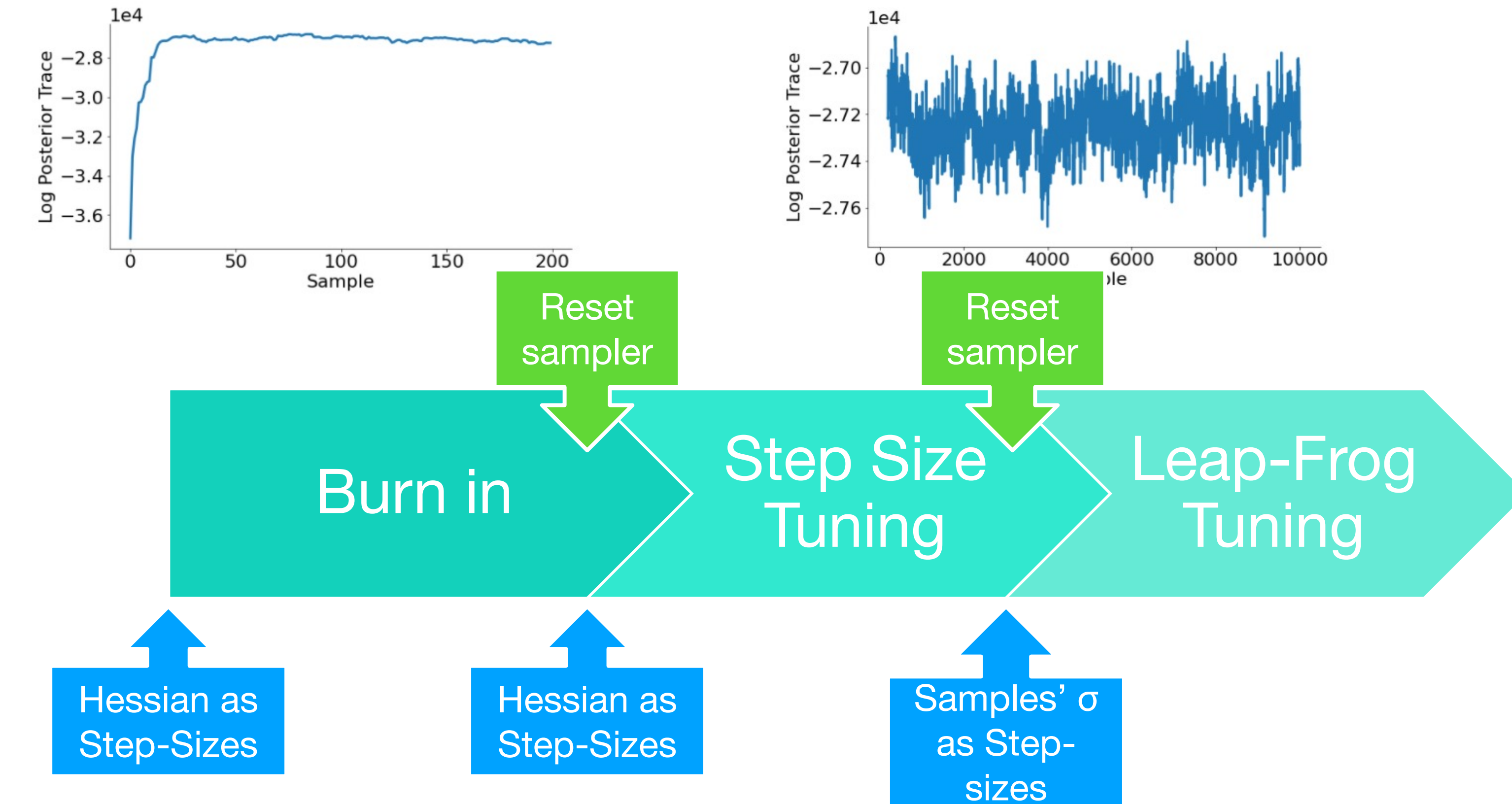
Three phase tuning



$$\mathcal{E} = \eta \left(\frac{\partial^2 \psi}{\partial \mathbf{x}^2} \right)^{-1/2}$$

Tuned HMC

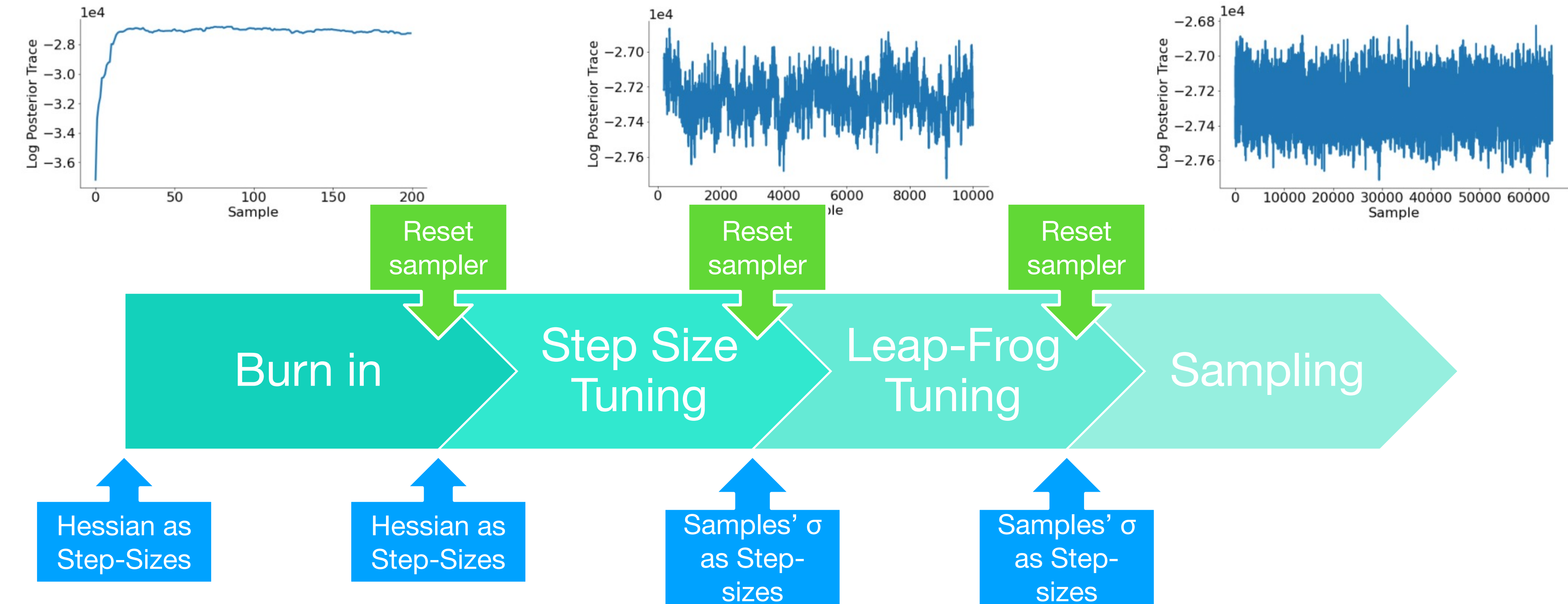
Three phase tuning



$$\mathcal{E} = \eta \left(\frac{\partial^2 \psi}{\partial \mathbf{x}^2} \right)^{-1/2}$$

Tuned HMC

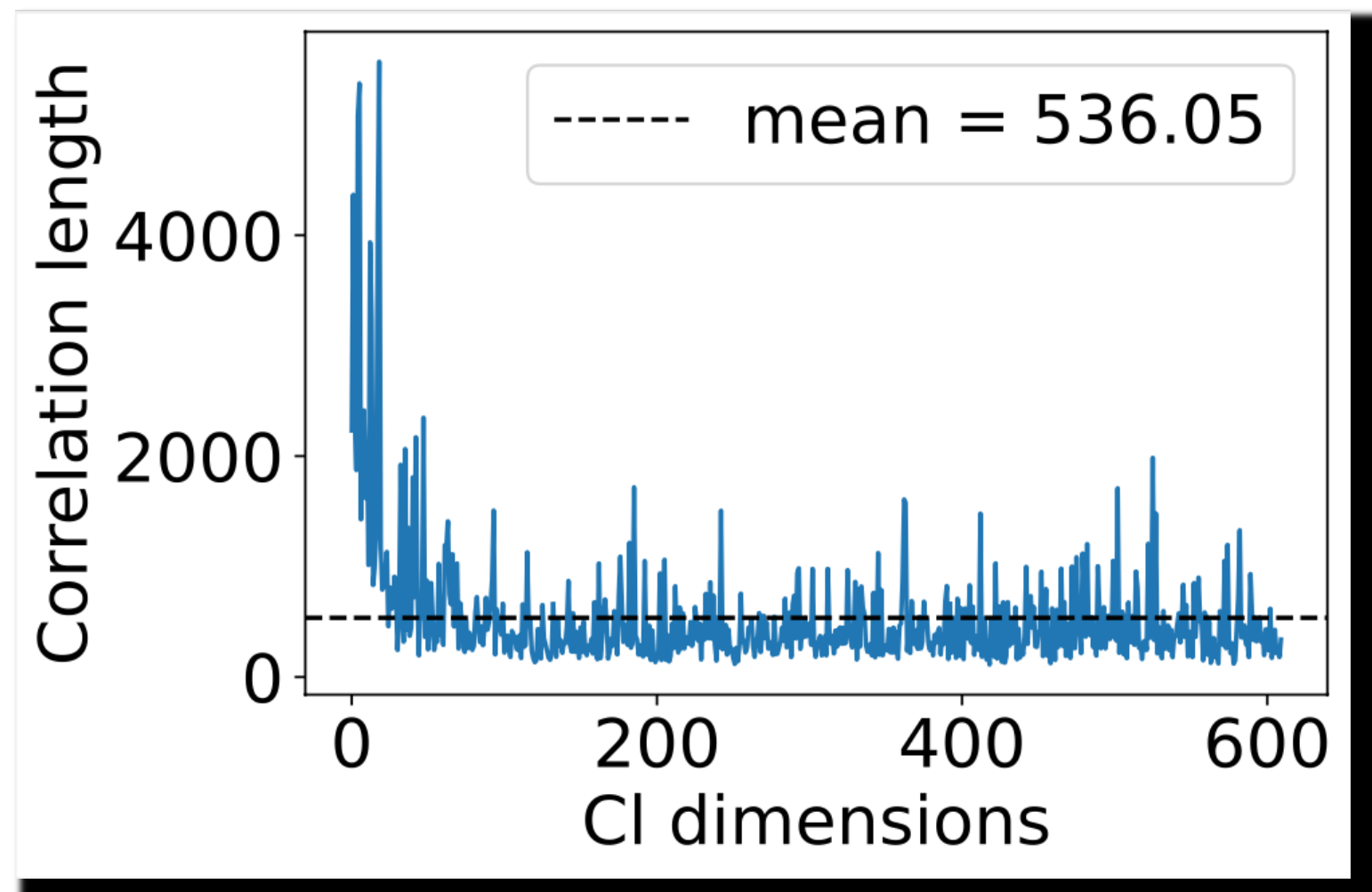
Three phase tuning



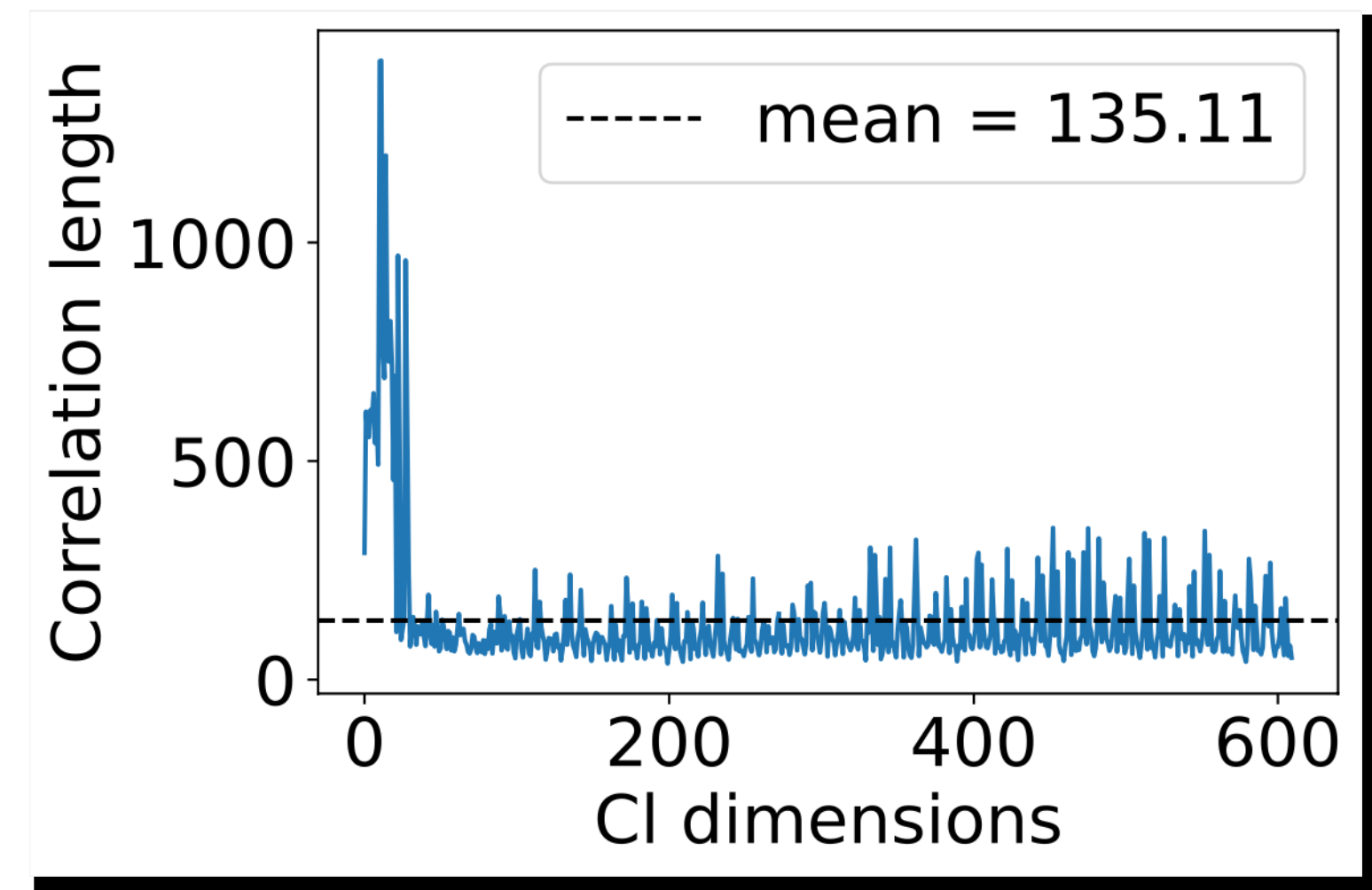
$$\mathcal{E} = \eta \left(\frac{\partial^2 \psi}{\partial \mathbf{x}^2} \right)^{-1/2}$$

