

Cosmic Shear Cosmology Beyond 2-Point Statistics: A Combined Peak Count and Correlation Function Analysis of DES-Y1

Joachim Harnois-Déraps^{1,2*}, Nicolas Martinet³, Tiago Castro^{4,5,6,7}, Klaus Dolag^{8,9}, Benjamin Giblin², Catherine Heymans^{2,10}, Hendrik Hildebrandt¹⁰ & Qianli Xia²

<https://arxiv.org/abs/2012.02777>

Many slides are a courtesy Nicolas Martinet

Why go beyond?

With 2PCF, the Density field is summarized as:

$$\langle \delta(\mathbf{k})\delta(\mathbf{k}') \rangle = (2\pi)^3 \delta_D(\mathbf{k} - \mathbf{k}') P(\mathbf{k})$$

$$\delta(\mathbf{x}) = \sum \tilde{\delta}(\mathbf{k}) \exp(i\mathbf{k} \cdot \mathbf{x}).$$

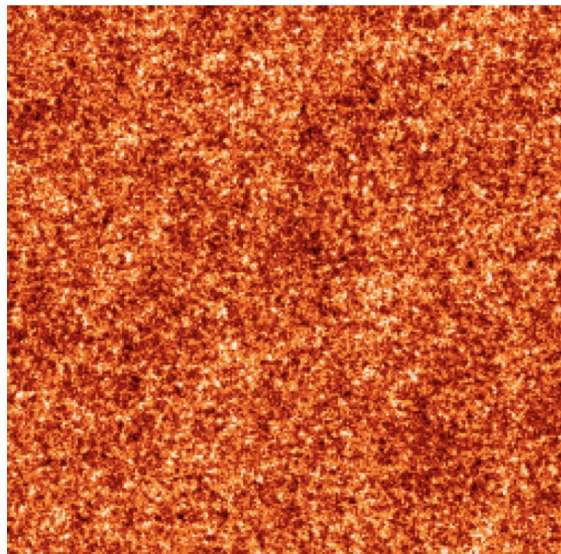
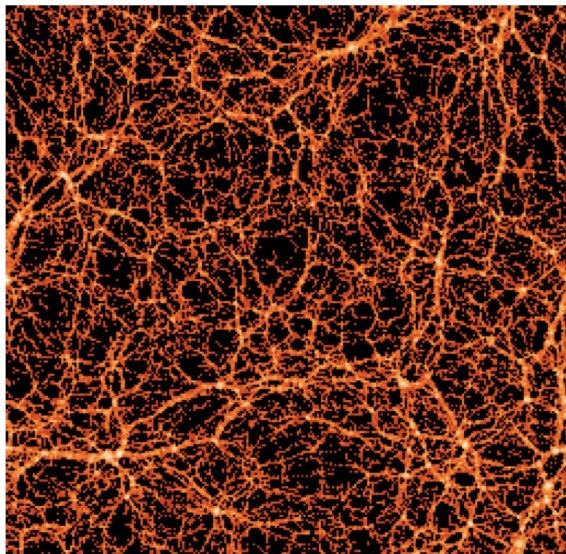
$$\tilde{\delta}(\mathbf{k}) = |\tilde{\delta}(\mathbf{k})| \exp(i\phi_{\mathbf{k}})$$

These 2 snapshots have the same $P(k)$!

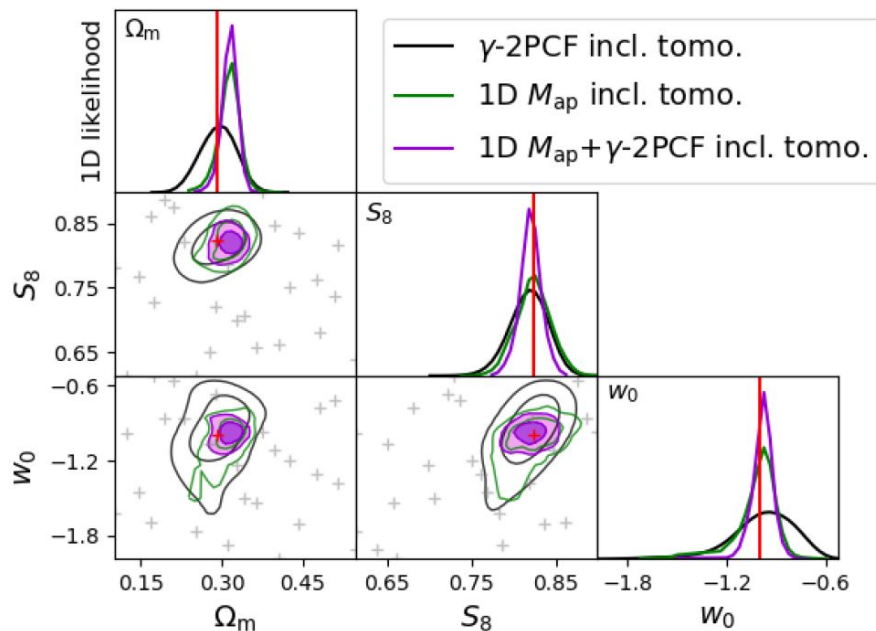
We are ignoring the cosmological information contained in these phases!

$$D_k \equiv \phi_{k+1} - \phi_k$$

Goal: access phase information with non-Gaussian statistics



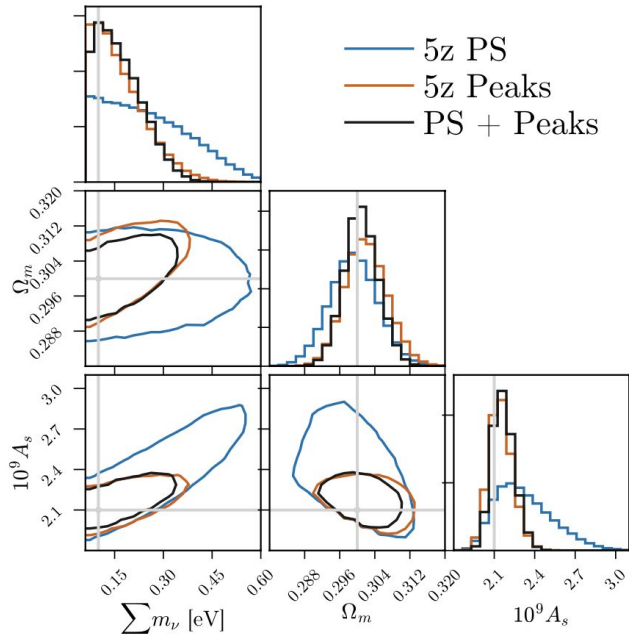
What is to gain: Dark Matter+Dark Energy



- Forecasts for 100 deg² of Euclid with a 5-slice tomography
- Constraints from PDF + shear 2PCF on w_0 are 3x smaller than 2PCF alone, 2x smaller for S_8)
- Huge potential for DE

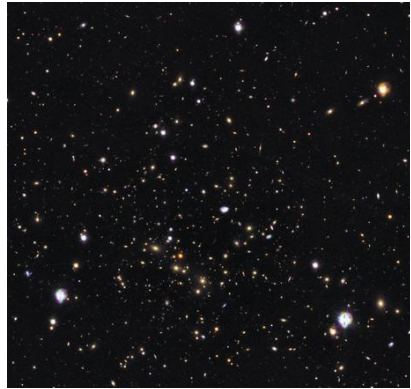
Martinet+(2020), <https://arxiv.org/abs/2010.07376>

What is to gain: Neutrino Mass



- Forecasts for LSST
- Constraints from Peaks + shear
C_{ell} on M_{nu} are 50% smaller

Cosmology with shear 2PCF



Observations

Ellipticities
(ϵ_1, ϵ_2)



Estimator: shear 2PCF

$$\hat{\xi}_{\pm}^{ij}(\theta) = \frac{\sum_{ab} w_a w_b [\epsilon_t^i(\vec{x}_a) \epsilon_t^j(\vec{x}_b) \pm \epsilon_{\times}^i(\vec{x}_a) \epsilon_{\times}^j(\vec{x}_b)]}{\sum_{ab} w_a w_b}$$

Tomography

Redshifts (z)

Calibration
(spectroscopic,
SOM, BPZ...)

Redshift
distribution:
n(z)



$$P_{\kappa}^{ij}(\ell) = \int_0^{x_H} d\chi \frac{q_i(\chi) q_j(\chi)}{[f_K(\chi)]^2} P_{\delta} \left(\frac{\ell}{f_K(\chi)}, \chi \right)$$

Systematic biases

- Shear calibration
- Mean redshift
- Intrinsic alignment
- Baryons
- etc



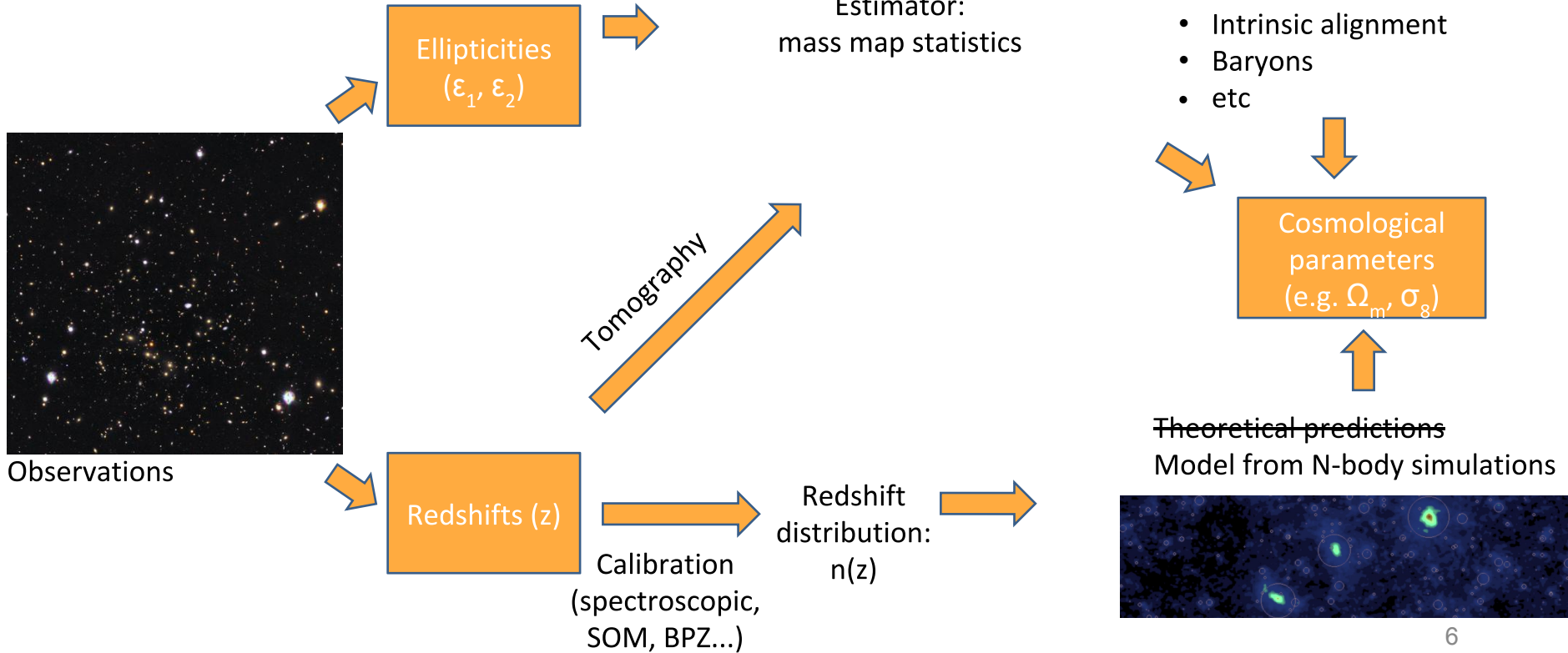
Cosmological
parameters
(e.g. Ω_m, σ_8)