Tuned HMC

Three phase tuning



Normal HMC



Tuned HMC

5. Applications to Weak Lensing

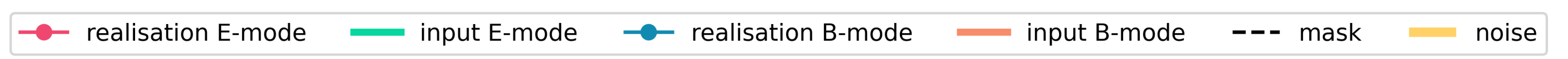
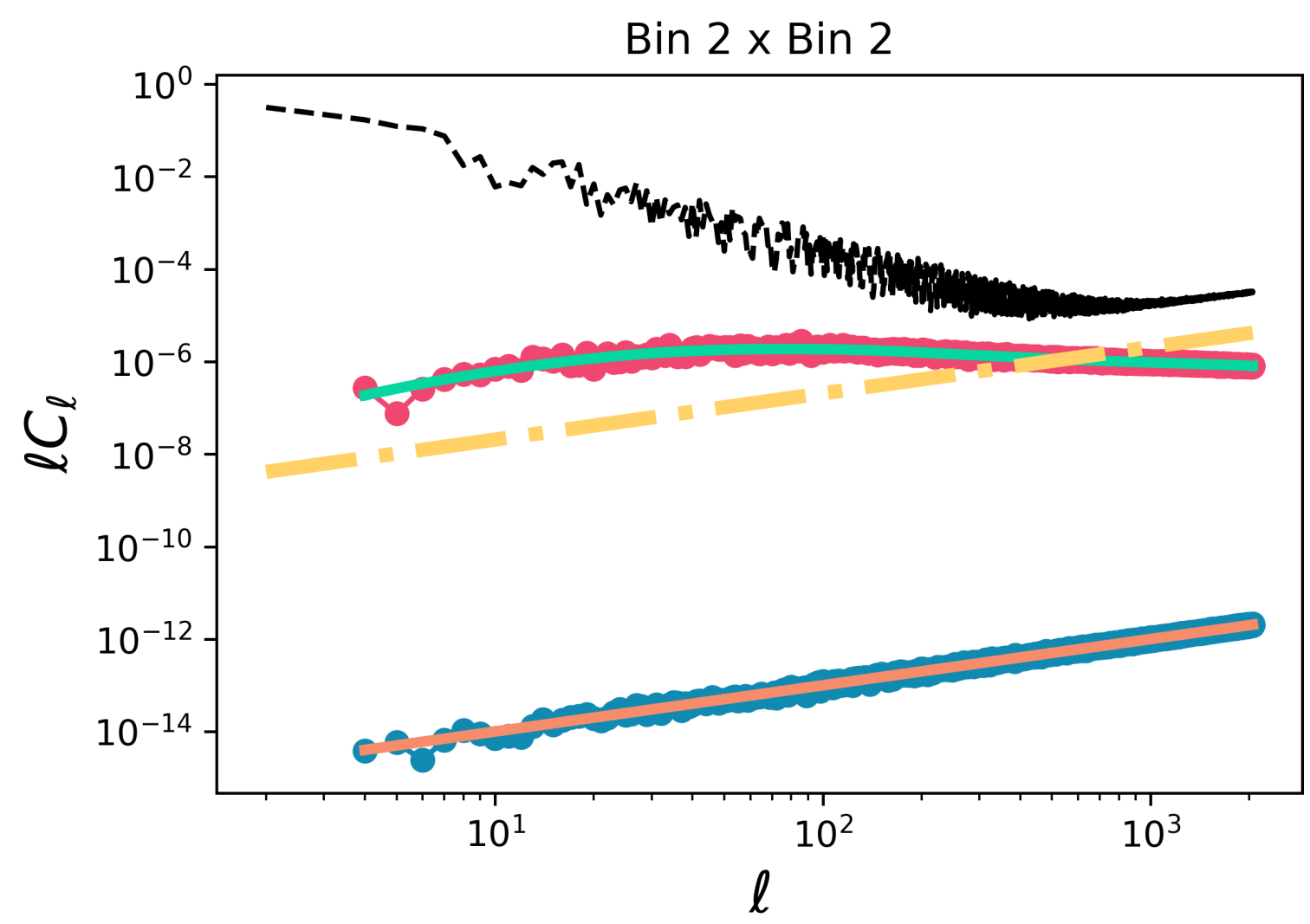
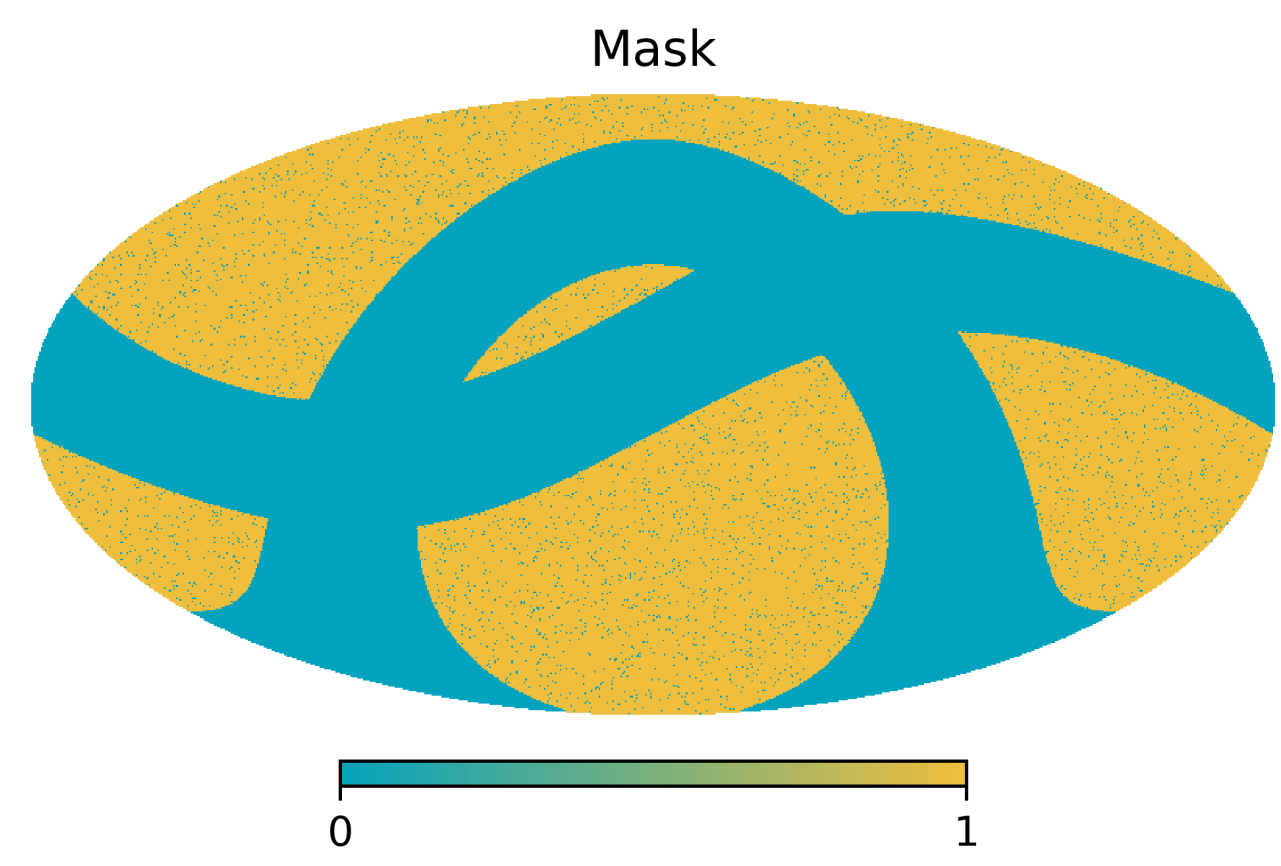
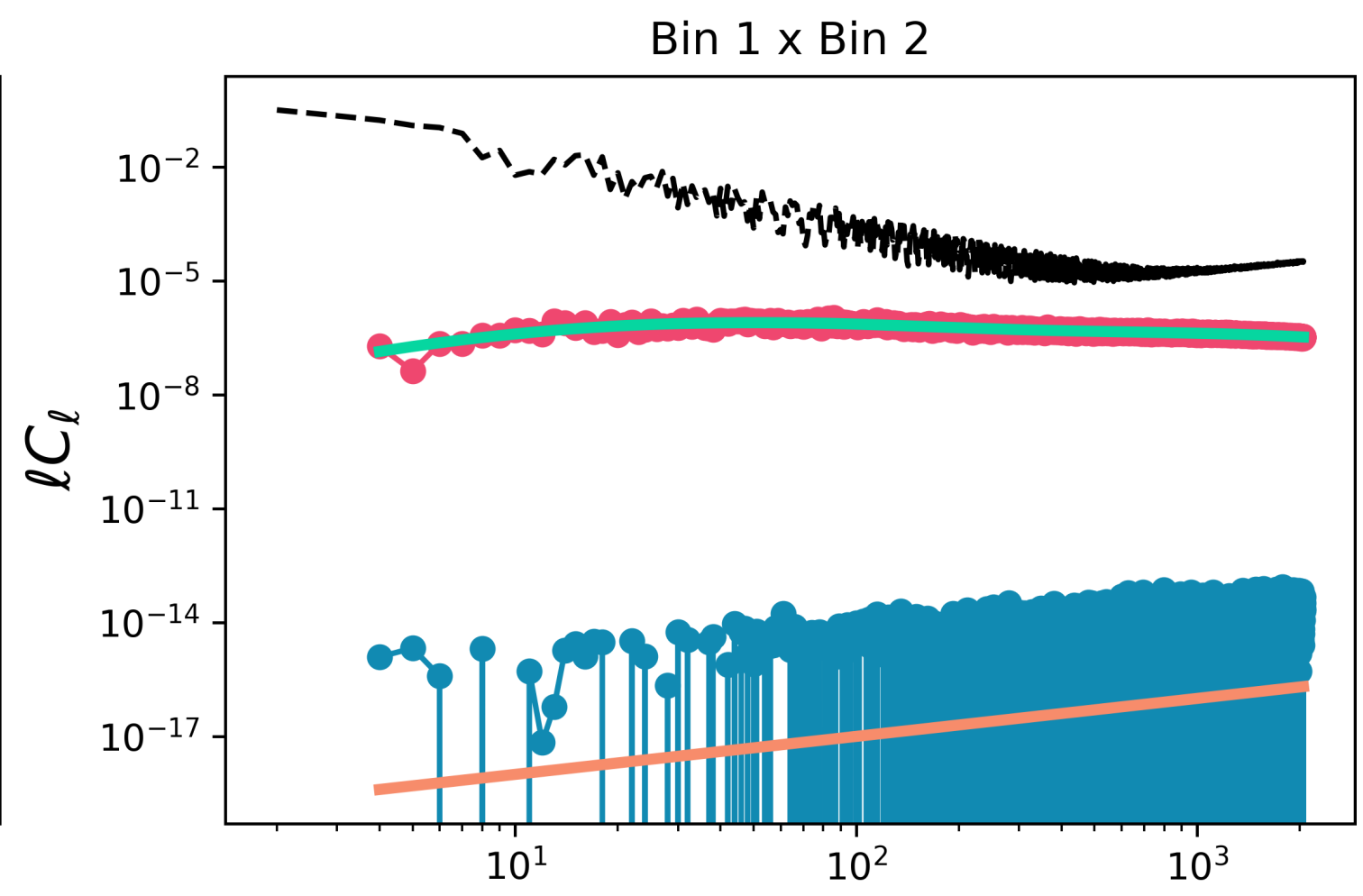
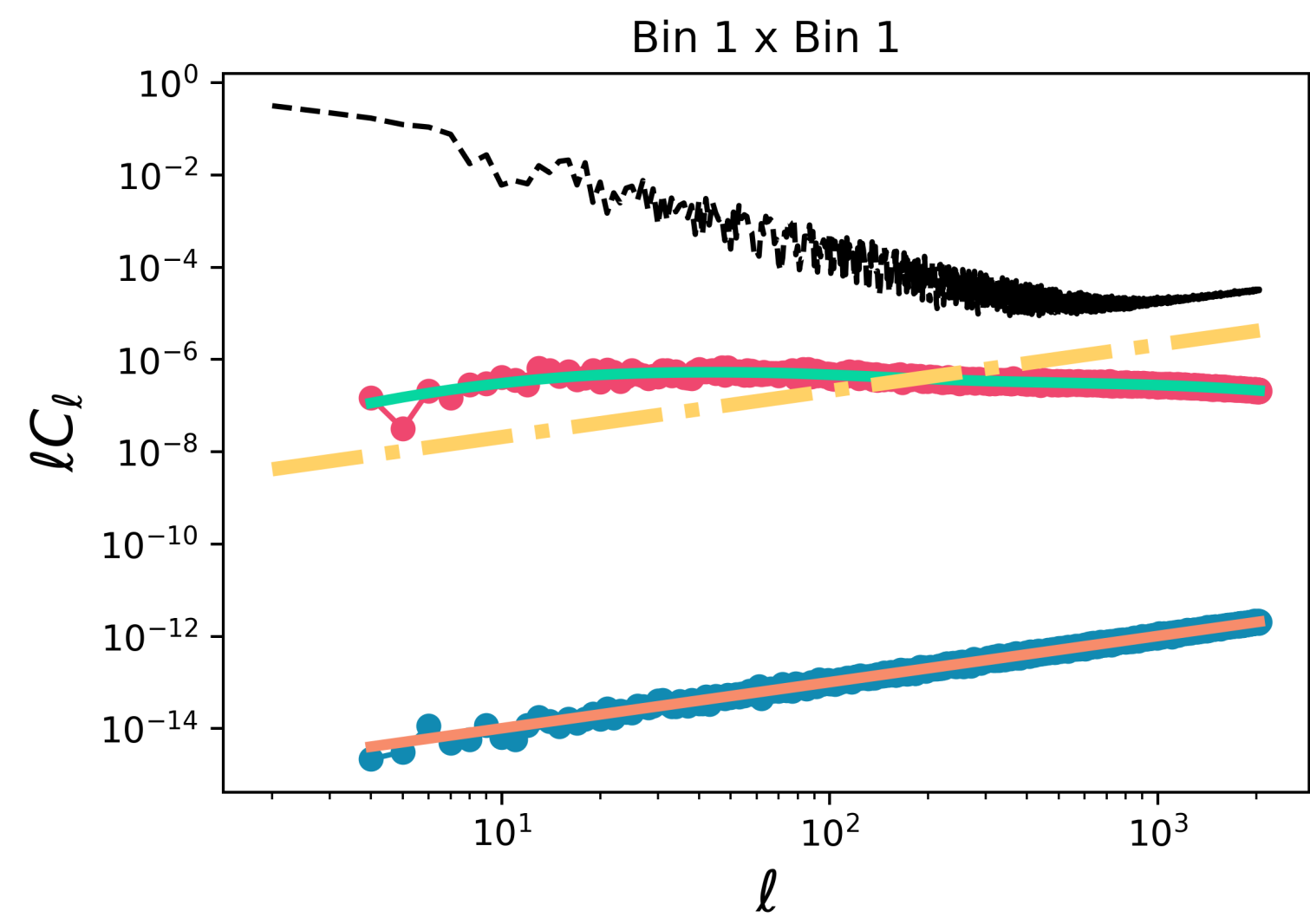
Simulated Euclid-like data