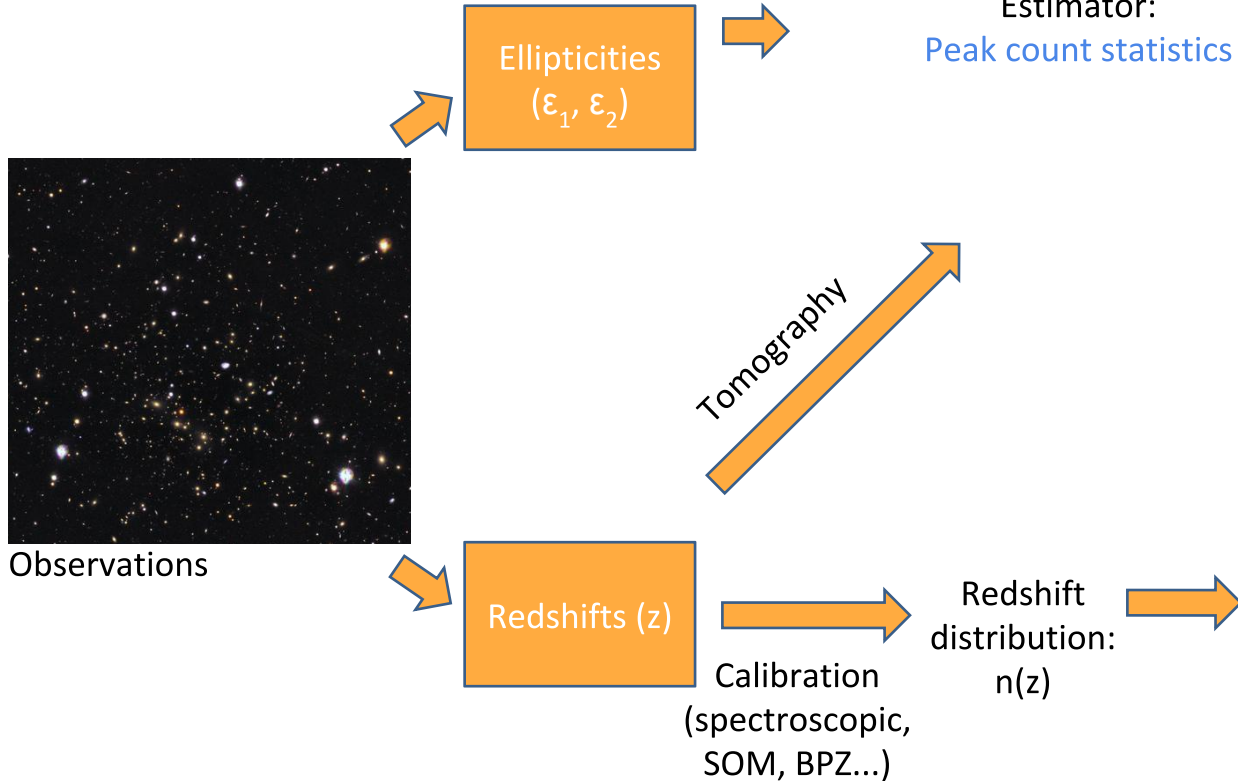
Theoretical predictions

$$\xi_{\pm}^{ij}(\theta) = \frac{1}{2\pi} \int d\ell \ell P_{\kappa}^{ij}(\ell) J_{0,4}(\ell\theta)$$

Cosmology with mass maps



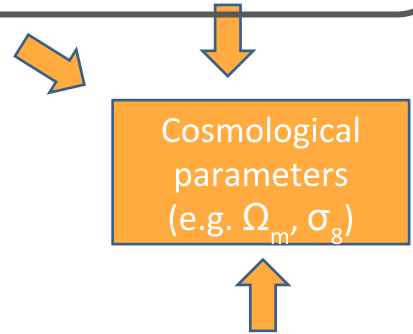
Cosmology with mass maps



This paper:

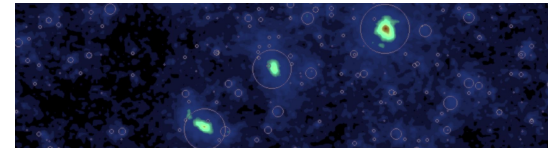
Systematic biases

- Shear calibration
- Mean redshift
- Intrinsic alignment
- Baryons
- etc



Theoretical predictions

Model from N-body simulations



Cosmological Inference

-Data: DES-Y1 (public)

-Model: cosmo-SLICS (JHD+2019)

-Covariance matrix: SLICS (JHD+2018)

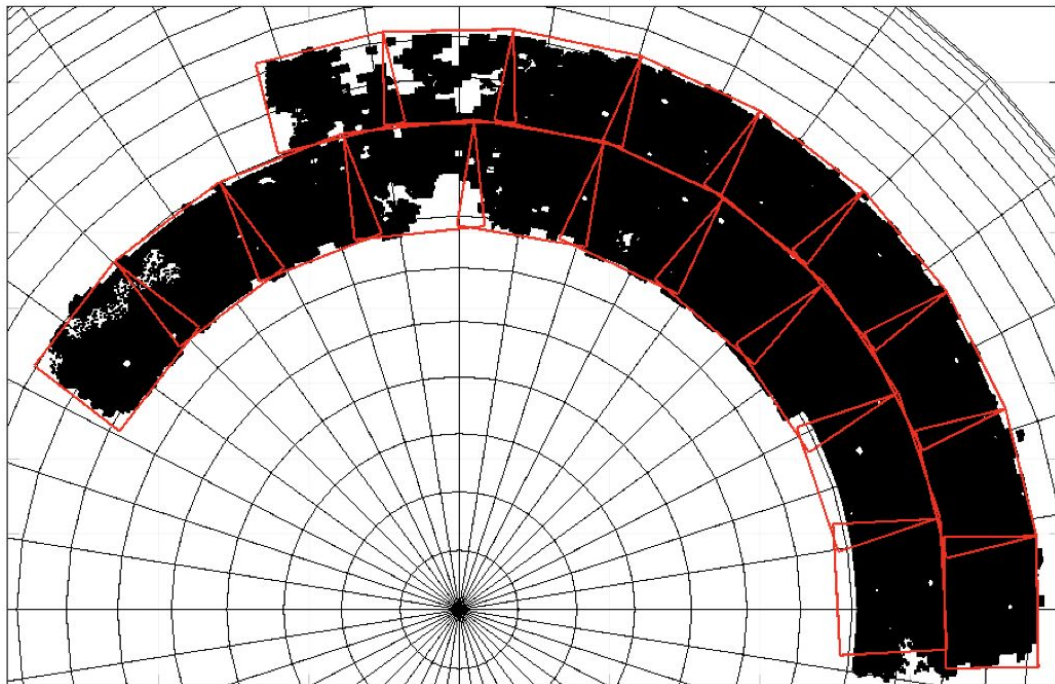
-Likelihood: cosmoSIS

$$\mathcal{L}(\boldsymbol{\pi}|\mathbf{d}) \propto \frac{N_{\text{sim}}}{2} \ln \left[1 + \chi^2 / (N_{\text{sim}} - 1) \right]$$

Sellentin & Heavens (2016)

DES-Y1 Mosaic

18 tiles or 100 sq. deg. each



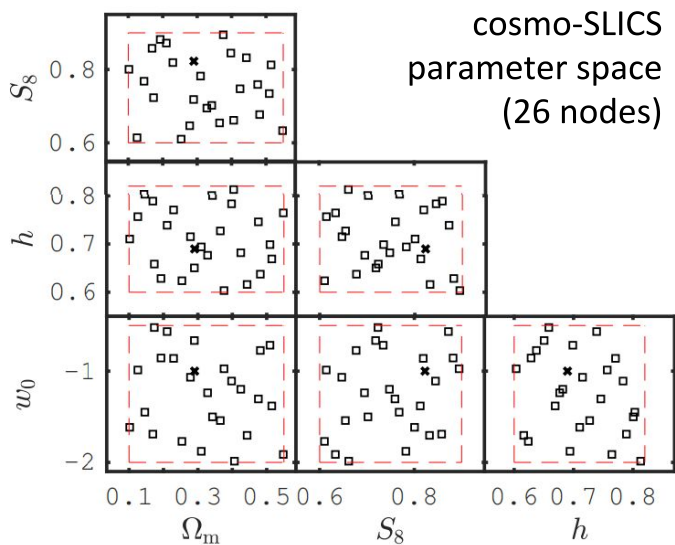
Data:

| tomo | Z_B range | No. of objects | n_{eff} | σ_ϵ | $\langle z_{\text{DIR}} \rangle$ |
|------|-------------|----------------|------------------|-------------------|----------------------------------|
| bin1 | 0.20 – 0.43 | 6,993,471 | 1.45 | 0.26 | 0.403 ± 0.008 |
| bin2 | 0.43 – 0.63 | 7,141,911 | 1.43 | 0.29 | 0.560 ± 0.014 |
| bin3 | 0.63 – 0.90 | 7,514,933 | 1.47 | 0.26 | 0.773 ± 0.011 |
| bin4 | 0.90 – 1.30 | 3,839,717 | 0.70 | 0.27 | 0.984 ± 0.009 |