Weak Lensing

Euclid-like case

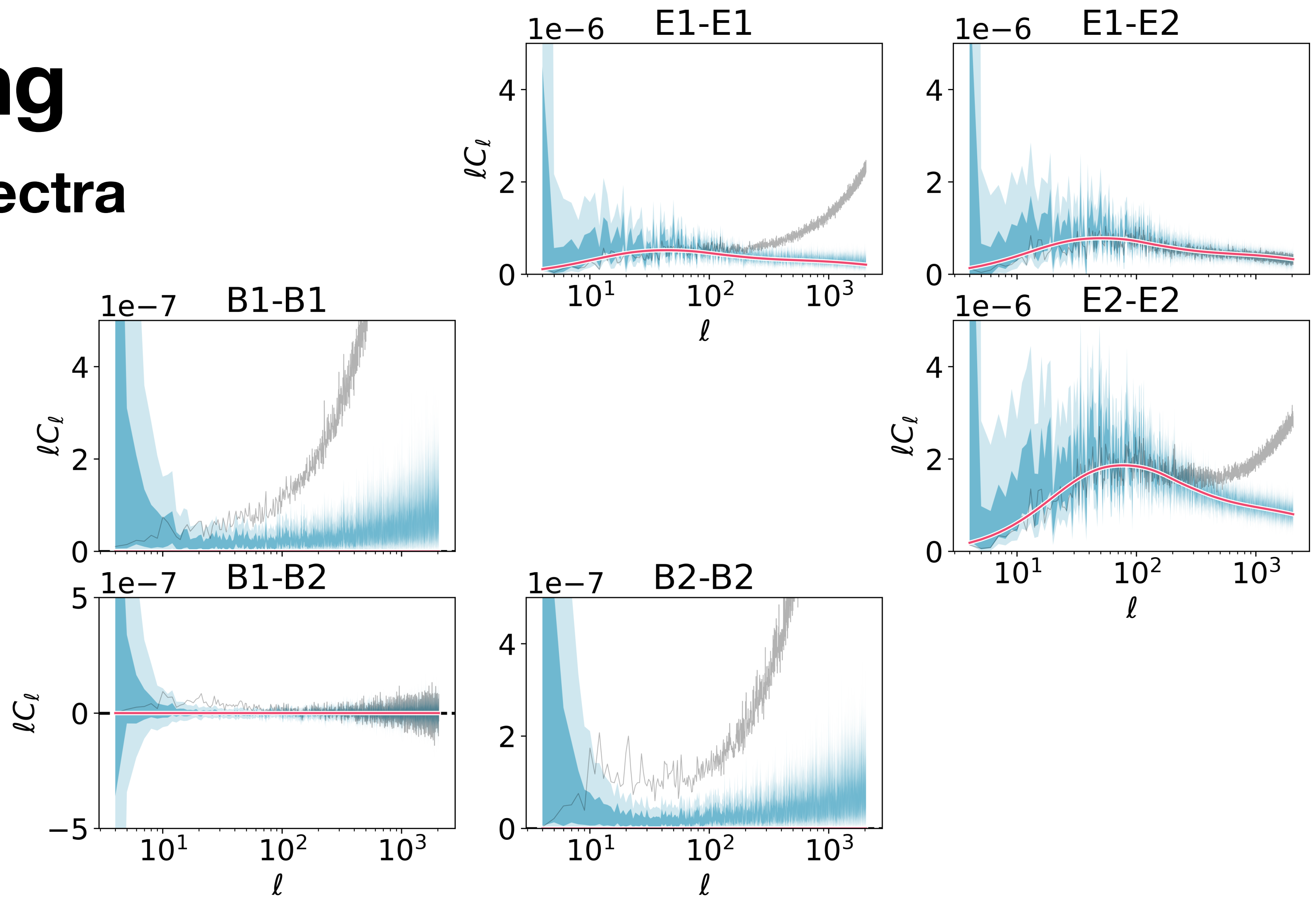
- Two tomographic bins
- Multipoles: 4, 2048
- $N_{\text{side}} = 1024$ (12.5M pixels)
- 16.8 Million free parameters; $\sim 20\text{k}$ are C_ℓ
- Noise:
 - 3 gals/arcmin²/bin
 - $\sigma(e) = 0.28$





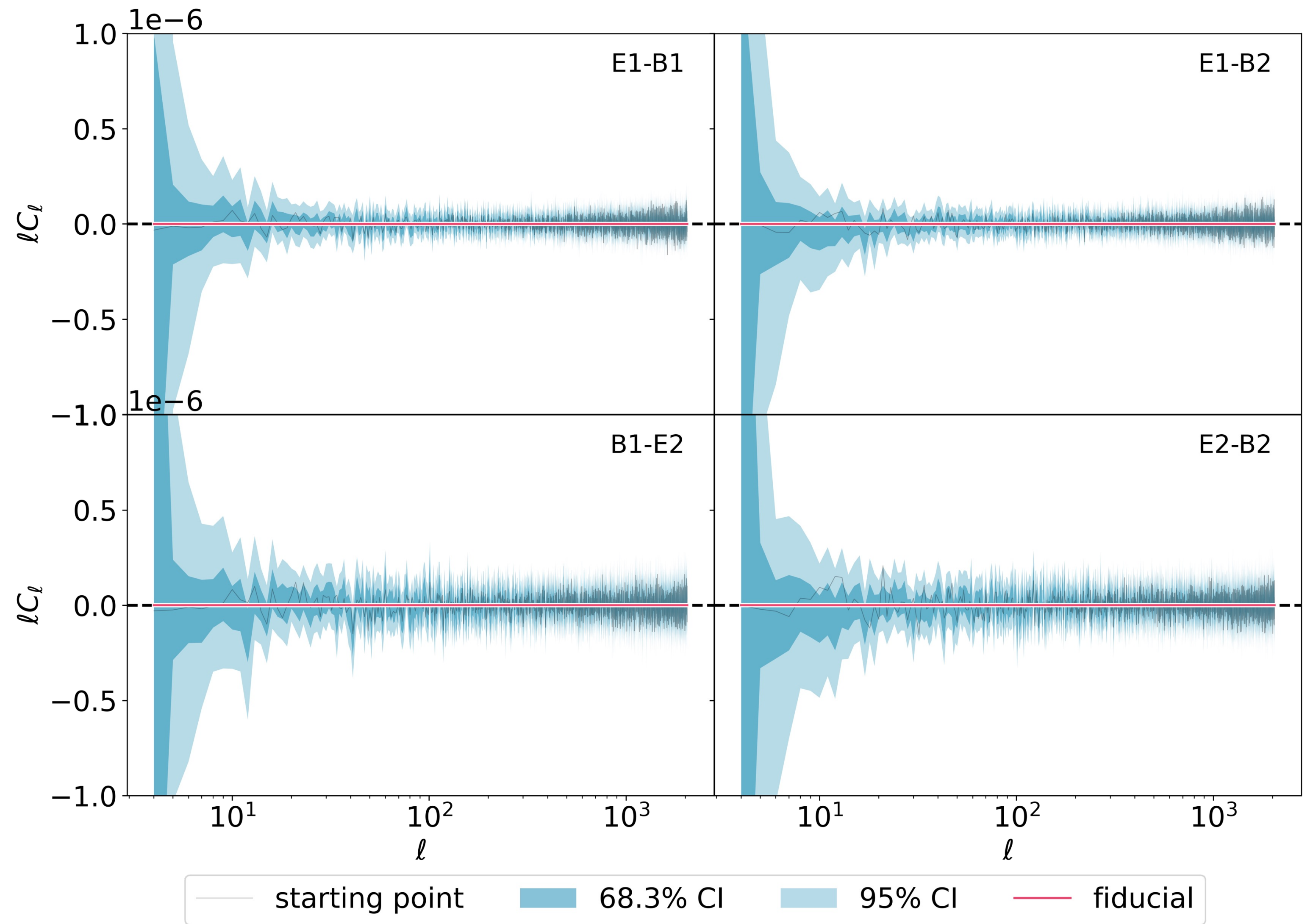
Weak Lensing

Angular Power Spectra





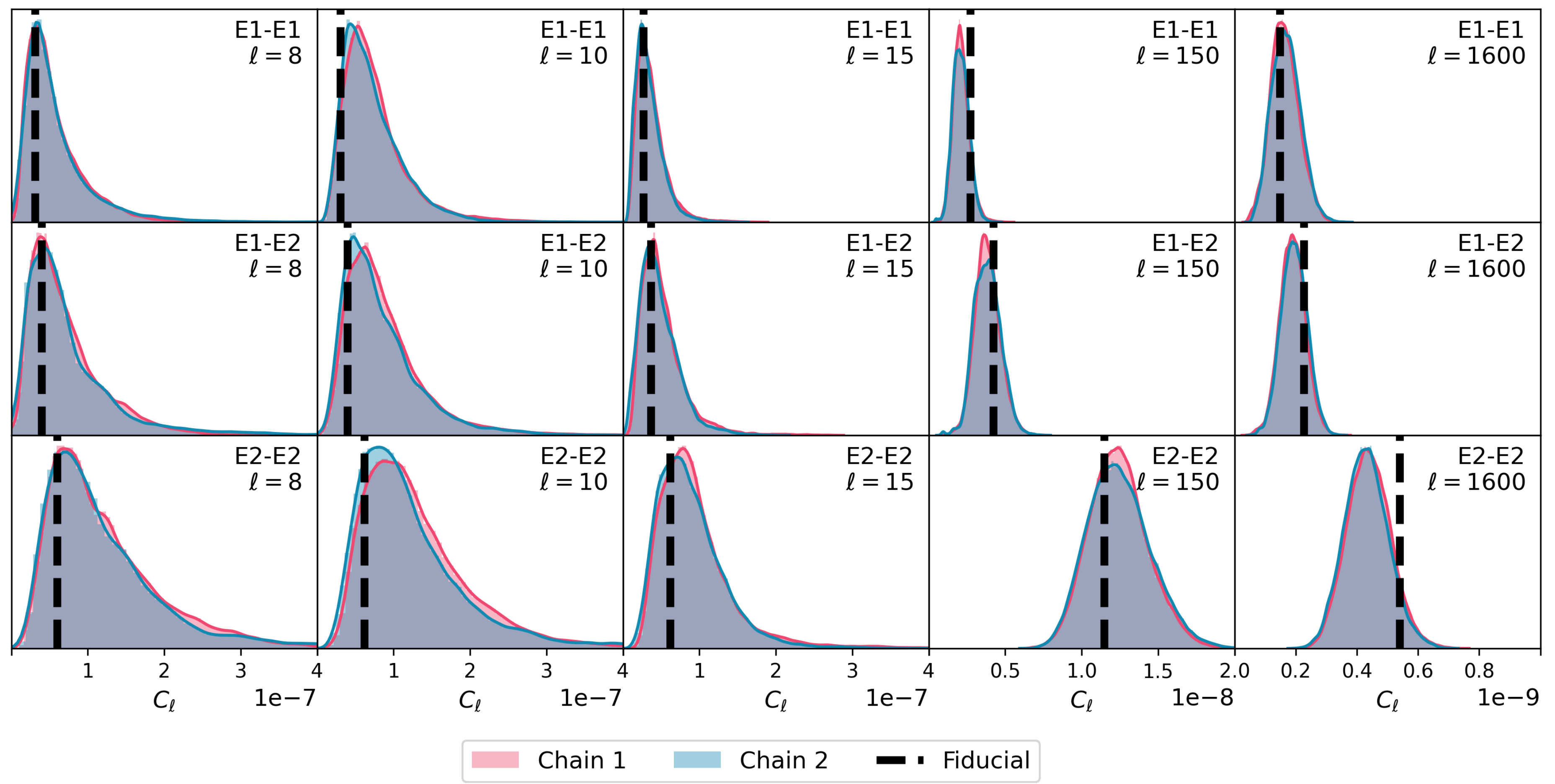
Weak Lensing Angular Power Spectra





Weak Lensing

Angular Power Spectra





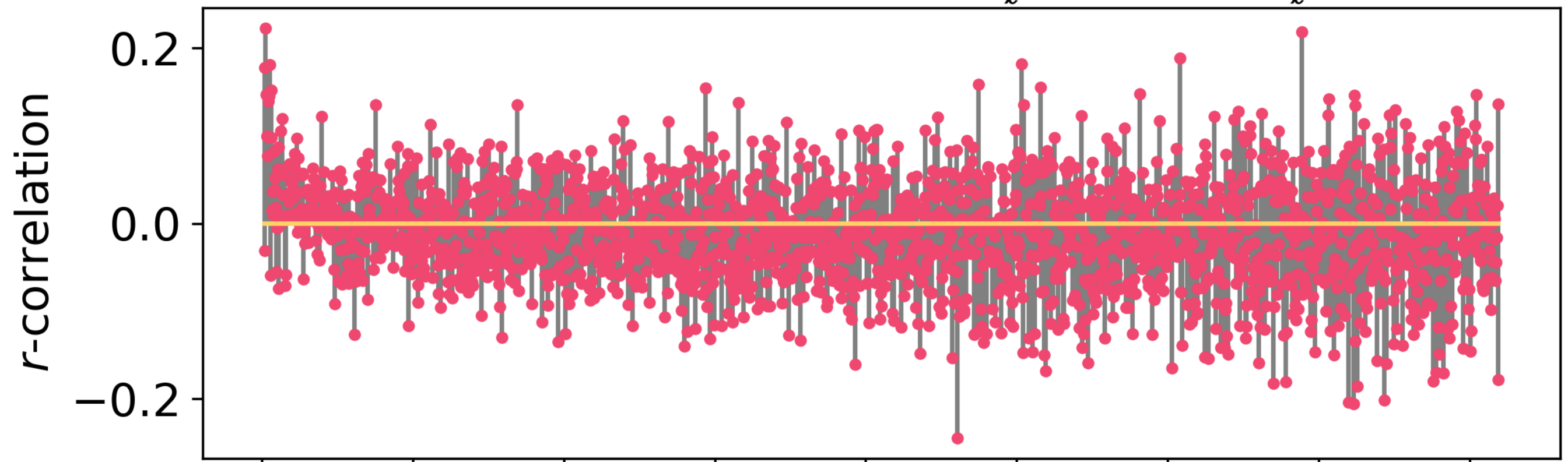
Weak Lensing

E/B Correlations

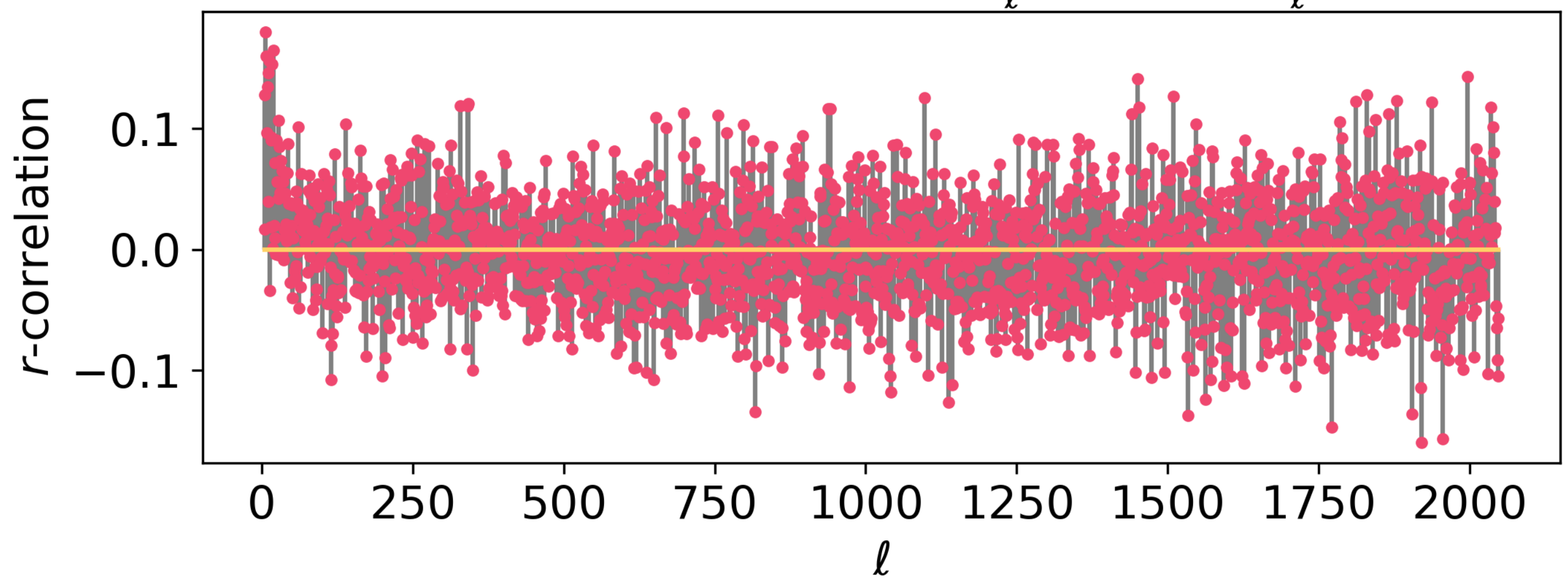
Safe to use the point estimates,
no E/B leak detected!