Sims:

| Sim. suite | L_{box} | n_p | N_{sims} | N_{LC} | N_{cosmo} |
|----------------------|------------------------|-------------------|-------------------|--------------------|--------------------|
| cosmo-SLICS | 505 | 1536^3 | 52 | 520 | 26 |
| SLICS | 505 | 1536^3 | 124 | 124 | 1 |
| SLICS-HR | 505 | 1536^3 | 5 | 50 | 1 |
| <i>Magneticum</i> 2 | 352 | 2×1583^3 | 1 | 10 | 1 |
| <i>Magneticum</i> 2b | 640 | 2×2880^3 | 1 | 10 | 1 |
| parameter sampling | Ω_m [0.1, 0.55] | S_8 [0.6, 0.9] | h [0.6, 0.82] | w_0 [-2.0, -0.5] | |

Model: w CDM simulations

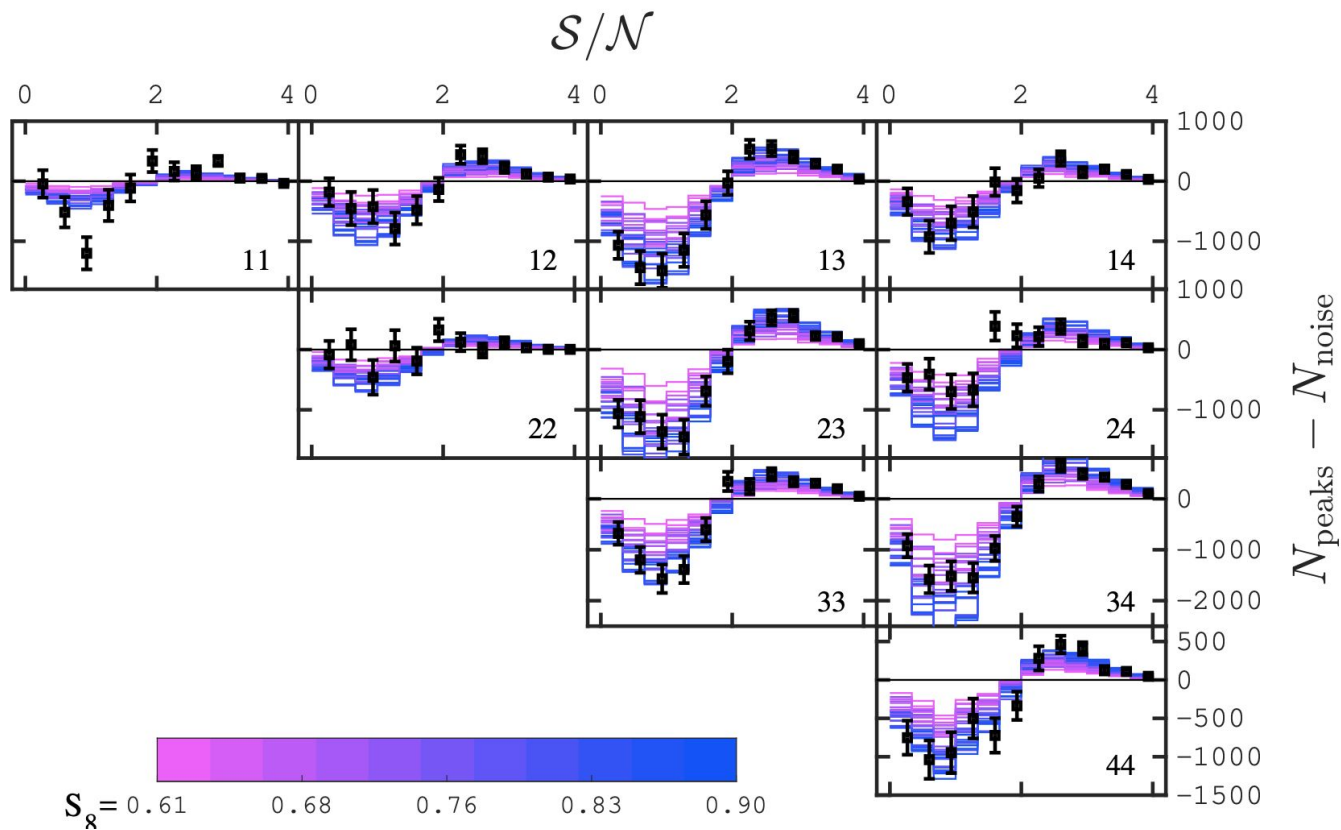


- Ray-trace the N-body suite
- Assign the 4 DES-Y1 redshift bins
- Use the positions, shapes ($|e|$) and responsivity per object
- Measure Peak Function $dN/d(\text{SNR})$
- Interpolate with a Gaussian Processes Regression Emulator

Covariance: LCDM simulations

- 1240 surveys (124 independent sims x 10 shape noise realisations)

Data vector : Peaks



Systematics

Interpolation error from the GPR

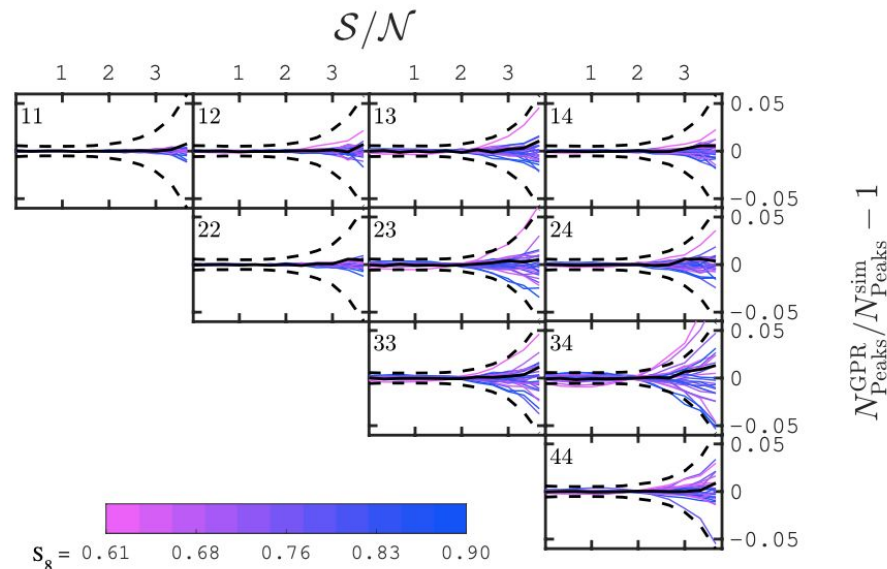
Photometric redshifts uncertainty

Shear calibration bias

Mass resolution

Baryonic feedback

Intrinsic alignments of galaxies



Systematics

Interpolation error from the GPR

Photometric redshifts uncertainty

Shear calibration bias

Mass resolution

Baryonic feedback

Intrinsic alignments of galaxies

Model with ray-tracing:

Sample 10 shifts in dm and dz

Fit each bin with a linear model

Compute $dN/d(dz)$ and $dN/d(dm)$

Marginalise in cosmoSIS

Systematics

Interpolation error from the GPR

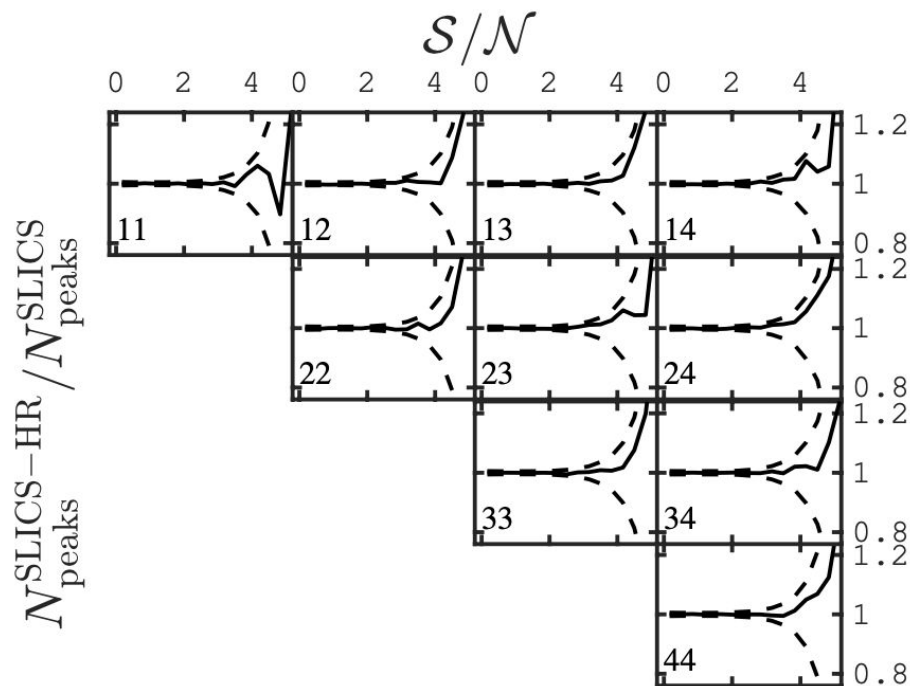
Photometric redshifts uncertainty

Shear calibration bias

Mass resolution

Baryonic feedback

Intrinsic alignments of galaxies



Systematics

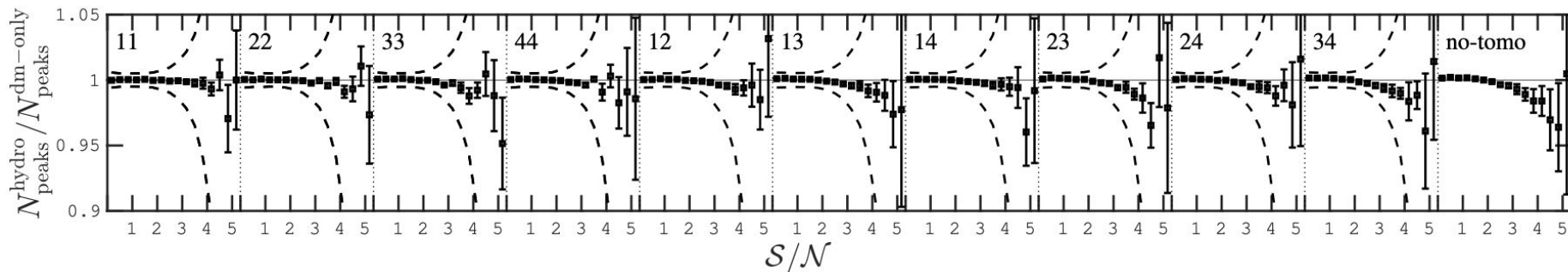
Interpolation error from the GPR

Photometric redshifts uncertainty

Shear calibration bias

Mass resolution

Baryonic feedback



Systematics

Interpolation error from the GPR

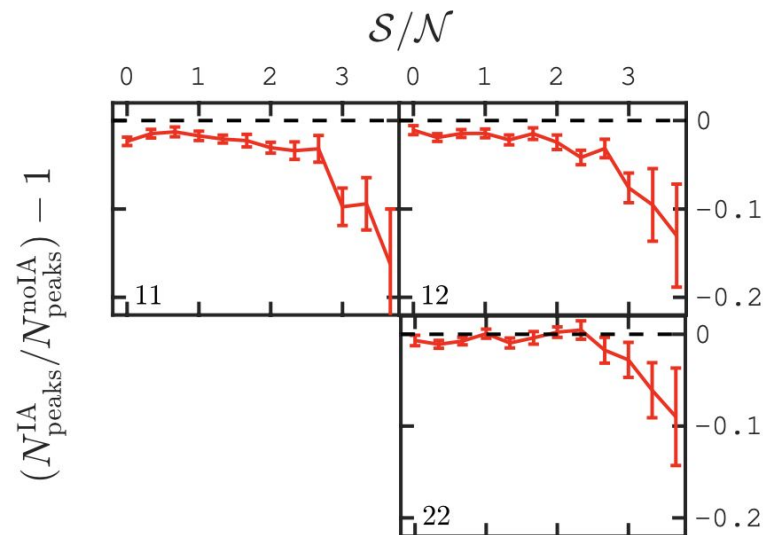
Photometric redshifts uncertainty

Shear calibration bias

Mass resolution

Baryonic feedback

Intrinsic alignments of galaxies



Systematics

Interpolation error from the GPR

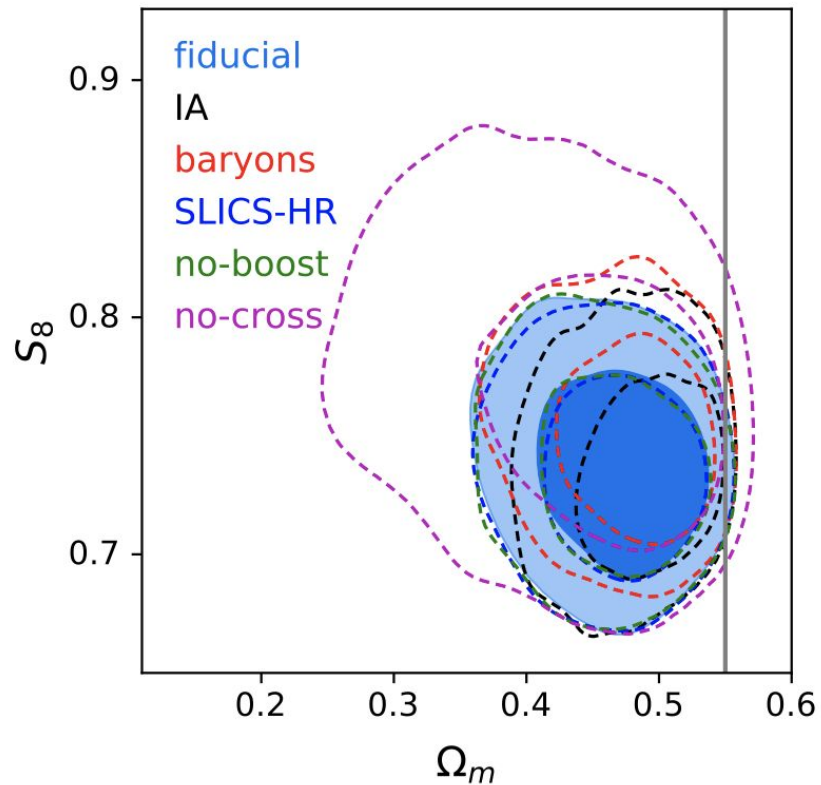
Photometric redshifts uncertainty