Correlations between $C_\ell^{E_1, E_1}$ and $C_\ell^{B_1, B_1}$



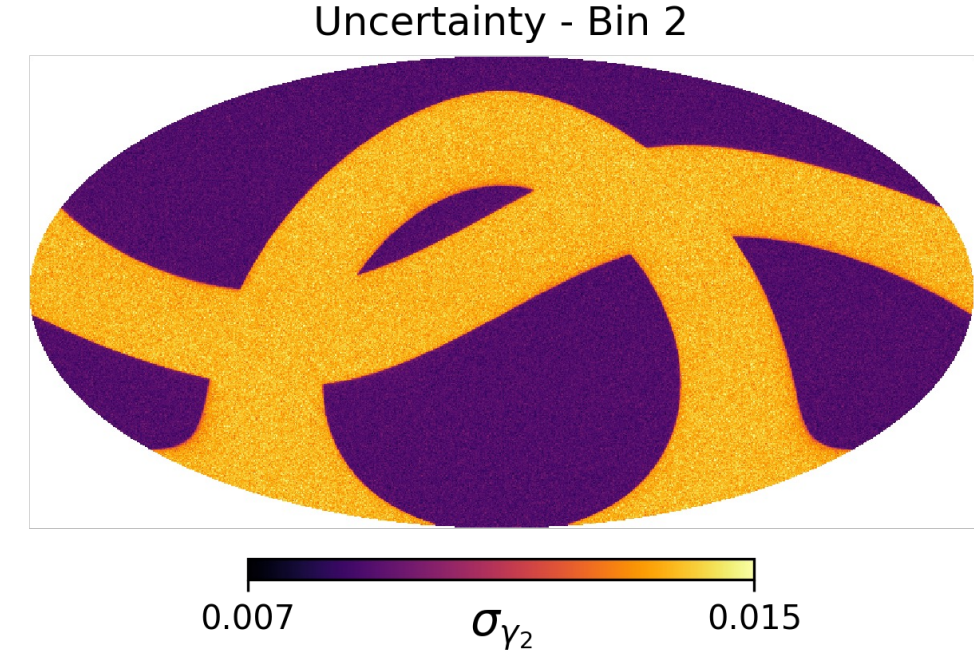
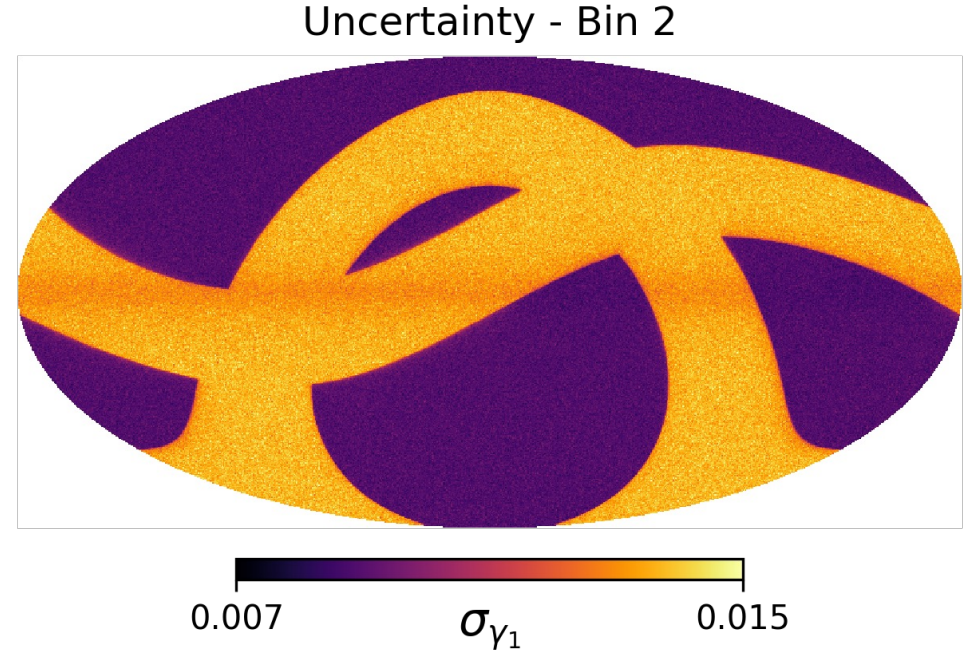
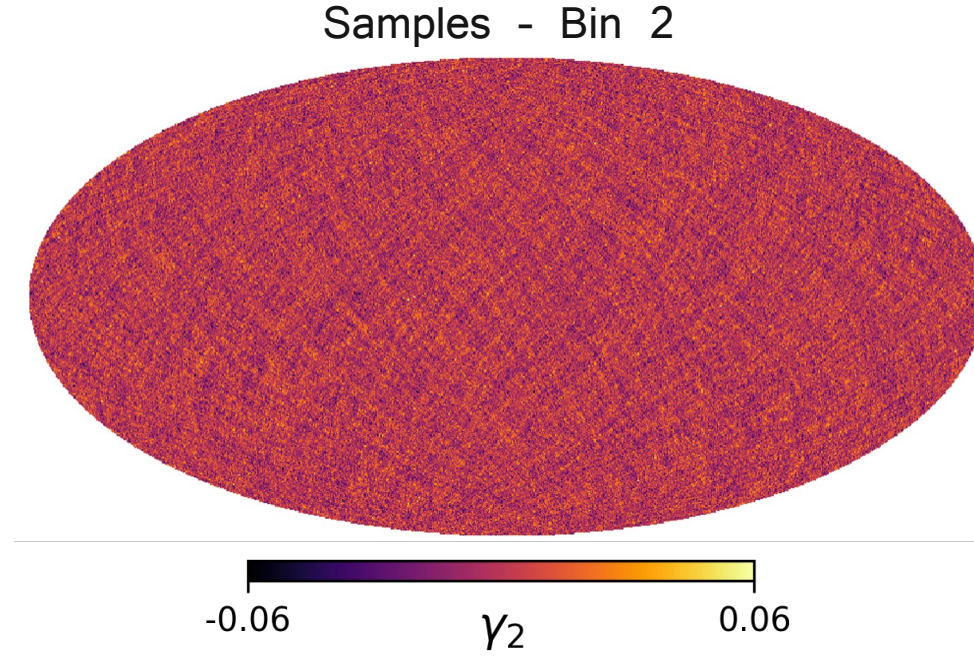
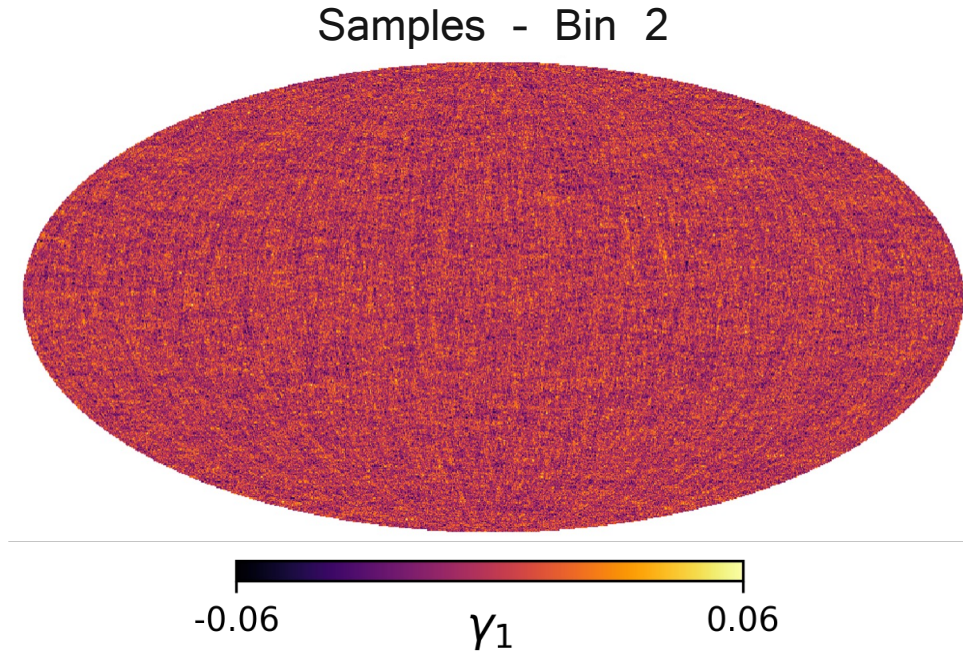
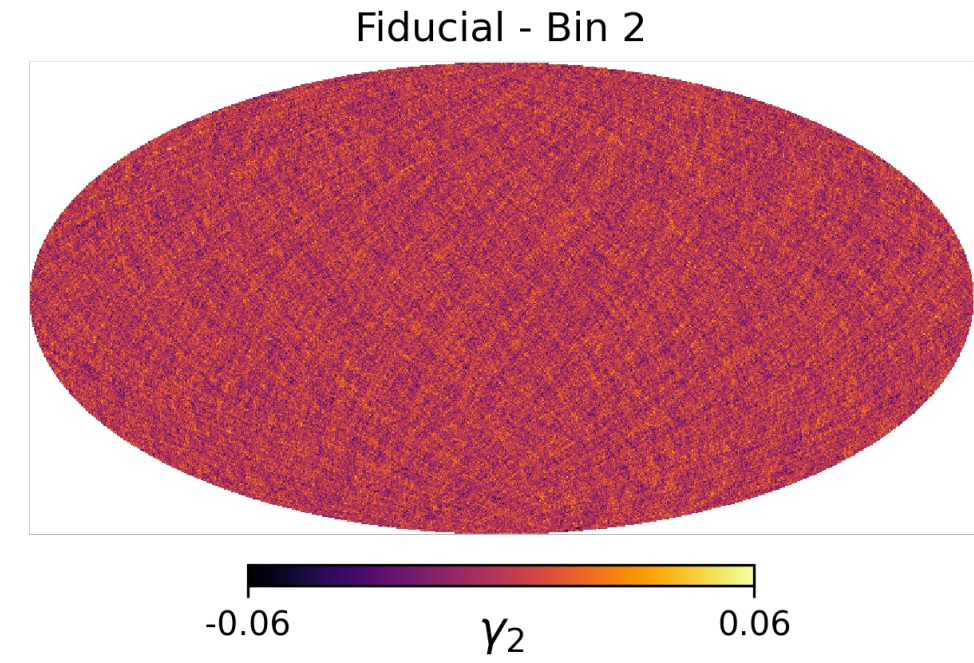
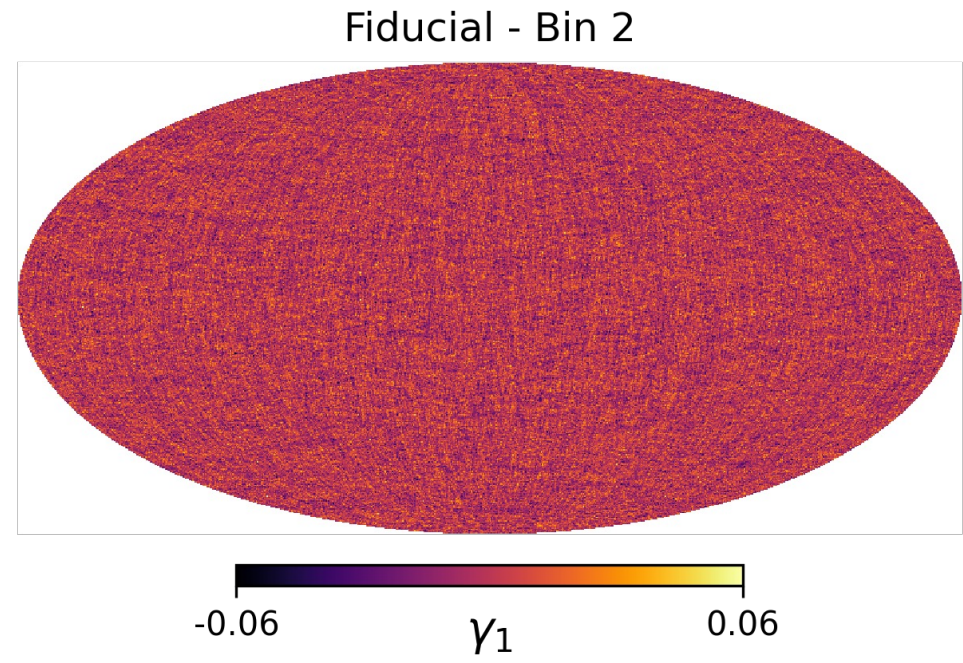
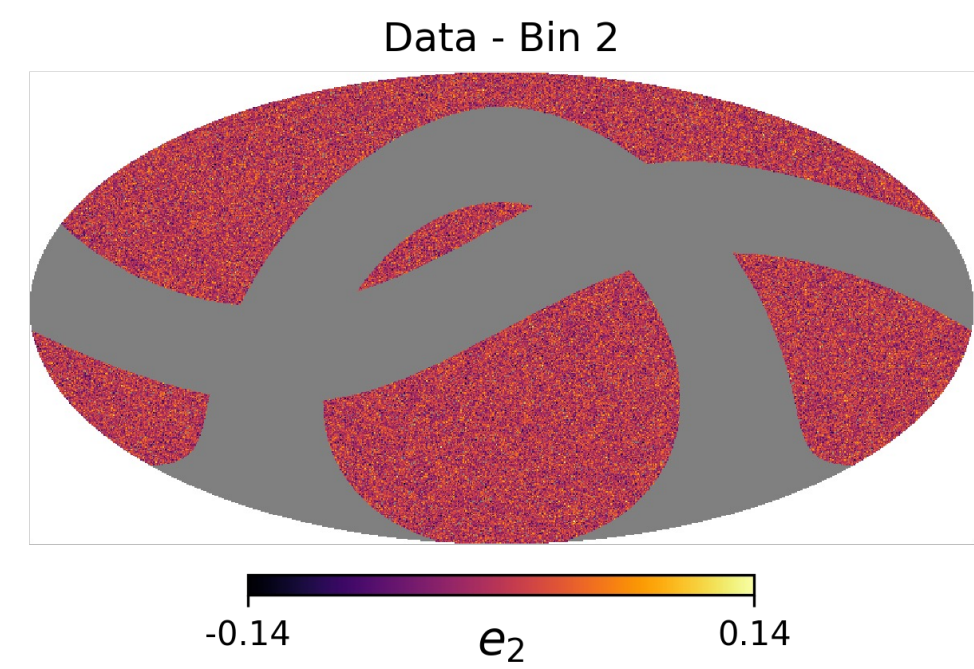
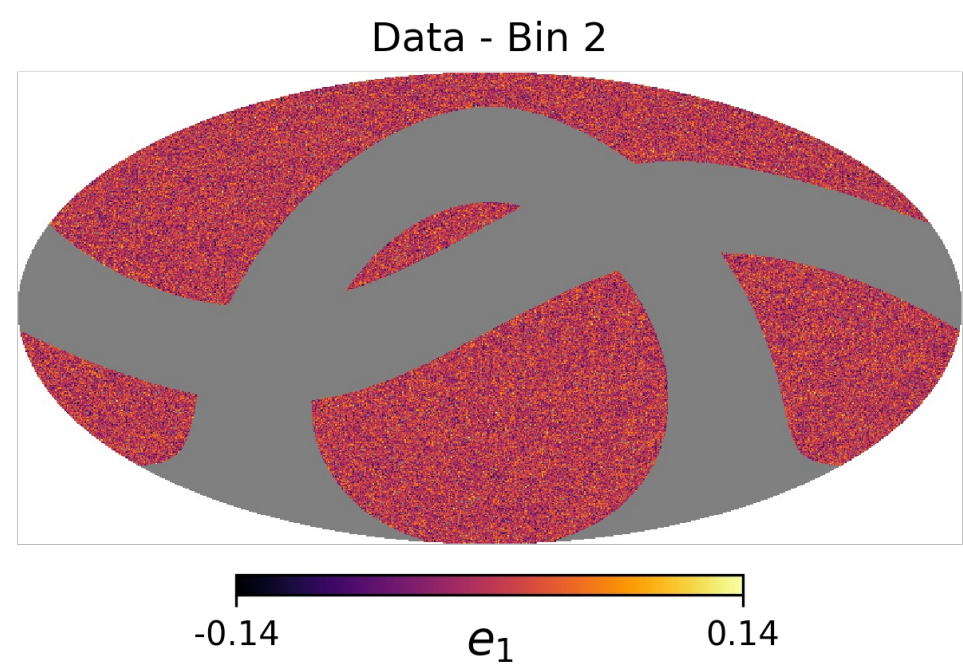
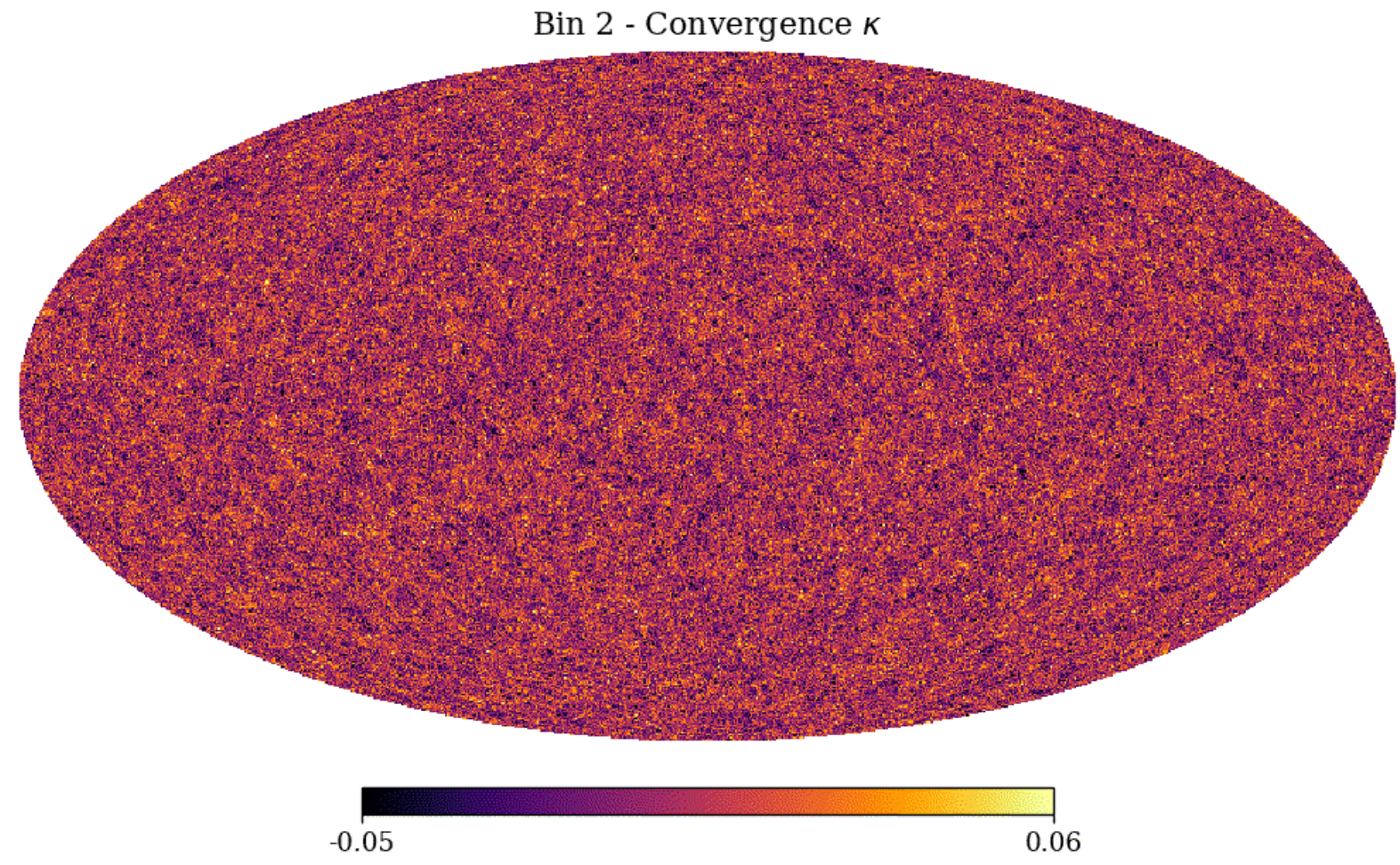
Correlations between $C_\ell^{E_2, E_2}$ and $C_\ell^{B_2, B_2}$