Shear calibration bias

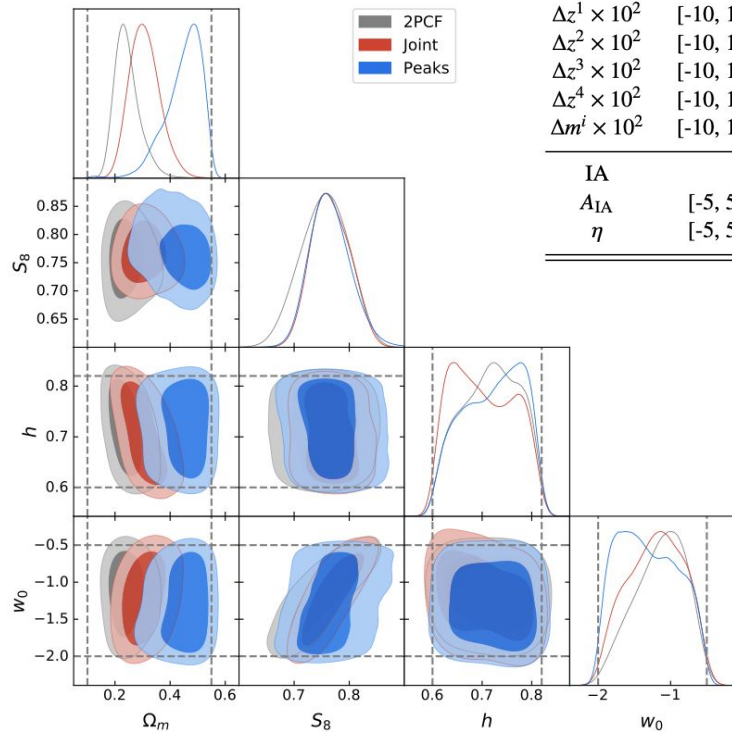
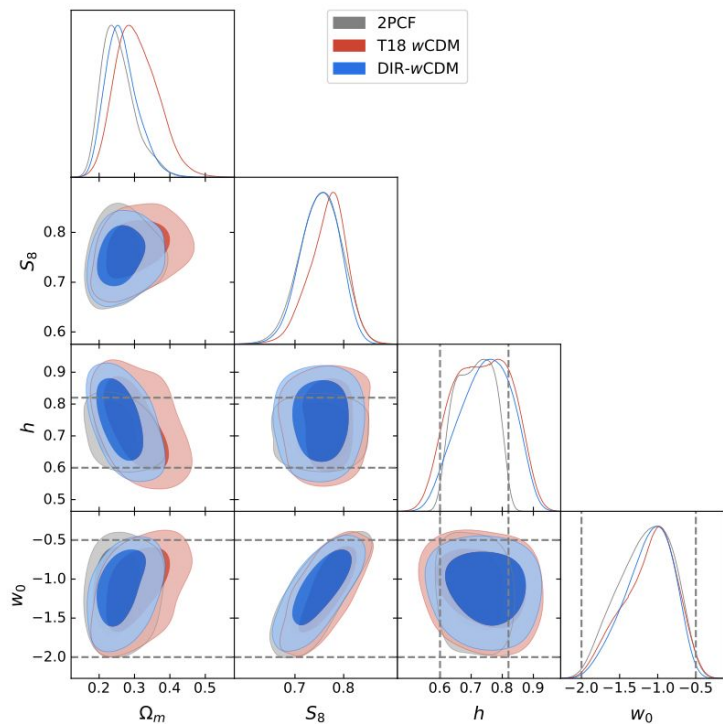
Mass resolution

Baryonic feedback

Intrinsic alignments of galaxies



Results:



| Parameter | range | prior |
|--------------------------|--------------|-------------------------|
| Cosmology | | |
| Ω_m | [0.1, 0.55] | Flat |
| σ_8 | [0.53, 1.3] | Flat |
| h | [0.6, 0.82] | Flat |
| w_0 | [-2.0, -0.5] | Flat |
| Nuisance | | |
| $\Delta z^1 \times 10^2$ | [-10, 10] | $\mathcal{G}(0, 0.8)$ |
| $\Delta z^2 \times 10^2$ | [-10, 10] | $\mathcal{G}(0, 1.4)$ |
| $\Delta z^3 \times 10^2$ | [-10, 10] | $\mathcal{G}(0, 1.1)$ |
| $\Delta z^4 \times 10^2$ | [-10, 10] | $\mathcal{G}(0, 0.9)$ |
| $\Delta m^i \times 10^2$ | [-10, 10] | $\mathcal{G}(1.2, 1.3)$ |
| IA | | |
| A_{IA} | [-5, 5] | Flat |
| η | [-5, 5] | Flat |

Results:

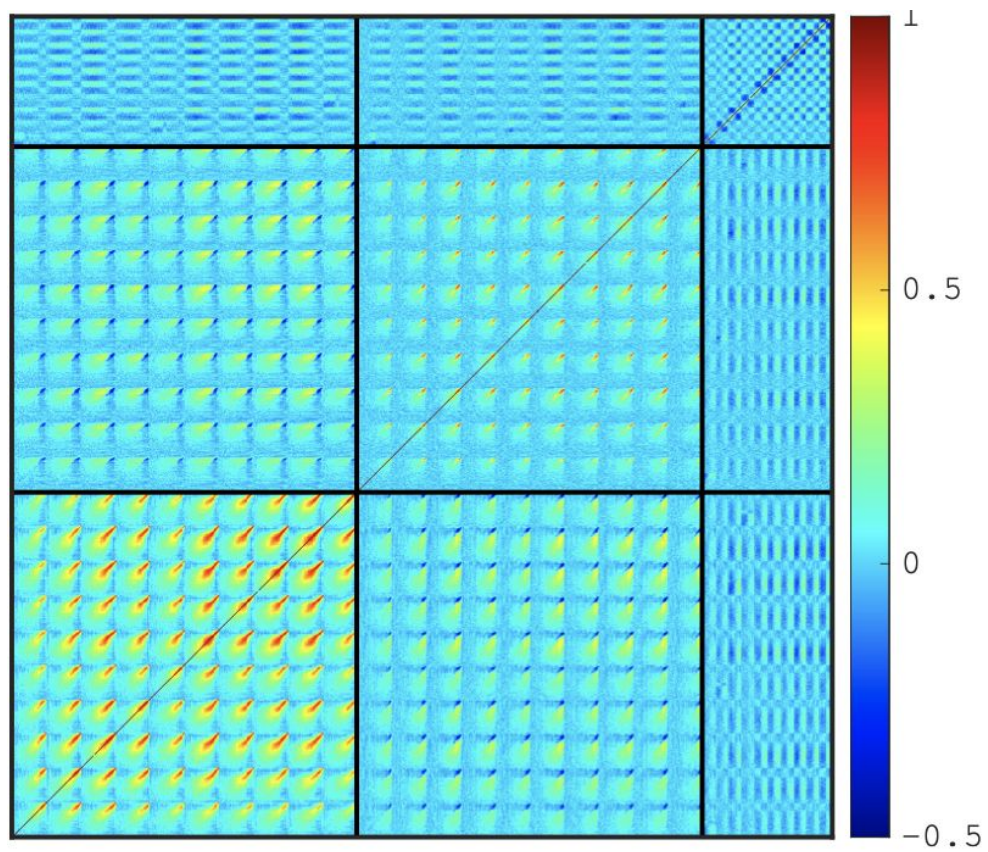
| | pipeline | S_8 | Ω_m |
|--------------------|-----------------------------------|-----------------------------|---------------------------|
| Fiducial | Peaks | $0.780^{+0.019}_{-0.056}$ | - |
| | 2PCF | $0.753^{+0.043}_{-0.043}$ | $0.254^{+0.033}_{-0.056}$ |
| | Joint | $0.766^{+0.033}_{-0.038}$ | - |
| Variations | 2PCF (T18, w CDM) | $0.797^{+0.037}_{-0.037}$ | $0.290^{+0.079}_{-0.051}$ |
| | 2PCF (DIR- w CDM) | $0.752^{+0.042}_{-0.037}$ | $0.264^{+0.035}_{-0.054}$ |
| | 2PCF (Λ CDM) | $0.761^{+0.027}_{-0.027}$ | $0.272^{+0.031}_{-0.056}$ |
| | 2PCF (T18, Λ CDM) | $0.792^{+0.032}_{-0.021}$ | $0.304^{+0.038}_{-0.062}$ |
| | 2PCF (J20, Λ CDM) | $0.765^{+0.036}_{-0.031}$ | $0.252^{+0.041}_{-0.086}$ |
| | Peaks (cross-tomo, with IA) | $0.735^{+0.024}_{-0.032}$ | - |
| | Peaks (cross-tomo, with baryons) | $0.750^{+0.026}_{-0.031}$ | - |
| | Peaks (cross-tomo, with SLICS-HR) | $0.734^{+0.025}_{-0.032}$ | - |
| | Peaks (cross-tomo, no-boost) | $0.736^{+0.025}_{-0.032}$ | - |
| | Peaks (cross-tomo) | $0.737^{+0.027}_{-0.031}$ | - |
| | Joint (cross-tomo) | $0.743^{+0.024}_{-0.024}$ | - |
| | Mocks | Peaks (cross-tomo, no syst) | $0.787^{+0.024}_{-0.024}$ |
| Peaks (cross-tomo) | | $0.776^{+0.045}_{-0.045}$ | $0.297^{+0.048}_{-0.066}$ |
| 2PCF (FID) | | $0.772^{+0.042}_{-0.042}$ | $0.314^{+0.049}_{-0.070}$ |

Conclusions: Map statistics are powerful!

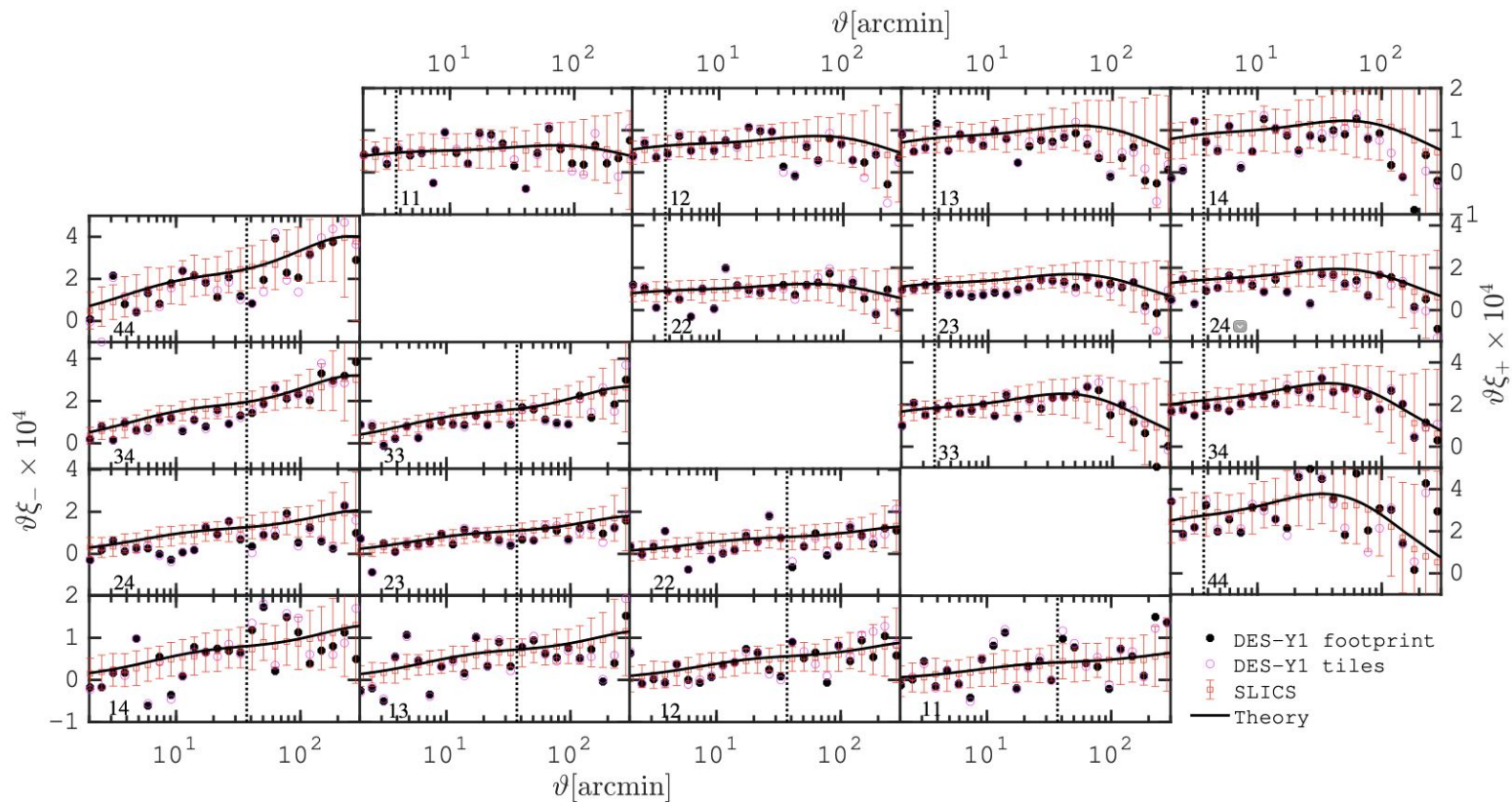
- 1D Map outperforms peaks, voids, and shear-2PCF
- Tomography with cross-bins improves the forecast precision by 50% compared to previous tomography
- 1D Map + shear-2PCF is twice better than shear-2PCF alone on the S8 forecast precision
- First combined forecasts on w_0 : 1D Map + shear-2PCF almost three times better than shear-2PCF
- Next: Baryons and IA (ongoing). If we want to get serious about this, we need to list the requirements for percent level accuracy, estimate the resources needed for new simulations, and establish a road map.