Weak Lensing

Inferred shear maps

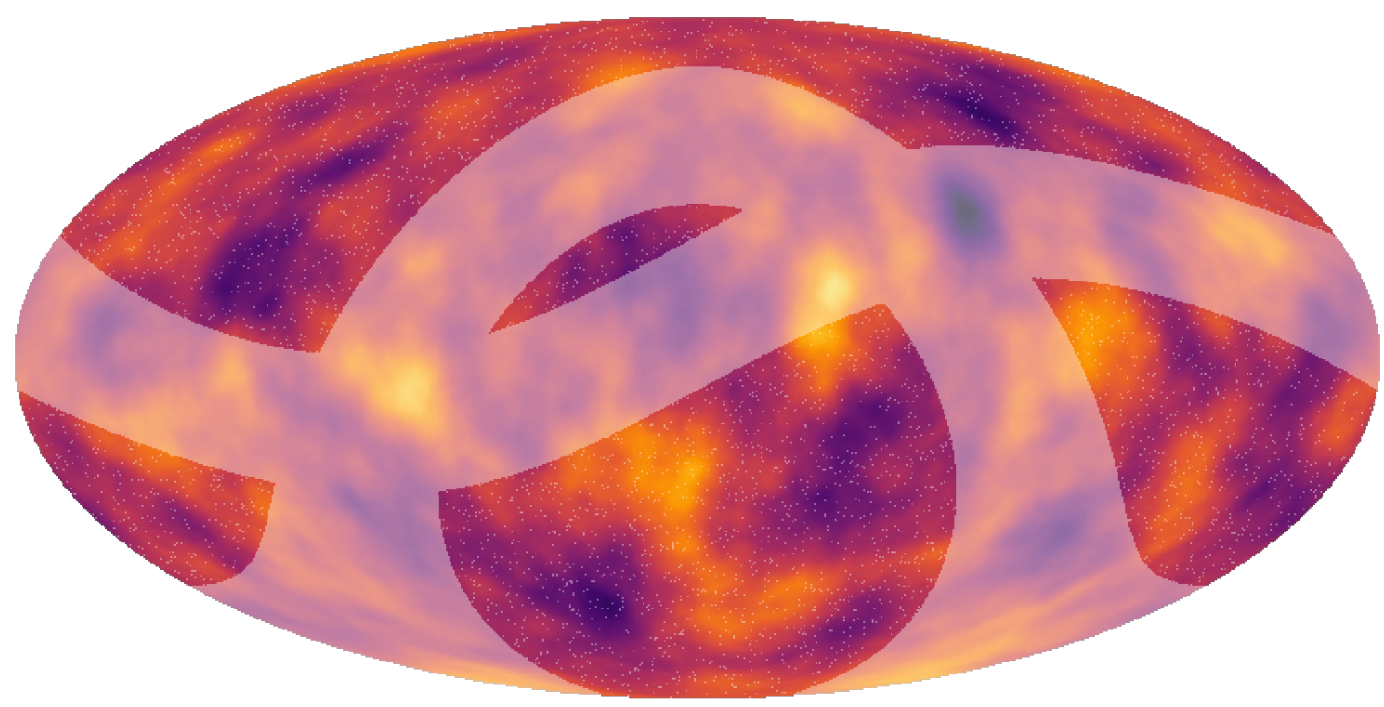




Weak Lensing

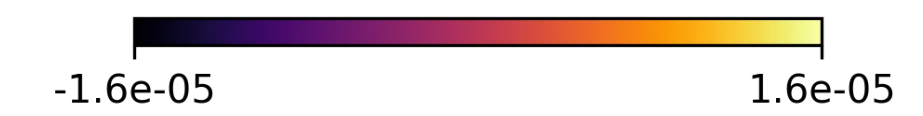
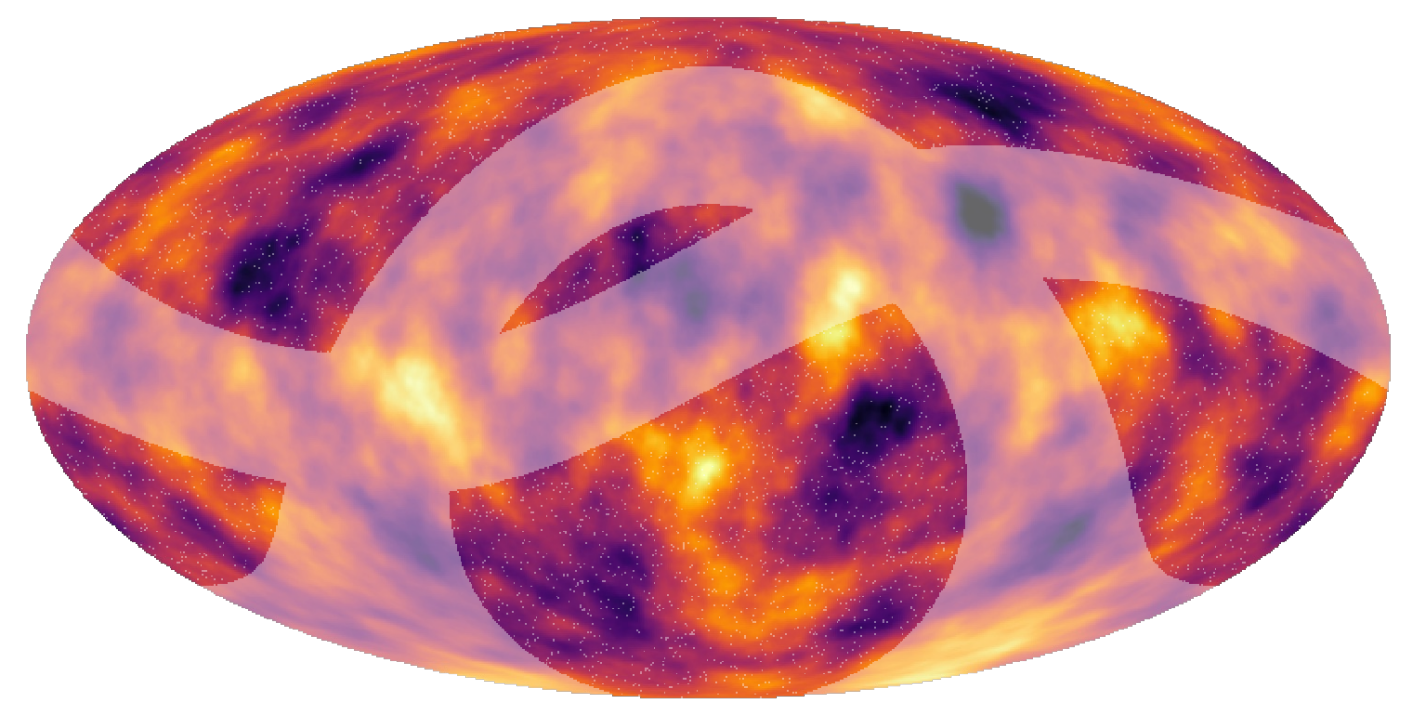
Reconstructed Lensing Potential