Additional Slides

Covariance Matrix



Data vector : 2PCF



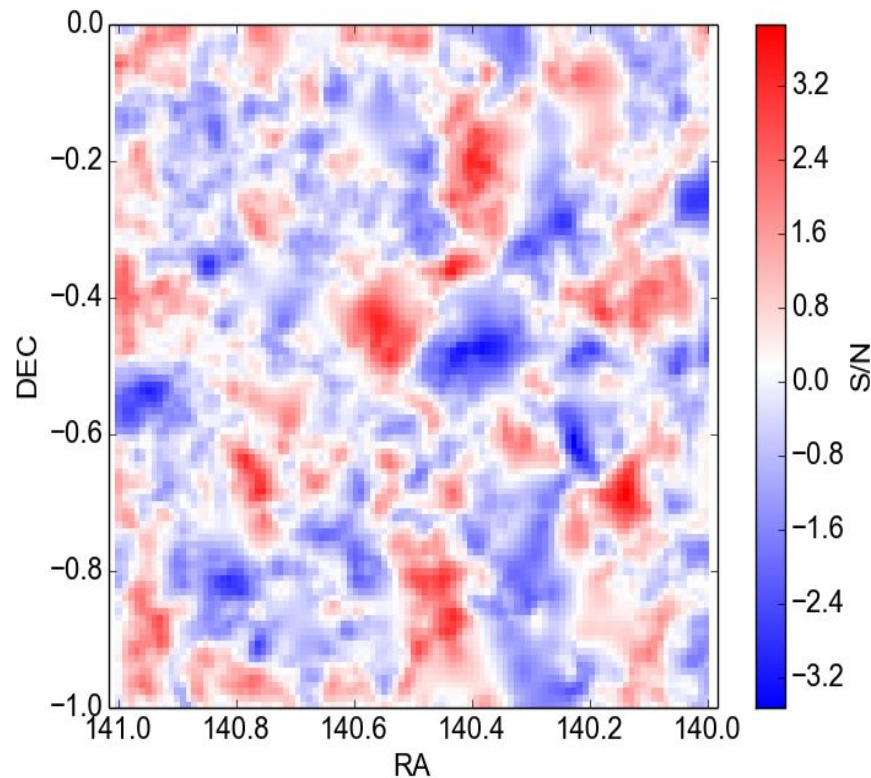
Aperture mass map

$$M_{\text{ap}}(\boldsymbol{\theta}_0) = \frac{1}{n_{\text{gal}}} \sum_i Q(|\boldsymbol{\theta}_i - \boldsymbol{\theta}_0|) \epsilon_t(\boldsymbol{\theta}_i, \boldsymbol{\theta}_0)$$

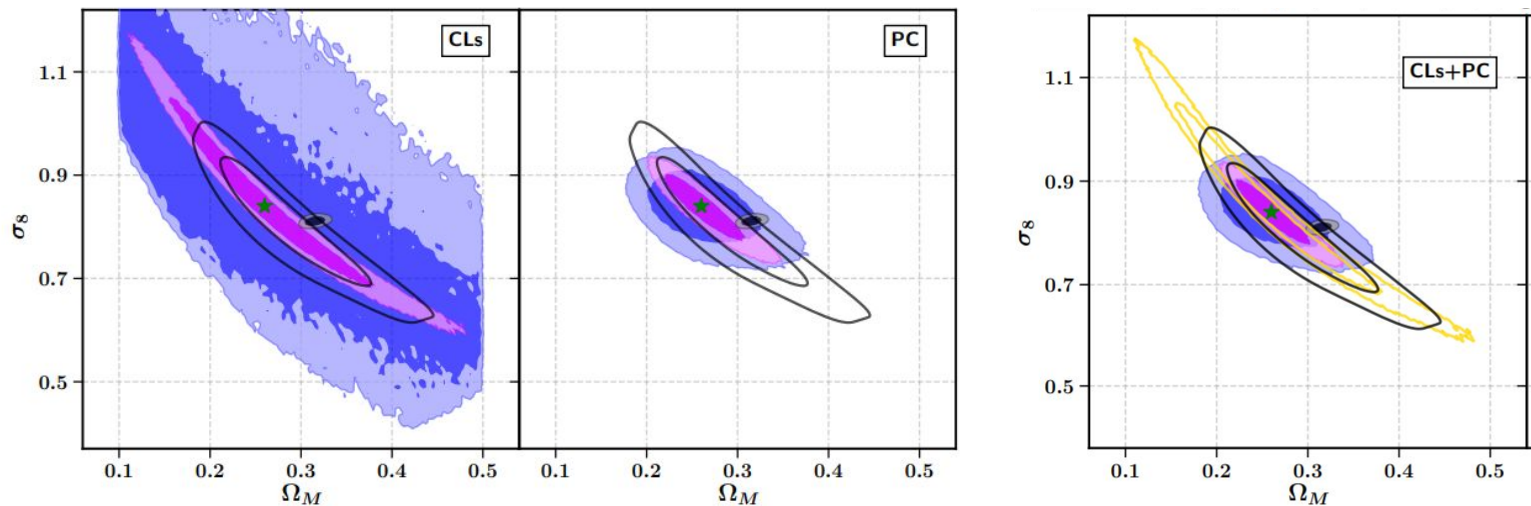
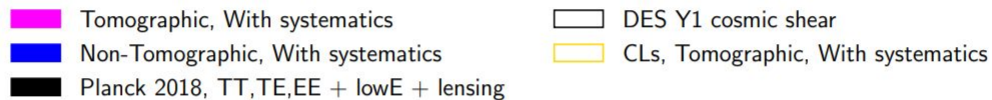
$$\epsilon_t(\boldsymbol{\theta}, \boldsymbol{\theta}_0) = -\Re \left[\hat{\epsilon}(\boldsymbol{\theta}) e^{-2i\phi(\boldsymbol{\theta}, \boldsymbol{\theta}_0)} \right]$$

$$\sigma(M_{\text{ap}}(\boldsymbol{\theta}_0)) = \frac{1}{\sqrt{2}n_{\text{gal}}} \left(\sum_i |\hat{\epsilon}(\boldsymbol{\theta}_i)|^2 Q^2(|\boldsymbol{\theta}_i - \boldsymbol{\theta}_0|) \right)^{1/2}$$

$$\frac{S}{N}(\boldsymbol{\theta}_0) = \frac{\sqrt{2} \sum_i Q(|\boldsymbol{\theta}_i - \boldsymbol{\theta}_0|) \epsilon_t(\boldsymbol{\theta}_i, \boldsymbol{\theta}_0)}{\sqrt{\sum_i |\hat{\epsilon}(\boldsymbol{\theta}_i)|^2 Q^2(|\boldsymbol{\theta}_i - \boldsymbol{\theta}_0|)}}$$



DES-Yr3 peak prediction with tomography (Zürcher et al. 2020)



- Constraints on S_8 improved by 25% with tomography
- Here, tomography works better for 2PCF than peaks *because of redshift bin cross-correlations*