Ground Truth - Bin 1



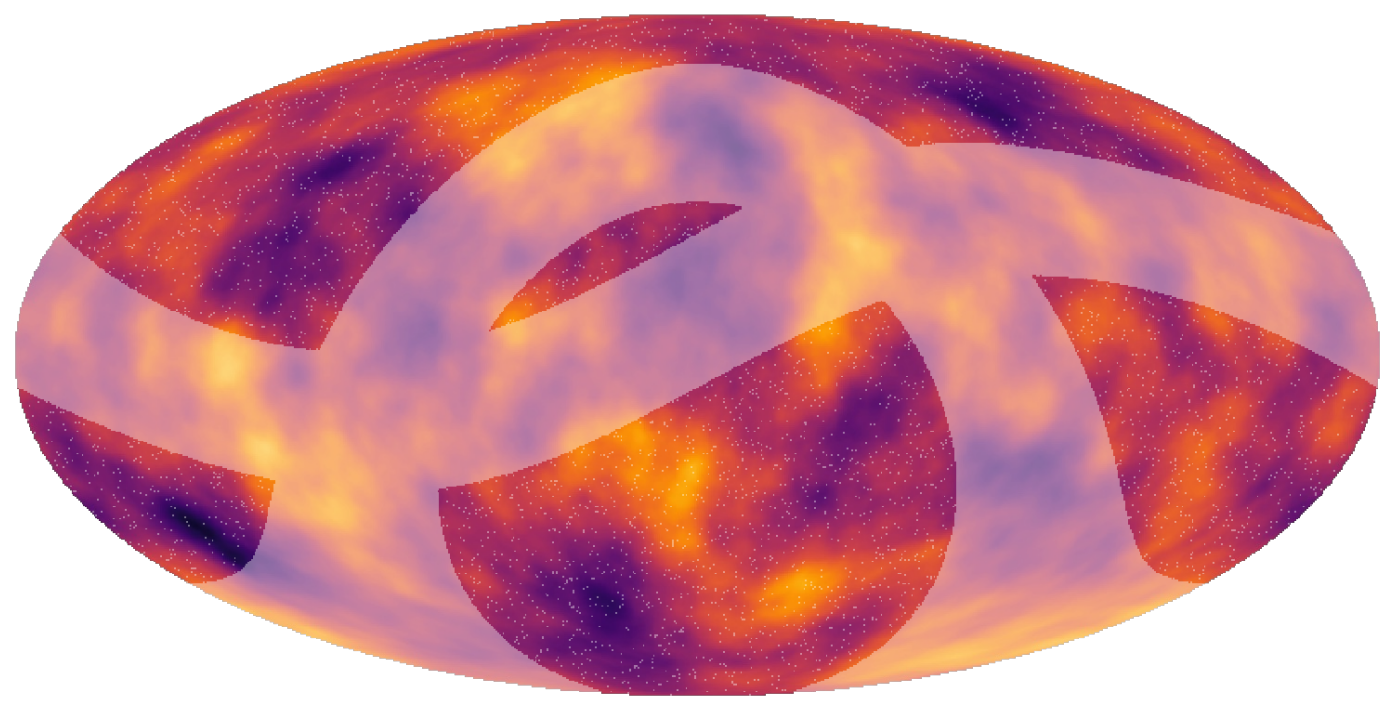
Lensing potential

Ground Truth - Bin 2



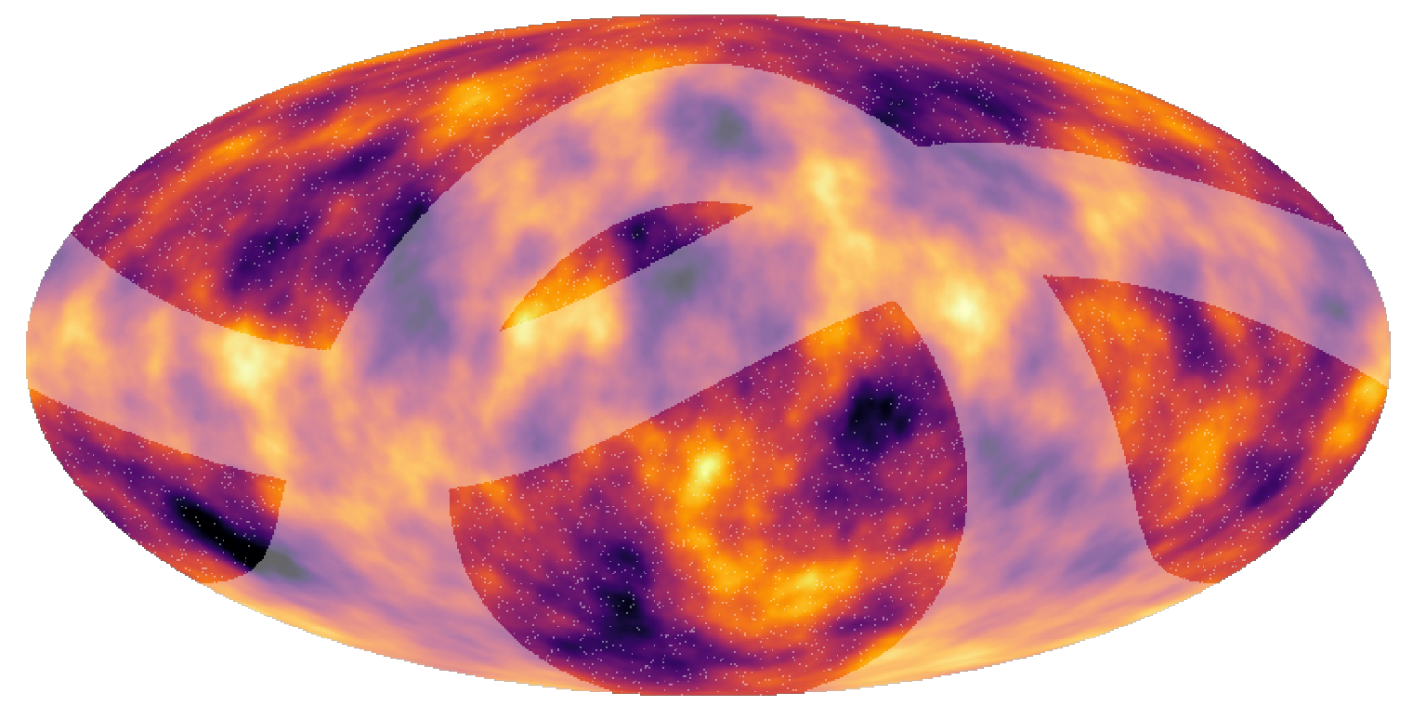
Lensing potential

Typical Sample Map from Almanac - Bin 1



Lensing potential

Typical Sample Map from Almanac - Bin 2



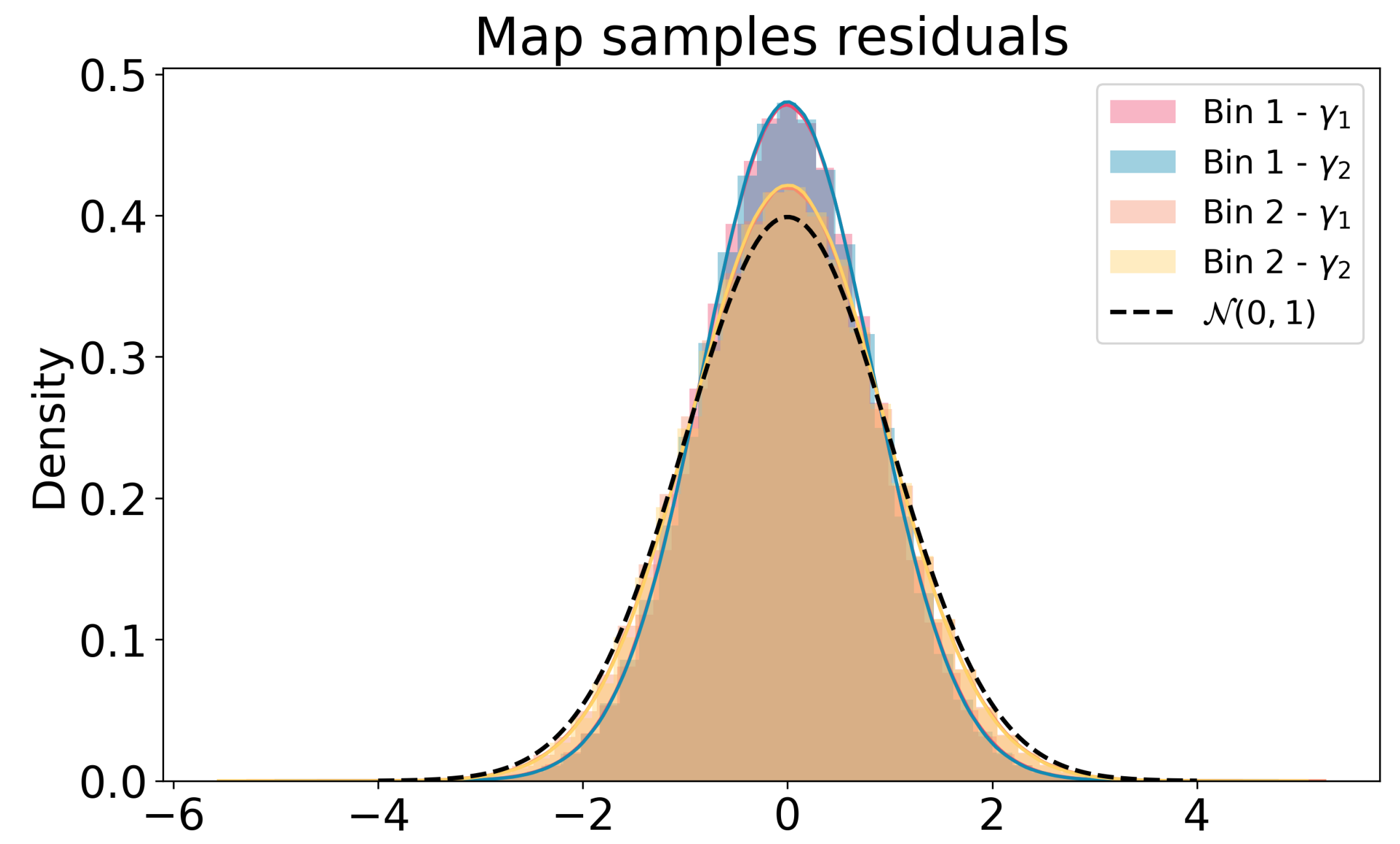
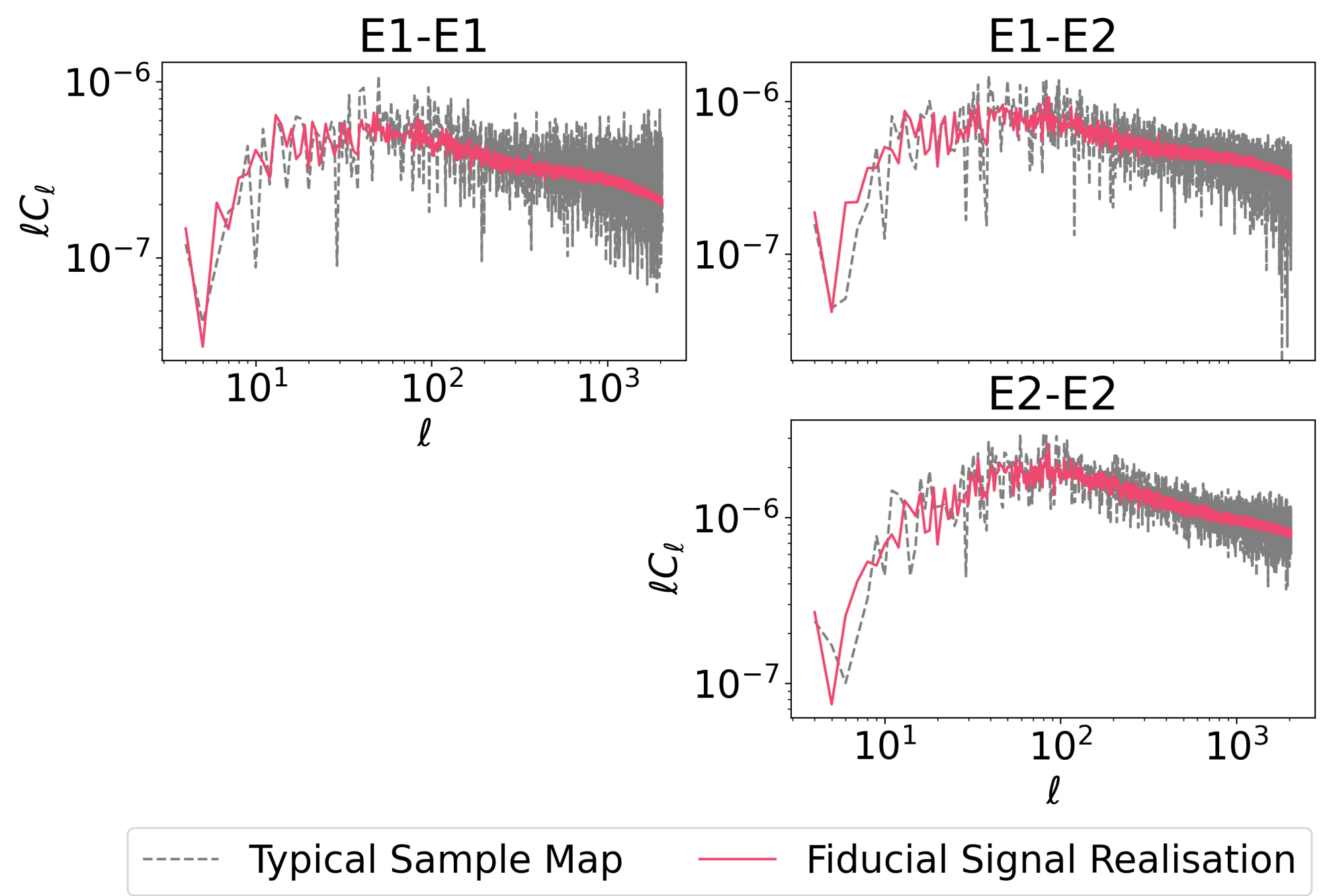
Lensing potential





Weak Lensing

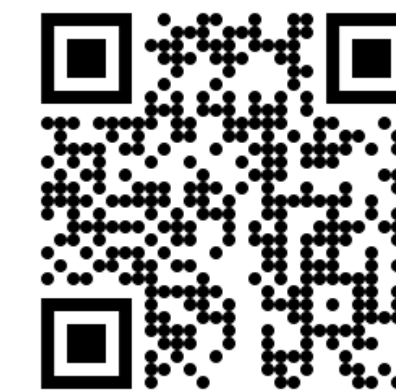
Map consistency check



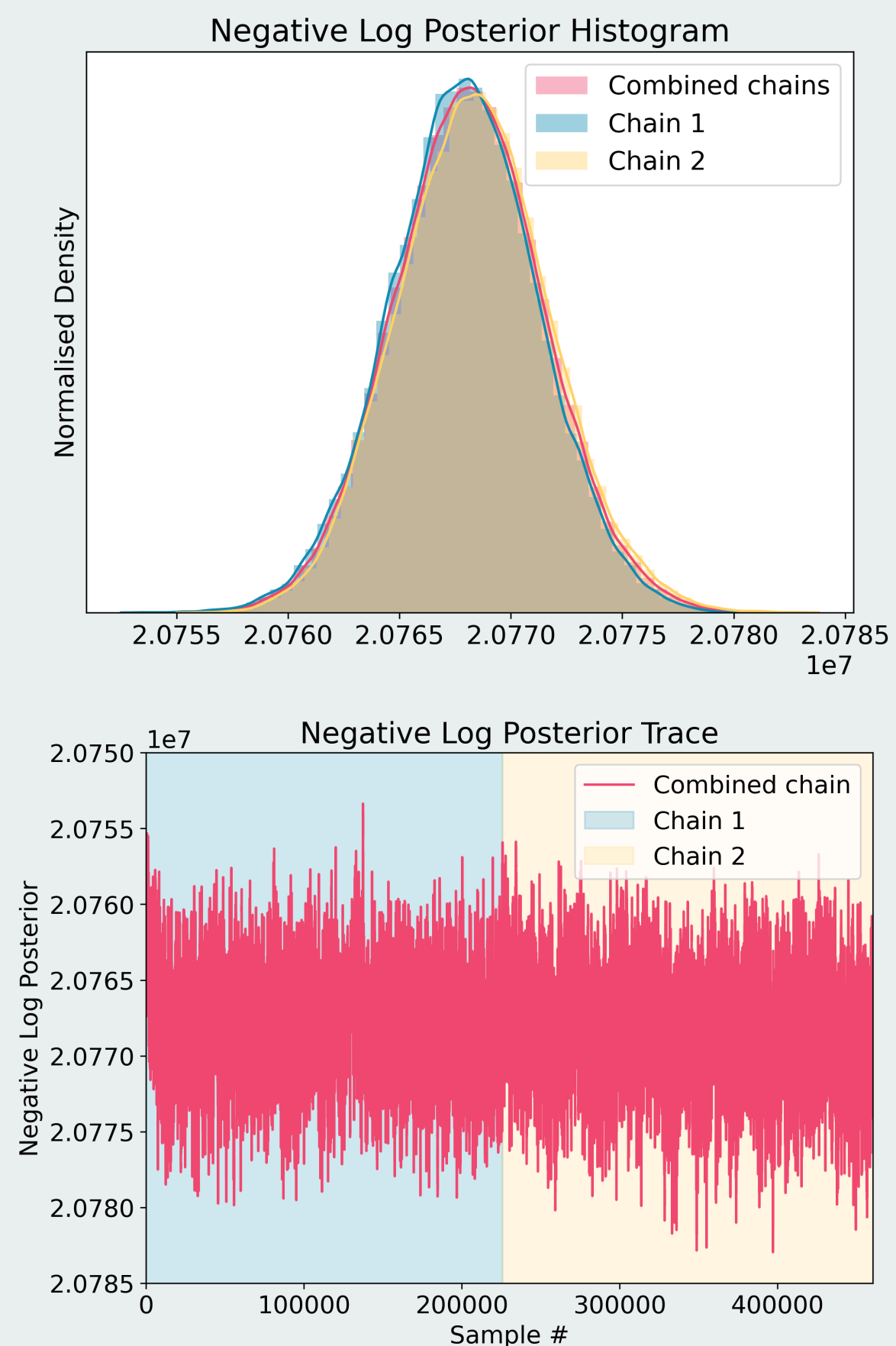
6. Convergence Testing

All diagnostics we carried out...

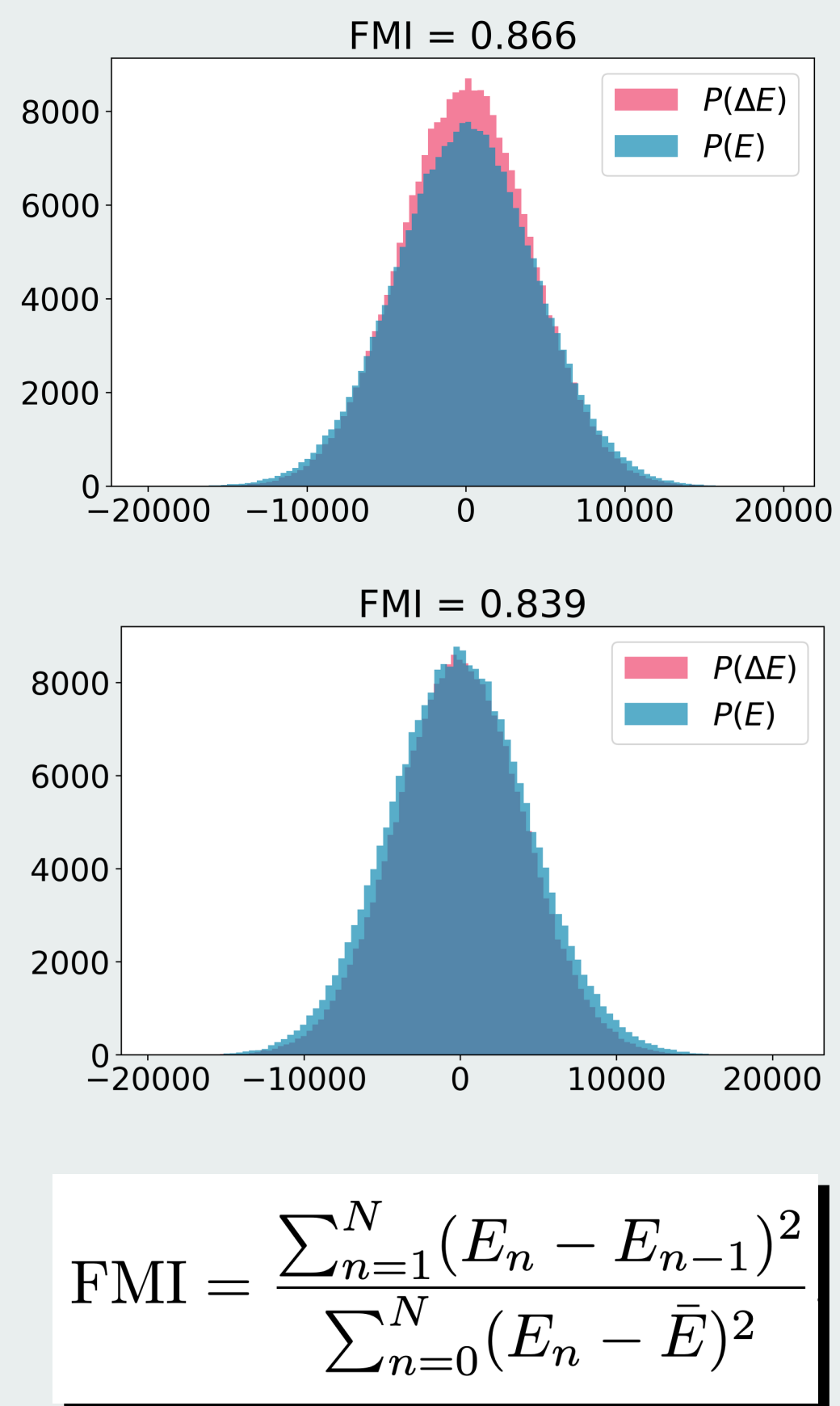
Convergence Diagnostics



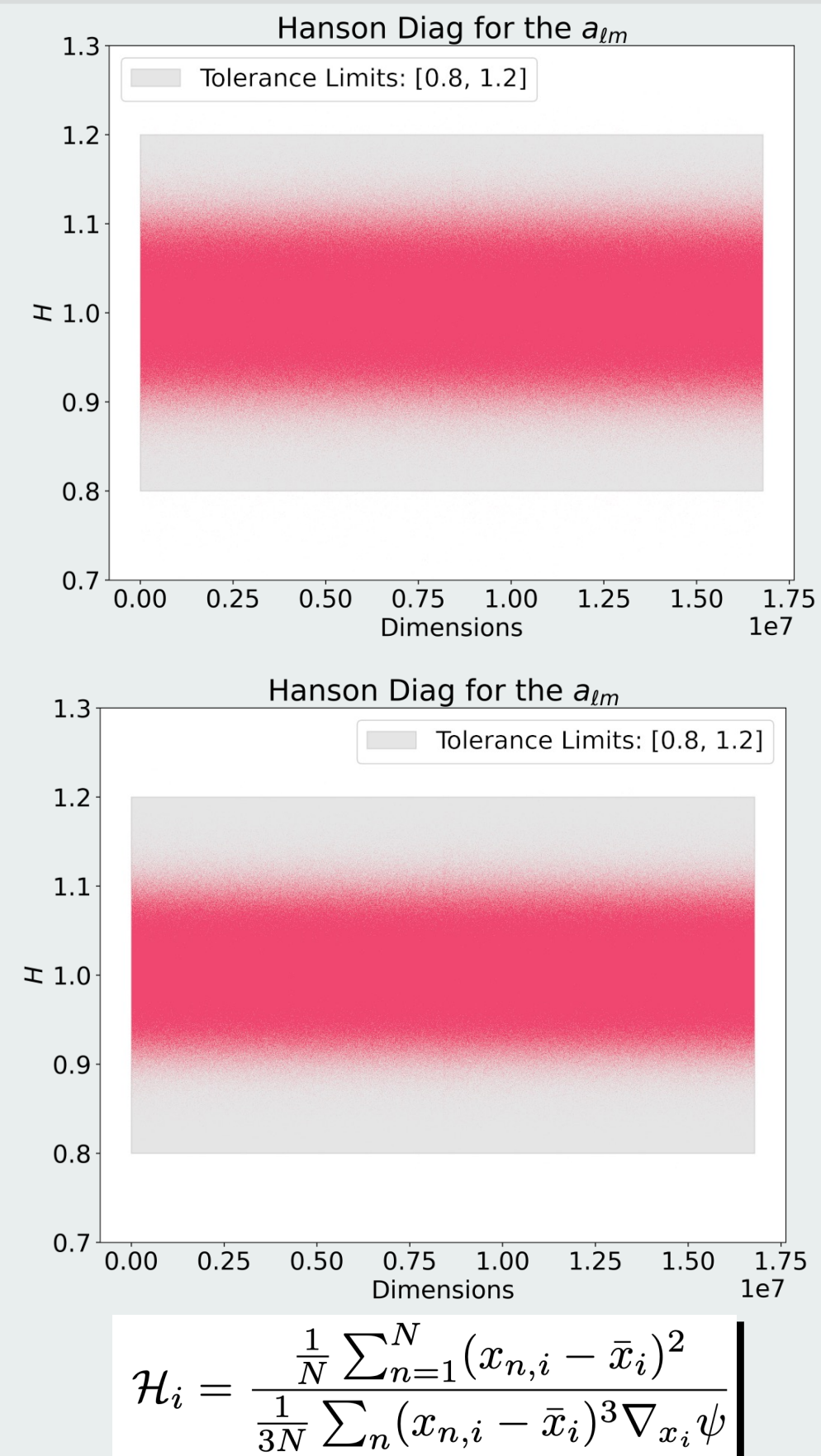
Posterior Trace Analysis



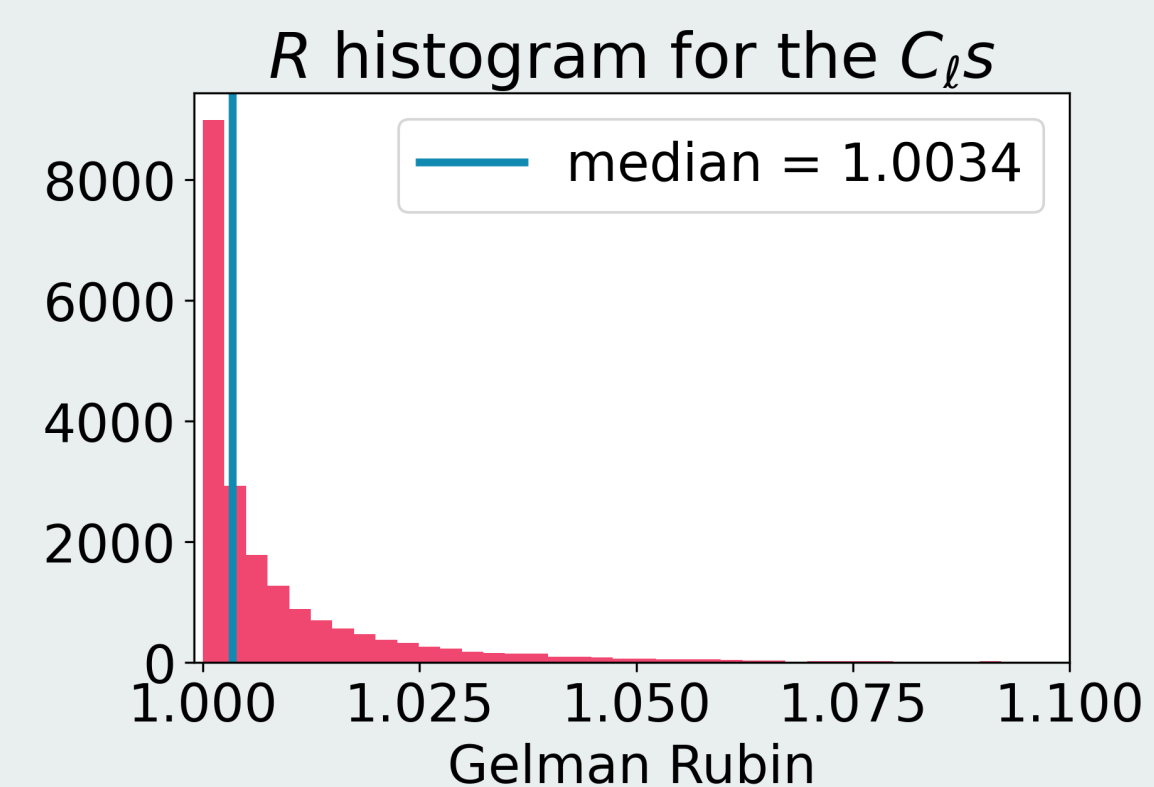
Fraction of Missing Info



Hanson Diagnostics



Gelman Rubin Test

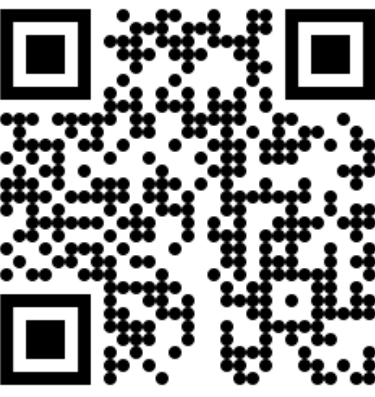


Correlation Length

Chain 1: 3042
Chain 2: 2585
Total samples: 2.25×10^5
Effective sample size: 165

7. Conclusions & Next Steps

What we achieved and where are we going from here?



Summary

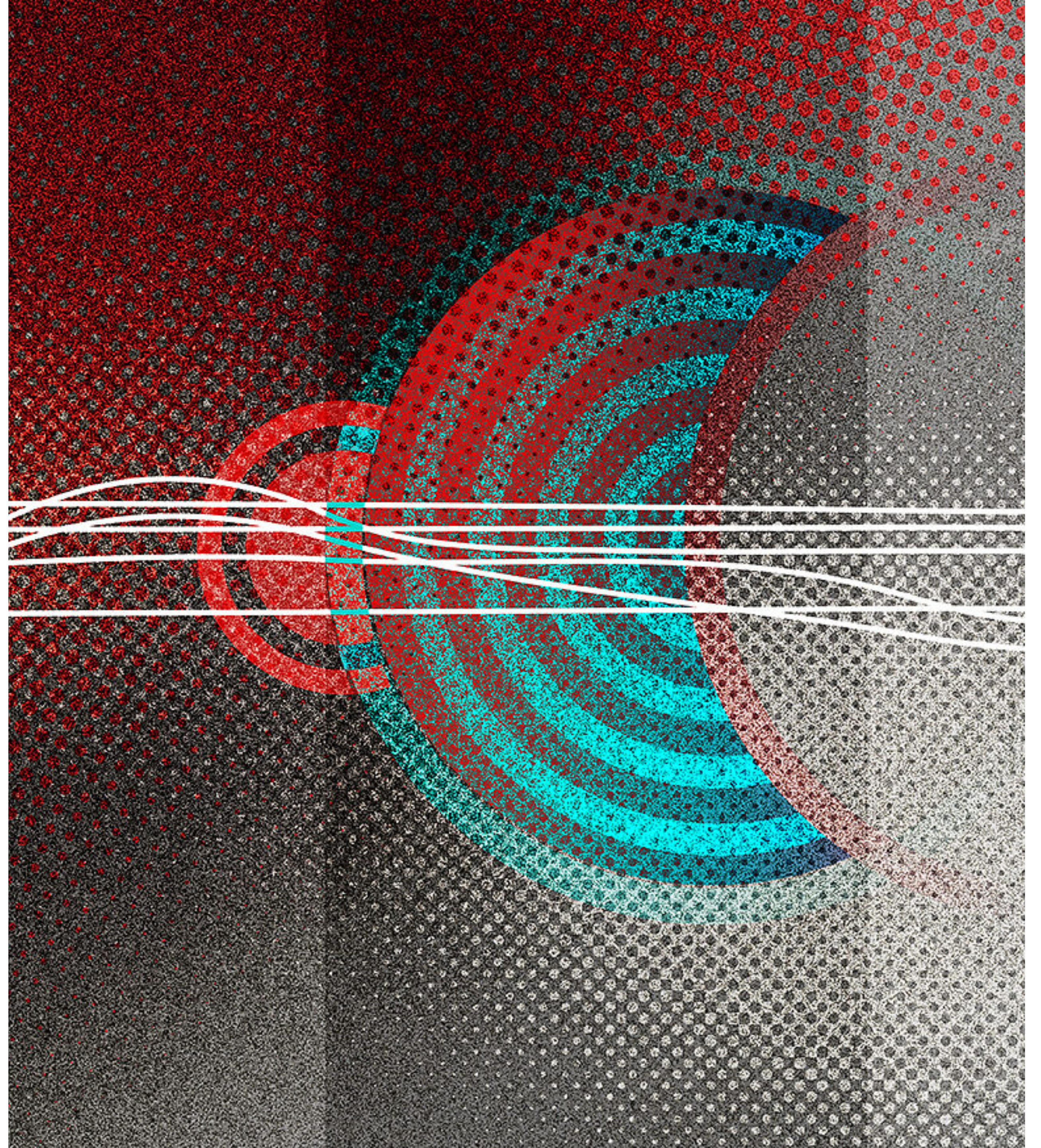
- Next Gen Surveys require Next Gen Cosmological Analysis
- Field Level Inference is an optimal way to extract cosmological information for upcoming cosmological surveys
- Almanac can recover the full sky posterior of high-resolution maps and angular power spectra ($l_{\text{max}} = 2048!$)
- We retain the ability to perform systematic contamination checks: EB “leakage”, B-modes, and more
- We can optimally (by construction) infer the largest scales accessible in Euclid/LSST, including their full marginalised posterior
- We can now also infer (aka have an educated guess) mass maps where surveys will not even observe!

Next:

- **A background paper on our new sampler with applications to CMB simulations is on the way.**
- Applications to Stage III Survey Data
- Cosmological analysis from point estimates (by Javier Lafaure)
- Cosmological analysis using normalising flows
- Primordial non-gaussianities with Weak Lensing Fields

Thanks!

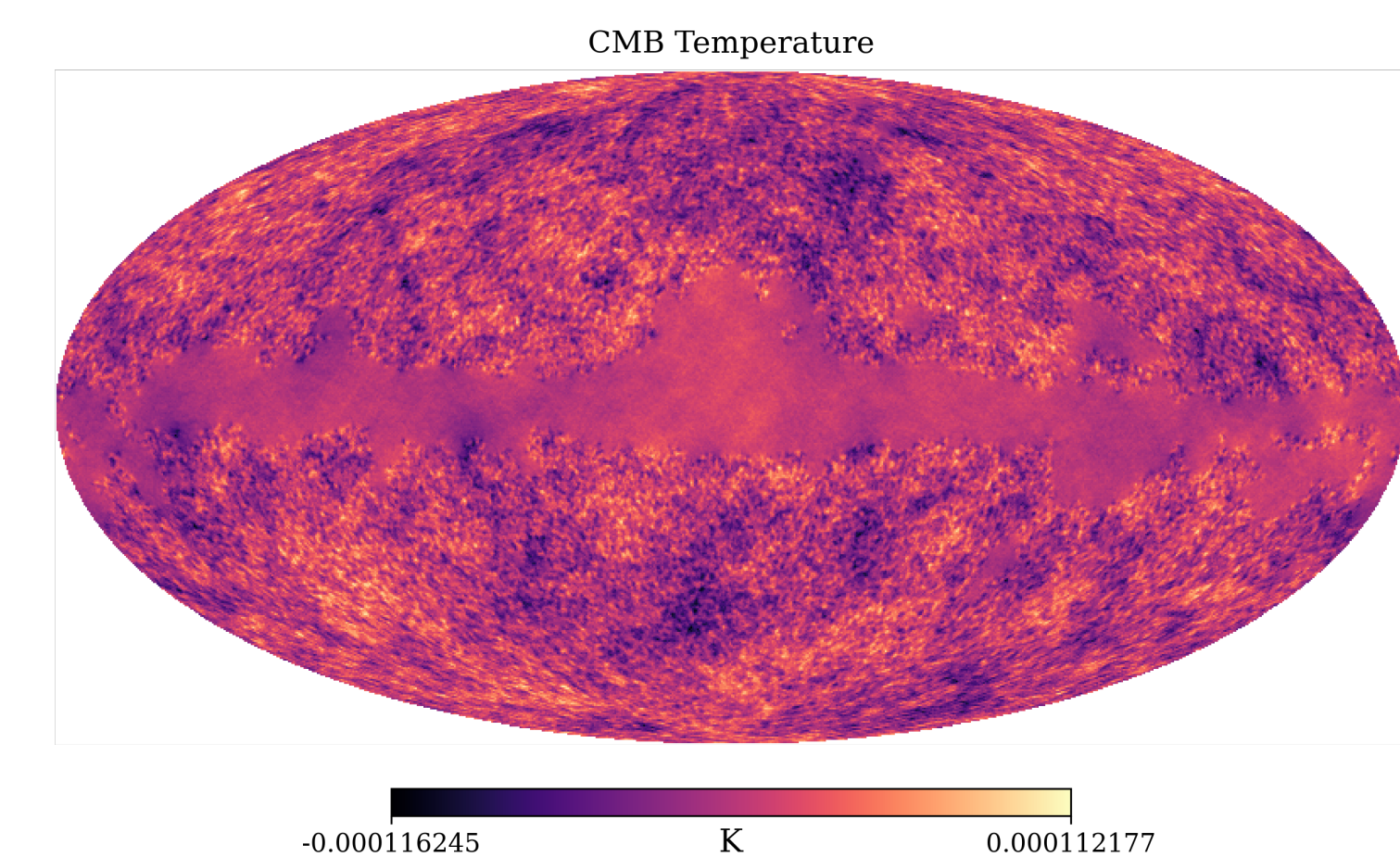
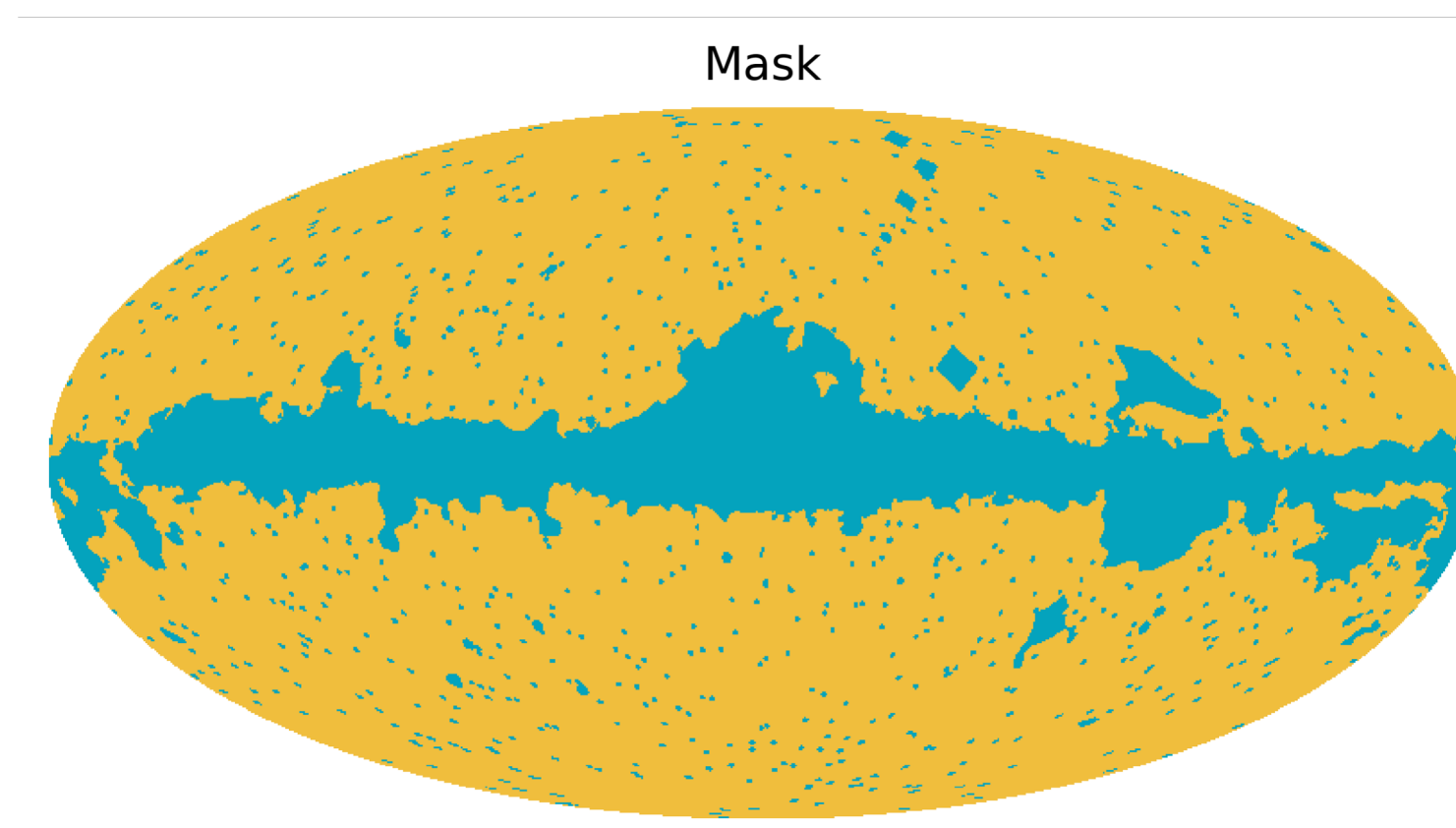
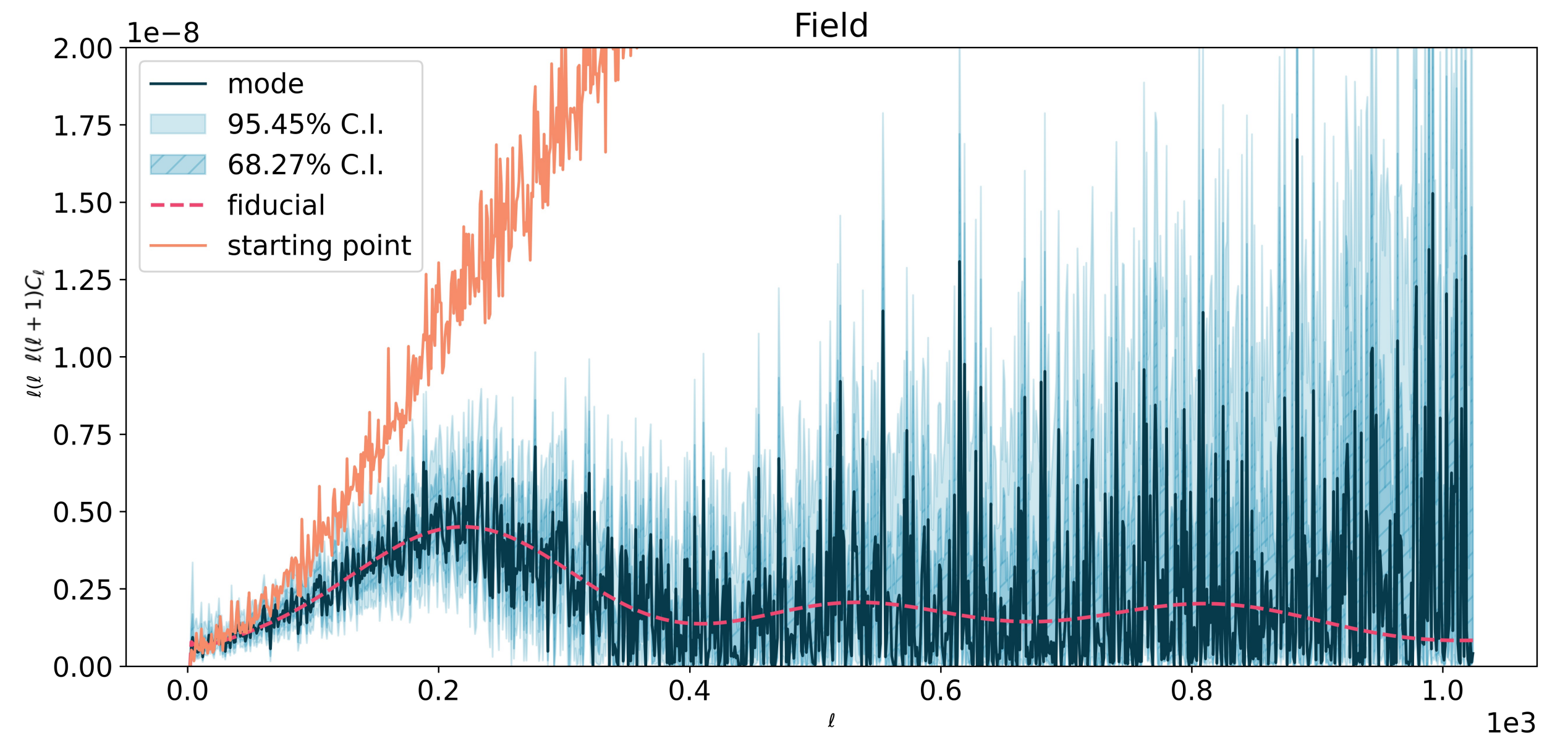
arthur.loureiro@fysik.su.se



CMB Temperature

Low Signal-to-noise case

- Temperature-only
- Single channel simulation
- Multipole range: 2, 1024
- Nside: 512 (3.14M pixels)
- Noise level: $1e-6$ K/pixel
- WMAP-Like Mask



Mean Map from the samples

CMB Polarisation

Mid Signal-to-noise

- Polarisation only, no EB-cross
- Single channel simulation
- Multipole range: 2, 1024
- Nside: 512 (3.14M pixels)
- Noise level: $2e-6$ K / pixel
- WMAP-Like Mask

